

# Assertions and Measurements for Mixed-Signal Simulation

## PhD Thesis

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# Cyber-Physical Systems

- ▶ Both discrete and continuous modes of operation
- ▶ Example: a cell phone
  - hardware design

- ▶ Verification is needed

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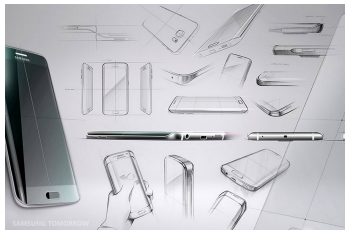
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(courtesy of Samsung and AppleInsider)

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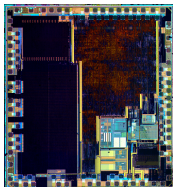


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# Mixed-Signal Simulation

## Integrated Circuits



(courtesy of ST Microelectronics)

- ▶ Implement both analog and digital electronics
- ▶ Design uses HDL and net lists at several stages

## Modeling

- ▶ Digital: event-driven



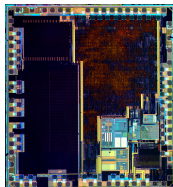
- ▶ Analog: algebraic differential equations

$$f_p\left(x, \frac{dx}{dt}\right) = 0$$

- ▶ Mixed-Signal: analog events  $\uparrow(x > 2.0)$  and digital control  $f_q$

# Mixed-Signal Simulation

## Integrated Circuits

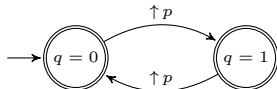


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# Simulation-Based Verification

- ▶ During the design stage run multiple simulations
- ▶ Each simulation produces a trace
  - Records evolution of quantities over time
  - Real-valued and Boolean signals
- ▶ Monitoring: each traced need to be analysed
  - Evaluate requirements: correctness, robustness, diagnostics
  - In general measuring some performance
- ▶ Automation of the monitoring activity:
  - Additional observer blocks
  - Declarative property or measurement languages

# Declarative Languages in Industry

## Assertions

- ▶ Digital domain
- ▶ Languages PSL and SVA built using two layers:
  - regular expression
  - temporal logic
- ▶ Discrete time interpretation

## Measurements

- ▶ Analog domain
- ▶ EXTRACT commands: signal processing, offline
- ▶ MEAS commands: event-driven, online

# Research on Realtime Properties

**Problem:** mixed-signal characterized by a synchronous interaction

**Solution:** use continuous-time representation

- ▶ Metric Temporal Logic (Koymans, 1990)
  - Signal Temporal Logic for real-valued signals (Maler and Nickovic, 2004)
  - Quantitative semantics for robustness estimate (Fainekos and Pappas, 2009)
- ▶ Timed Regular Expressions (Asarin, Caspi and Maler, 1998)

# Limitations of Existing Tools and Techniques

- ▶ Digital assertions bound to precision of sampling clock
- ▶ Realtime properties monitoring not implemented
- ▶ Robustness computation is not efficient
- ▶ No easy diagnostic of temporal logic properties failure
- ▶ Measurements not controllable by sequential conditions
- ▶ No analog measures in a digital context

# Outline

1. Preliminaries
2. Robustness Computation
3. Diagnostics
4. Regular Expressions Monitoring
5. Pattern-Based Measurements
6. Analog Measures in Digital Environment
7. Conclusion

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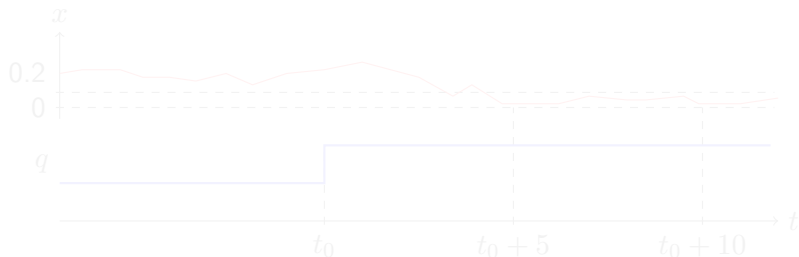
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# Signal Temporal Logic

