

A Lutin Tutorial

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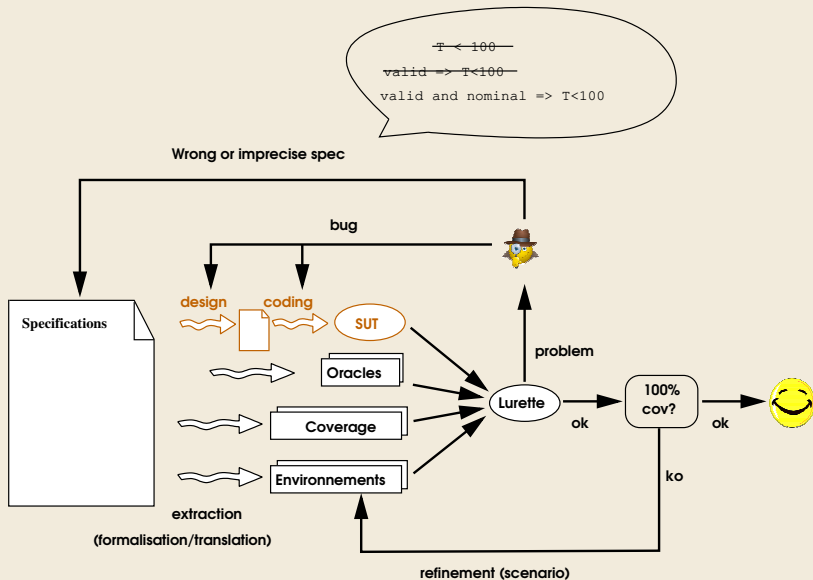
Outline

- 1 Forewords
- 2 Execute Lutin programs
- 3 The Lutin Language
- 4 The `run` operator
- 5 Advanced examples

Plan

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Motivations: testing reactive programs



Lutin in one slide

- Lustre-like: Dataflow, parallelism, modular, logic time, pre.
- But not exactly Lustre though
 - ▶ Plus
 - **Control structure** operators (regular expressions)
 - **Stochastic** (controlled and pseudo-Aleatory)
 - ▶ Minus
 - No implicit top-level loop
 - No topological sort of equations

In order to run this tutorial

You first need to install opam. For instance, on debian-like boxes do

```
sudo apt-get install opam
opam init ; opam switch 4.04.0 ; eval `opam config env`
```

and then do:

```
sudo apt-get install gnuplot tcl
opam repo add verimag-sync-repo "http://www-verimag.imag.fr/DIST-TOOLS/SYNCHRONE/op
opam update
opam install lutin
```

and also the Lustre V4 distribution (for luciole and sim2chro)
<http://www-verimag.imag.fr/DIST-TOOLS/SYNCHRONE/lustre-v4/distrib/index.html>

```
<prompt> echo "go!"
```

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Stimulate Lutin programs

- A program that increments its input

Let's consider the following Lutin program named `incr.lut`.

```
node incr(x:int) returns (y:int) =
  loop [10] y = x+1
```

```
<prompt> lutin incr.lut
```

- A program with no input

```
node one() returns (y:int) =
  loop y = 1
```

```
<prompt> lutin -l 5 one.lut
```

- Be quiet

```
<prompt> lutin -l 5 -quiet one.lut
```


Stimulate Lutin programs graphically with `luciole`

```
node incr(x:int) returns (y:int) =  
  loop [10] y = x+1
```

```
<prompt> luciole-rif lutin incr.lut
```

Store and Display the produced data: `sim2chro` and `gnuplot-rif`

- Generate a RIF file

It is possible to store the lutin RIF output into a file using the `-o` option.

```
<prompt> lutin -l 10 -o ten.rif N.lut ; ls -lh ten.rif
```

```
node N() returns (y:int) =  
  y = 0 fby loop y = pre y+1
```

- Visualize a RIF file

```
<prompt> cat ten.rif
```

- Visualize a RIF file (bis)

```
<prompt> cat ten.rif | sim2chrogtk -ecran > /dev/null
```

