

Problem

Your goal is to complete a model of the Needham-Schroeder-Lowe protocol in Tamarin (its Alice-Bob notation is given below).

1. $I \rightarrow R: \{ '1', ni, I \}_{pk(R)}$
2. $I \leftarrow R: \{ '2', ni, nr, R \}_{pk(I)}$
3. $I \rightarrow R: \{ '3', nr \}_{pk(R)}$

where:

- * $pk(X)$ - long-term public key of X
- * ni - nonce generated by I (once per session)
- * nr - nonce generated by R (once per session)
- * the goal is to exchange the nonces ni and nr as fresh shared secrets

In this protocol, each party A has a long-term private key $ltkA$ and a corresponding public key $pk(A) = Pk(A, ltkA)$. An asymmetric encryption scheme is used, and $\{m\}_{pk(A)}$ denotes the encryption of message m with the public key of A .

To start a session, the initiator I first creates a fresh nonce ni . He then concatenates ni with its I 's identity, encrypts the result using the public key of R , and sends it to R . The responder R stores the received value, generates a fresh nonce nr , concatenates ni with nr and its own identity, encrypts the result using the public key of I , and sends it to I . Finally, the initiator sends back to the responder the encryption of nr . After a completed session, both parties assume that the nonces nr and nr are fresh and secret. The incomplete modelization you should consider is given in Figures 1 and 2. Exercises:

1. Can you formulate an "executable" lemma in Tamarin that says that both participants (an initiator and a responder) can complete a session (even if the adversary does not corrupt anyone)?

Hint: You should use an "exists-trace" assertion that uses the predicates $OUT...(...)$, $IN...(...)$ and $RevLtk(...)$.

2. Can you formulate a "secrecy_claim" lemma in Tamarin that models the secrecy property of the generated nonces (with respect to a session where both participants are not corrupted) ?

Hint: The assertion should use the predicates $Secret(...)$, $K(...)$ and $RevLtk(...)$.

3. We recall the definition of (perfect) forward secrecy: compromise of long-term keys of a set of principals does not compromise the session secrets established in previous protocol runs involving those principals. Can you formulate a "PFS_securety_claim" lemma that models the PFS secrecy property of the session secrets?

Hint: You should complete the previous lemma by allowing the adversary to corrupt the involved participants after the completion of the target session.

4. Can you complete the rules of the protocol and formulate a "PFS_securety_claim_I" lemma that models the PFS secrecy property of the session secrets from the point of view of the initiator?

Hint: You should add an action fact $SecretI(...)$ on one of the rules corresponding to the side of the initiator.

5. Complete the rules of the protocol such that the lemma "injective_agree" should correspond to the Injective agreement property from the perspective of both the initiator and the responder.

Hint: You should add action facts $Commit(...)$ and $Running(...)$ on the right rules.

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theory NSLPK
begin
builtins: asymmetric-encryption
/* . Protocol: The Needham-Schroeder-Lowe Public Key Protocol */

// Public key infrastructure
rule Register_pk:
  [ Fr(~ltkA) ] --> [ !Ltk($A, ~ltkA), !Pk($A, pk(~ltkA)), Out(pk(~ltkA)) ]

rule Reveal_ltk:
  [ !Ltk(A, ltkA) ] --[ RevLtk(A) ]-> [ Out(ltkA) ]

/* We formalize the following protocol
protocol NSLPK
  1. I -> R: {'1',ni,I}pk(R)
  2. I <- R: {'2',ni,nr,R}pk(I)
  3. I -> R: {'3',nr}pk(R)
*/

rule I_1:
  let m1 = aenc{'1', ~ni, $I}pkR in
  [ Fr(~ni) , !Pk($R, pkR) ] --[ OUT_I_1($I, $R, ~ni) ]->
  [ Out( m1 ) , St_I_1($I, $R, ~ni) ]

rule R_1:
  let m1 = aenc{'1', ni, I}pk(ltkR) m2 = aenc{'2', ni, ~nr, $R}pkI in
  [ !Ltk($R, ltkR) , In( m1 ) , !Pk(I, pkI) , Fr(~nr) ]
  --[ IN_R_1( $R, I, ni ) , OUT_R_1( $R, I, ni, ~nr ) ]->
  [ Out( m2 ) , St_R_1($R, I, ni, ~nr) ]

rule I_2:
  let m2 = aenc{'2', ni, nr, R}pk(ltkI) m3 = aenc{'3', nr}pkR in
  [ St_I_1(I, R, ni) , !Ltk(I, ltkI) , In( m2 ) , !Pk(R, pkR) ]
  --[ IN_I_2( I, R, ni, nr), OUT_I_2(I, R, nr), Secret(I,R,nr), Secret(I,R,ni) ]->
  [ Out( m3 ) ]

rule R_2:
  let m3 = aenc{'3', nr}pk(ltkR) in
  [ St_R_1(R, I, ni, nr) , !Ltk(R, ltkR) , In( m3 ) ]
  --[ IN_R_2( R, I, nr ) , Secret(R, I, ni), Secret(R, I, nr) ]->
  [ ]

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Figure 1: A Model of NSLPK

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/* 1. */
lemma executable:
  ...

/*2. If there exists a session whose one secret s is known to the Adversary,
then the long term key of one of the two participants involved in that session was revealed */
lemma secrecy_claim:
  ...

/*3. If there exists a session whose one secret s is known to the Adversary, then the long term key
of one of the two participants involved in that session was revealed before that session */
lemma PFS_secrecy_claim:
  ...

/*4. If there exists a session where the initiator has accepted a secret s and s is known to the
Adversary, then the long term key of one of the two participants involved in that session
was revealed before that session */
lemma PFS_secrecy_claim_I:
  ...

//5. Injective agreement from the perspective of both the initiator and the responder.
lemma injective_agree:
  " /* Whenever somebody commits to running a session, then*/
  All actor peer params #i. Commit(actor, peer, params) @ i
  ==>
  /* there is somebody running a session with the same parameters */
  (Ex #j. Running(actor, peer, params) @ j & j < i
  /* and there is no other commit on the same parameters */
  & not(Ex actor2 peer2 #i2. Commit(actor2, peer2, params) @ i2 & not(#i = #i2))
  )
  /* or the adversary perform a long-term key reveal on actor or peer */
  | (Ex #r. RevLtk(actor) @ r) | (Ex #r. RevLtk(peer) @ r)
  "
end

```

Figure 2: Properties