- ▶ Propositions  $p$ : Boolean variables  $q$ , conditions  $x \leq c$ , and events  $\uparrow p$
- ▶ Temporal operators:
  - Until:  $\varphi \text{ U}_I \psi$
  - Eventually:  $\diamond_I \psi = \top \text{ U}_I \psi$
  - Always:  $\square_I \psi = \neg \diamond_I \neg \psi$

Formulas can be written with  $\diamond_{[a,b]}$  and  $\text{U}$  only

- ▶ Example: stabilization property  $\varphi = \square(\uparrow q \rightarrow \diamond_{[0,5]} \square_{[0,5]} x \leq 0.2)$

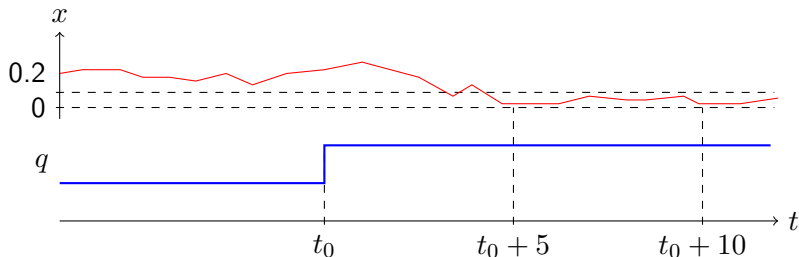


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# Monitoring

Offline approach (Maler and Nickovic, 2004): for each subformula  $\varphi$  compute set of times  $[\varphi]_{\mathbf{w}}$  where  $\varphi$  holds according to  $\mathbf{w}$

## Definition (Satisfaction Set)

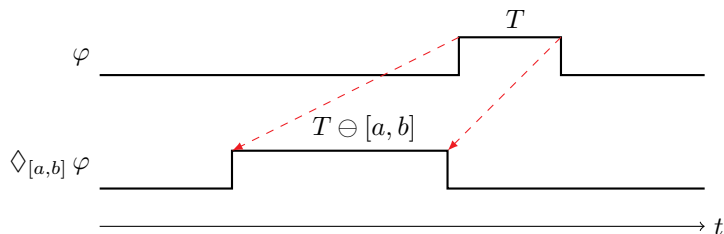
$$\begin{aligned} [p]_{\mathbf{w}} &= \{t : p_{\mathbf{w}}(t) = 1\} & [\neg\varphi]_{\mathbf{w}} &= \overline{[\varphi]_{\mathbf{w}}} \\ [\diamond_{[a,b]} \varphi]_{\mathbf{w}} &= [\varphi]_{\mathbf{w}} \ominus [a, b] & [\varphi \vee \psi]_{\mathbf{w}} &= [\varphi]_{\mathbf{w}} \cup [\psi]_{\mathbf{w}} \end{aligned}$$

# Computation

## Theorem

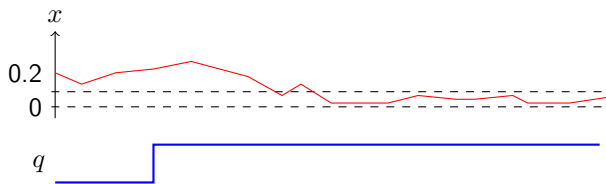
For any  $\varphi$  and  $w$  with finite variability,  $[\varphi]_w$  is finite union of intervals

- ▶ Eventually operator:



- ▶ Worst-case complexity  $O(|\varphi|)^2 \cdot |w|$

# Example



$$x \leq 0.2$$

$\uparrow q$

$$\square_{[0,5]} x \leq 0.2$$

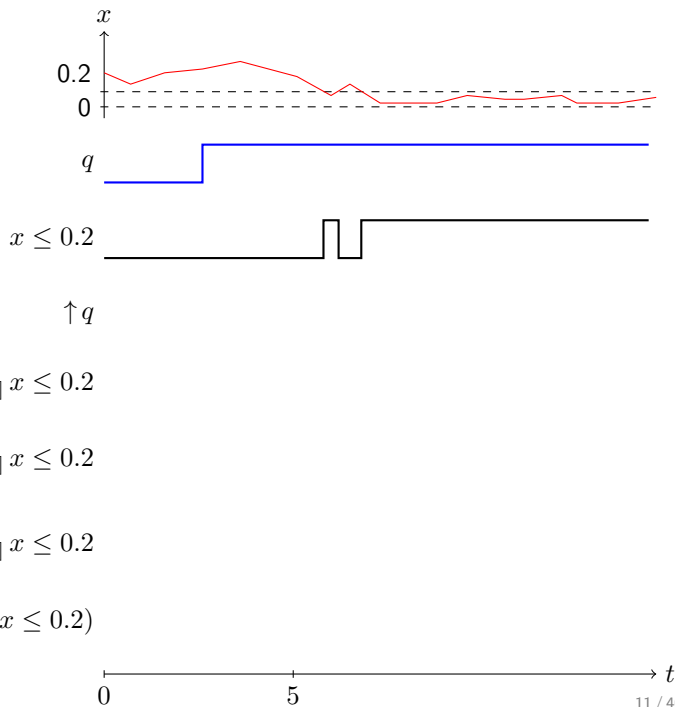
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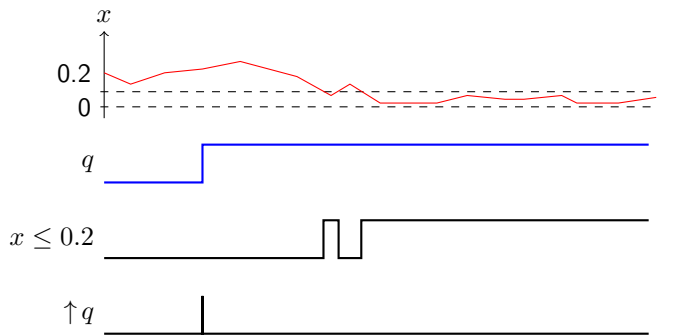
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# Example