- Visualize a RIF file (ter)

```
<prompt> gnuplot-rif ten.rif
```

Automatic stimulation of Lutin programs

```
node incr(x:int) returns (y:int) =
  loop y = x+2
node decr(y:int) returns (x:int) =
  x = 42 fby loop x = y-1
```

```
<prompt> lurette -sut "lutin decr.lut -n incr" -env "lutin
decr.lut -n decr" -o res.rif
```

```
<prompt> sim2chrogtk -ecran -in res.rif > /dev/null
```



- I've bought 2 electronic chess games
- connected one to another
- And now I'm at peace

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Back to programs of Section 1

- Let's come back to the Lutin programs mentioned so far.

```
node incr(x:int) returns (y:int) =  
  loop [10] y = x+1
```

- Those programs illustrate the 2 kinds of expressions we have in Lutin.
 - ▶ **constraint expressions** ($y = x+1$) that asserts facts outputs variables.
 - ▶ **trace expression** (`loop <te>`) that allows one to combine constraint expressions.

Non deterministic programs

- A First non-deterministic program

```
node trivial() returns(x:int; f:real ; b:bool) =  
  loop true
```

```
<prompt> lutin -l 10 -q trivial.lut
```

- It is possible to set the variable range at declaration time, as done in trivial2.lut:

```
node trivial() returns(x:int [-100;100];  
                      f:real [-100.0;100.0];b:bool)=  
  loop true
```

```
<prompt> lutin -l 10 -q trivial2.lut
```

Non deterministic programs (cont)

Now consider the range.lut program:

```
node range() returns (y:int) = loop 0 <= y and y <= 42
```

```
<prompt> lutin range.lut -l 10 -q
```

- Linear constraints \rightarrow union of convex polyhedra
- Several heuristics are defined to perform the solution draw
- `--step-inside (-si)`: draw inside the polyhedra (the default)
- `--step-vertices (-sv)` draw among the polyhedra vertices
- `--step-edges (-se)`: promote edges

```
<prompt> lutin range.lut -l 10 -q -step-vertices
```

Non deterministic programs (cont)

- A 3D non-deterministic example

```
node polyhedron() returns(a,b,c:real) =  
  loop (0.0 < c and c < 4.0 and  
    a + 1.0 * b > 0.0 and  
    a + 1.0 * b - 3.0 < 0.0 and  
    a - 1.0 * b < 0.0 and  
    a - 1.0 * b + 3.0 > 0.0)
```

```
<prompt> lutin polyhedron.lut -l 1000 -q > poly.data;  
echo 'set point 0.2; splot "poly.data" using 1:2:3;pause  
mouse close'| gnuplot
```

- One can observe the effect of `-step-edges`
and `-step-vertices` options on the repartition of generated points

Non deterministic programs (cont)

Constraint may also depend on inputs.

```
node range_bis(i:int) returns (y:int) =  
  loop 0 <= y and y <= i
```

```
<prompt> luciole-rif lutin range-bis.lut
```

Controlled non-determinism: the choice operator

```
node choice() returns(x:int) =
  loop {
    | x = 42
    | x = 1
  }
```

`<prompt> lutin -l 10 -q choice.lut`

It is possible to favor one branch over the other using weight directives (:3):

```
node choice() returns(x:int) =
  loop {
    |3: x = 42
    |1: x = 1
  }
```

In choice2.lut, x=42 is chosen with a probability of 3/4.

`<prompt> lutin -l 10000 -q choice2.lut | grep 42 | wc -l`

Controlled non-determinism: the choice operator

```
node choice(b:bool) returns(x:int) =  
  x=0 fby  
  x=-15 fby  
  loop {  
    |1: x = 1 and b  
    |9: x = 2 and b  
    | x = 3 and not b  
  }
```

```
<prompt> luciole-rif lutin choice3.lut
```

Combinators

A *combinator* is a well-typed macro that eases code reuse. One can define a combinator with the `let/in` statement, or just `let` for top-level combinators.