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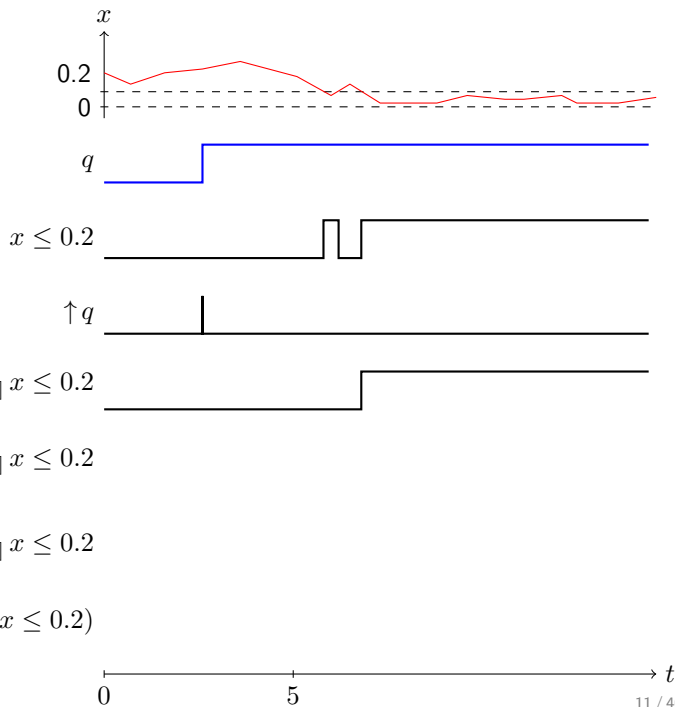
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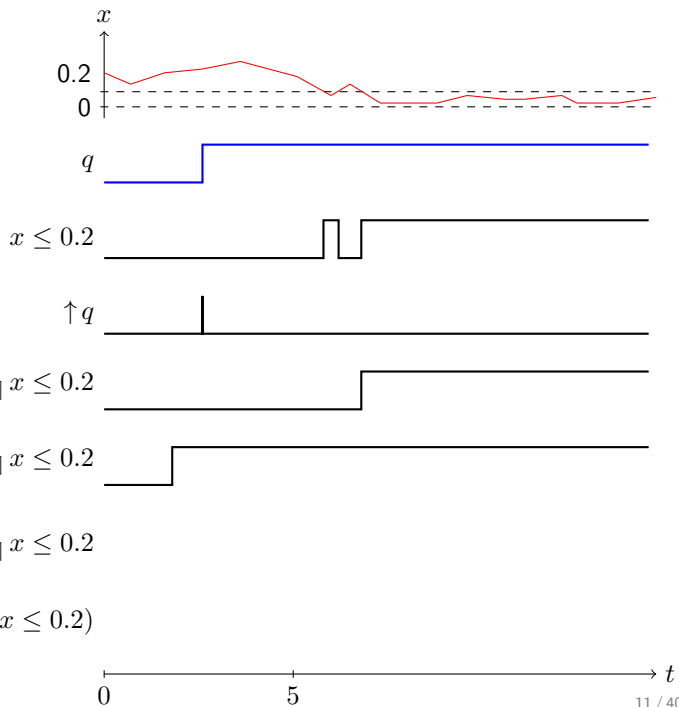
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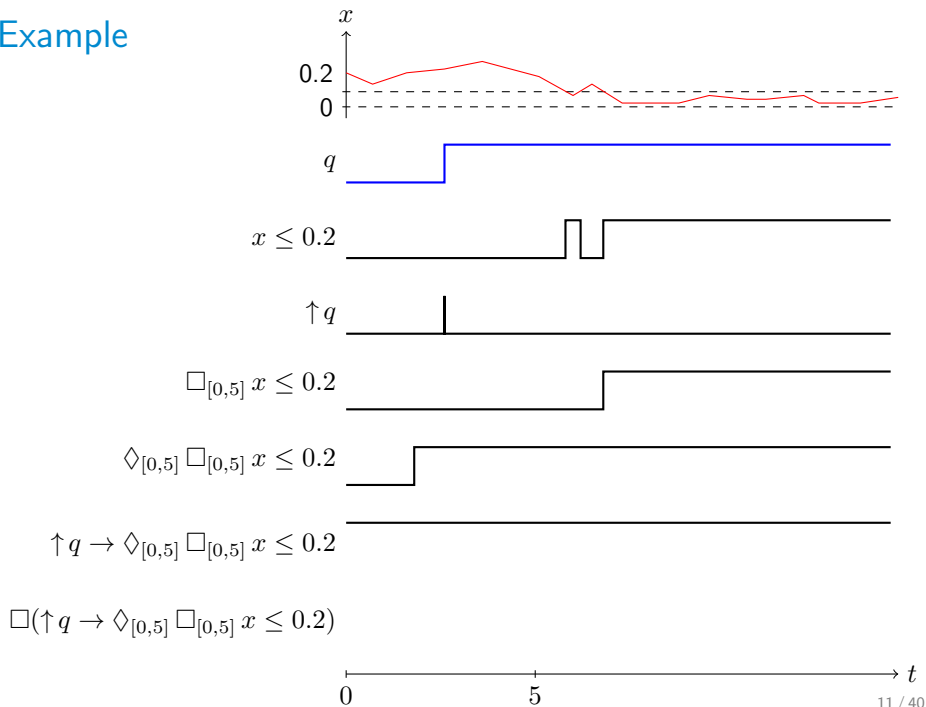
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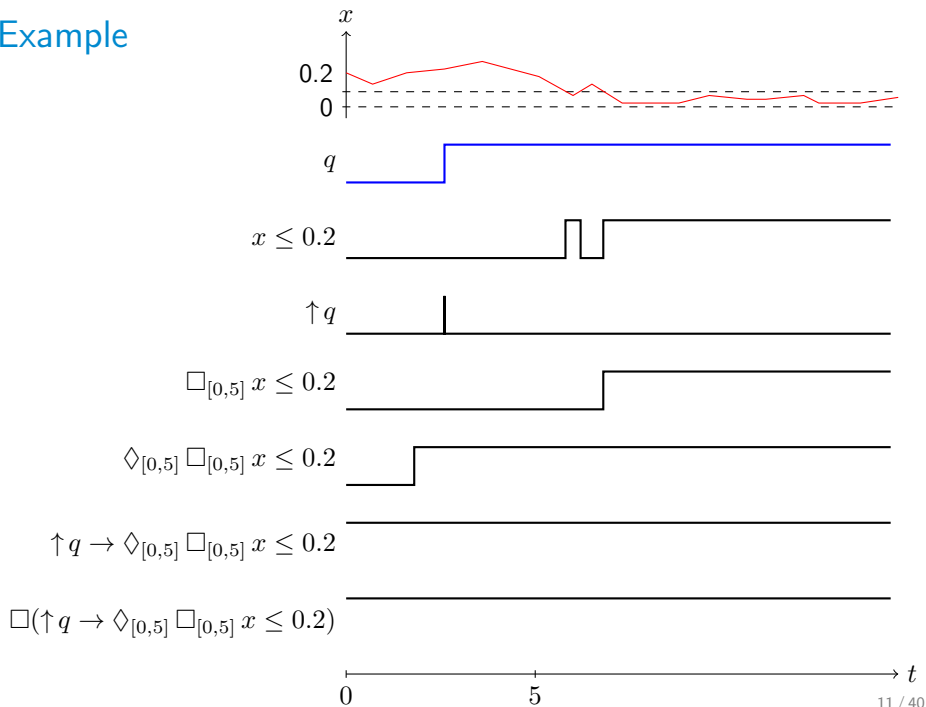


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# Example



# Quantitative Semantics

Robustness value  $\llbracket \varphi \rrbracket_{\mathbf{w}}$  indicates how strongly  $\varphi$  is satisfied / violated by  $\mathbf{w}$

- ▶ Positive if satisfied / negative if violated
- ▶ Magnitude = conservative estimate of distance to satisfaction / violation boundary

## Definition (Robustness Signal)

$$\begin{aligned} \llbracket x \leq c \rrbracket_{\mathbf{w}} &= c - x_{\mathbf{w}} & \llbracket \neg \varphi \rrbracket_{\mathbf{w}} &= - \llbracket \varphi \rrbracket_{\mathbf{w}} \\ \llbracket \Diamond_{[a,b]} \varphi \rrbracket_{\mathbf{w}} &= t \mapsto \sup_{t' \in [t+a, t+b]} \llbracket \varphi \rrbracket_{\mathbf{w}}(t') & \llbracket \varphi \vee \psi \rrbracket_{\mathbf{w}} &= \max\{\llbracket \varphi \rrbracket_{\mathbf{w}}, \llbracket \psi \rrbracket_{\mathbf{w}}\} \end{aligned}$$

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# Principle

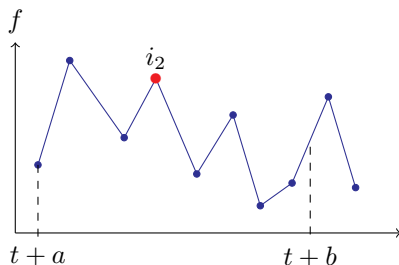
## Theorem

*For any  $\varphi$  and  $w$  piecewise linear,  $[[\varphi]]_w$  is piecewise linear*

- ▶ Until rewrite rules preserve the robustness value
- ▶ Timed eventually computed using optimal streaming algorithm of (Lemire, 2006) adapted to variable-step sampling

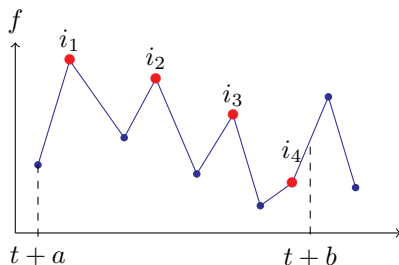
# Eventually Computation

- ▶ Problem: compute  $g(t) = \sup_{t' \in [t+a, t+b]} f(t')$
- ▶ Solution: take maximum of  $f$  at  $t + a, t + b$  and sampling points inside  $(a, b)$