- A simple combinator

```
let n = 3

node foo() returns (i:int) =
  loop [3] 0<= i and i < n fby
  let s=10 in
  loop [3] s<= i and i < s+n
```

```
<prompt> lutin -quiet letdef.lut
```

A parametric combinator

The combinator.lut program illustrates the use of parametric combinators:

```
let within(x, min, max: int): bool =  
  (min <= x) and (x <= max)  
  
node random_walk() returns (y:int) =  
  within(y,0,100) fby loop within(y,pre y-1,pre y+1)
```

```
<prompt> lutin -l 100 combinator.lut -o walk.rif ;  
gnuplot-rif walk.rif
```

Combinators (cont)

- A combinator that needs memory (ref)

```

let within(x, min, max: real) :bool = (min <= x) and (x <= max)
let up (delta:real;x:real ref):bool = within(x,pre x,pre x+delta)
let down(delta:real;x:real ref):bool = within(x,pre x-delta,pre x)
node up_and_down(min,max,d:real) returns (x:real) =
  within(x, min, max) fby
  loop {
    | loop { up (d, x) and pre x < max }
    | loop { down(d, x) and pre x > min }
  }

```

<prompt> luciole-rif lutin up-and-down.lut

<prompt> gnuplot-rif luciole.rif

Question: *what happens if you guard the `up` combinator by `x < max` instead of `pre x < max`?*

Local variables

Sometimes, it is useful to use auxiliary variables that are not output variables. Such variables can be declared using the `exist/in` construct. Its use is illustrated in the `true-since-n-instants.lut` program:

```
let n = 3
node ok_since_n_instants(b:bool) returns (res:bool) =
  exist cpt: int = n in
    loop {
      cpt = (if b then (pre cpt-1) else n) and
      res = (b and (cpt <= 0))
    }
```

```
<prompt> luciole-rif lutin true-since-n-instants.lut
```

Local variables again

Local variables can also plain random variables, as illustrated the local.lut program:

```
node local() returns(x:real = 0.0) =
  exist target : real in
  loop {
    0.0 < target and target < 42.0 and x = pre x
    fby
    loop [20] { x = (pre x + target) / 2.0 and
                target = pre target }
  }
```

```
<prompt> lutin local.lut -l 100 -o local.rif ; gnuplot-rif
local.rif
```

Question: modify the previous program so that x reaches the target after a damped oscillation

Damped oscillation

```
node local() returns(target, x:real = 0.0) =
  exist px : real = 0.0 in -- Because pre pre x is currently not supported in Lutin
  assert px = pre x in
  loop {
    0.0 < target and target < 42.0 and x = pre x
    fby
    loop [20] {
      x = (pre x + target) / 2.0
        + 0.6*(px - pre px) -- adding inertia...
      and
      target = pre target
    }
  }
}
```

Distribute a constraint into a scope: assert

Consider for instance the true-since-n-instants2.lut program:

```
node ok_since_n_instants(b:bool;n:int)returns(res:bool)=
  exist cpt: int in
    cpt = n and res = (b and (cpt <= 0))
  fby
    loop {
      cpt = (if b then (pre cpt-1) else n) and
      res = (b and (cpt <= 0))
    }
```

- One flaw is that $res = (b \text{ and } (cpt \leq 0))$ is duplicated.
- $\text{assert } \langle ce \rangle \text{ in } \langle te \rangle \equiv \langle te' \rangle$,
where $\langle te' \rangle = \langle te \rangle [c/c \text{ and } ce]_{\forall c \in \mathcal{C} \text{ onstraints}(te)}$

Question: Rewrite the true-since-n-instants2.lut using the assert/in construct and avoid code duplication.

Answer

External code

Lutin program can call any function defined in a shared library (.so)

```
extern sin(x: real) : real
let between(x, min, max : real) : bool = ((min < x) and (x < max))
node bizzare() returns (x,res: real) =
  exist noise: real in
  assert between(noise,-0.1, 0.1) in
  res = 0.0 and x = 0.0 fby
  loop x = pre x + 0.1 + noise
    and res = sin(pre x)
```

```
<prompt> lutin -L libm.so -l 200 ext-call.lut -o
ext-call.rif;gnuplot-rif ext-call.rif
```

Exceptions

- Global exceptions can be declared outside the main node:

```
exception ident
```

- or locally within a trace statement:

```
exception ident in st
```

- An existing exception ident can be raised with the statement:

```
raise ident
```

- An exception can be caught with the statement:

```
catch ident in st1 do st2
```

If the exception is raised in st1, the control immediately passes to st2. If the “do” part is omitted, the statement terminates normally.

Exceptions (cont)

- The predefined Deadlock exception can only be caught

```
catch Deadlock in st1 do st2
```



```
try st1 do st2
```

- If a deadlock is raised during the execution of st1, the control passes immediately to st2. If st1 terminates normally, the whole statement terminates and the control passes to the sequel.

Exceptions (cont)

```
node toto(i:int) returns (x:int)=  
  loop {  
    exception Stop in  
    catch Stop in  
      loop [1,10] x = i fby raise Stop fby x = 43  
      do x=42  
  }
```

<prompt> `luciole-rif lutin except.lut`

Note that the 43 value is generated iff $i=43$.

Combinators (again)

- Trace Combinators

```
let myloop(t:trace) : trace = loop try loop t
```

Here we restart the loop from the beginning whenever we are blocked somewhere inside `t`. (`myloop.lut`)

```
let myloop(t:trace) : trace = loop try loop t
node use_myloop(reset:bool) returns(x:int) =
  myloop(
    x = 0 fby
    assert not reset in
    x = 1 fby
    x = 2 fby
    x = 3 fby
    x = 4
  )
```

```
<prompt> luciole-rif lutin myloop.lut
```

Parallelism: &>

```
node n(i:int) returns(x,y:int) = {
  loop { -i < x and x < i }
  &> y = 0 fby loop { y = pre x } }
```

<prompt> `luciole-rif lutin paralel.lut`

nota bene: this construct can be expensive because of:

- **the control structure**: such a product is equivalent to an automata product, which, in the worst case, can be quadratic;
- **the data**: the polyhedron resolution is exponential in the dimension of the polyhedron.

Use the `run/in` construct instead if performance is a problem.

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Cheap parallelism: Calling Lutin nodes `run/in`

The idea is the following: when one writes:

```
run (x,y) := foo(a,b) in
```

in order to be accepted the following rules must hold:

- `a` and `b` be uncontrollable variables (e.g., inputs or memories)
- `x` and `y` should be controllable variables (e.g., outputs or locals)
- in the scope of such a `run/in`, `x` and `y` becomes uncontrollable.

nb : it is exactly the parallelism of Lustre, with an heavier syntax. In Lustre, one would simply write

```
(x,y)=foo(a,b);
```

Moreover in Lutin, the order of equations matters.

Cheap parallelism: Calling Lutin nodes `run/in`

- The `run/in` construct is another (cheaper) way of executing code in parallel
- The only way of calling Lutin nodes.
- Less powerful: constraints are not merged, but solved in sequence

```
include "N.lut"  
include "incr.lut"  
node use_run() returns(x:int) =  
  exist a,b : int in  
    run a := N() in  
    run b := incr(a) in  
    run x := incr(b) in  
    loop true
```

```
<prompt> lutin -l 5 -q run.lut -m use_run
```

Why does the `run/in` statement is important?

Using combinators and `&>`, it was already possible to reuse code, but `run/in` is

- Much more efficient: polyhedra dimension is smaller
- Mode-free (args can be in or out) combinators are error-prone

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Wearing sensors

The `sensors.lut` program that makes extensive use of the `run` statements.

```
<prompt> luciole-rif lutin sensors.lut -m main
```

Waiting for the stability of a signal

- Defining and checking the stability of a variable (in particular in presence of noise) is not that easy.
- One definition could be that a variable is stable if it remains within an interval during a certain amount of time. More precisely:

A variable V is (d,ε) -stable at instant i if there exists an interval I of size ε , such that, for all n in $[i-d,i]$, $V(n)$ is in I .

$$\exists I, \text{st } |I| = \varepsilon, \forall n \in [i-d, i] V(n) \in I$$

The Lutin version

```
<prompt> luciole-rif lutin is_stable.lut -m is_stable
```