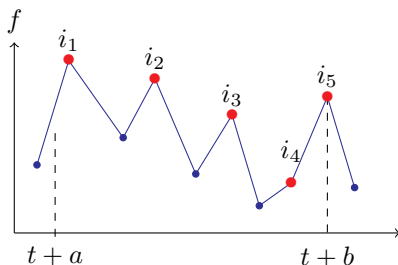
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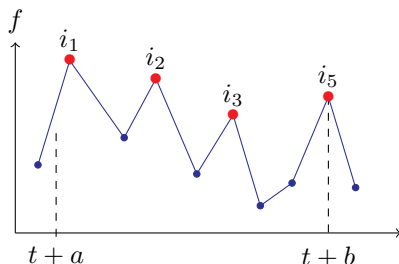
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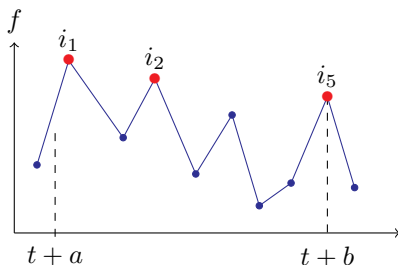
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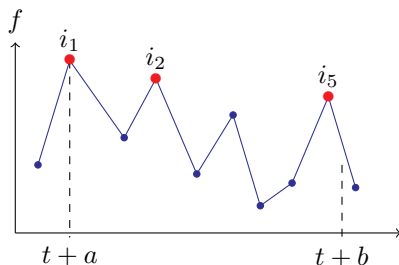
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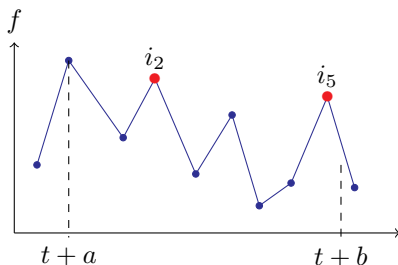
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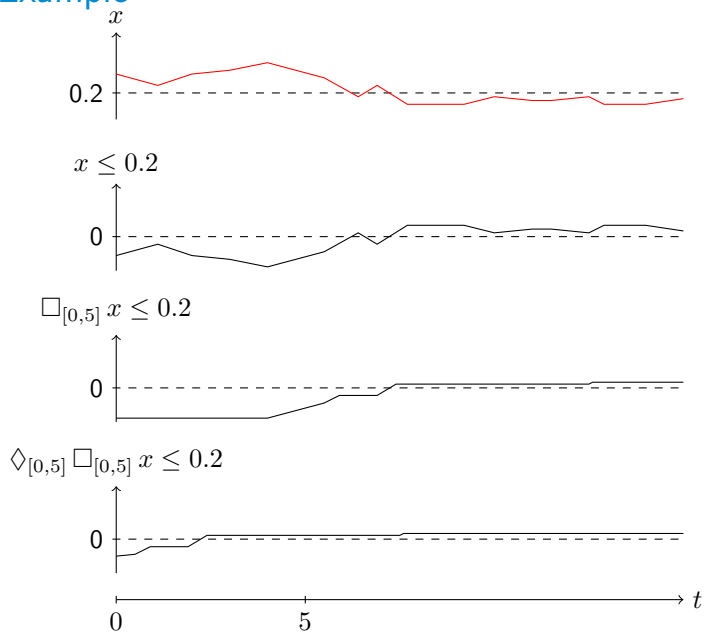


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## Example



# Evaluation

- ▶ Worst-case complexity in  $2^{O(|\varphi|)} \cdot |\mathbf{w}|$
- ▶ Implementation benchmarked with random signals:

$ \mathbf{w} $	$10^2$	$10^3$	$10^4$	$10^5$
$\diamond_{[1,2]}$	0.0031	0.0030	0.0040	0.019
$\diamond_{[1,11]}$	0.0029	0.0026	0.0039	0.017
$\diamond_{[1,21]}$	0.0027	0.0026	0.0041	0.018
$\diamond_{[1,31]}$	0.0030	0.0028	0.0041	0.021

- ▶ Cost of computing  $\diamond_{[a,b]}$  independent from  $b - a$
- ▶ Improves on related works by several orders of magnitude

## Publications

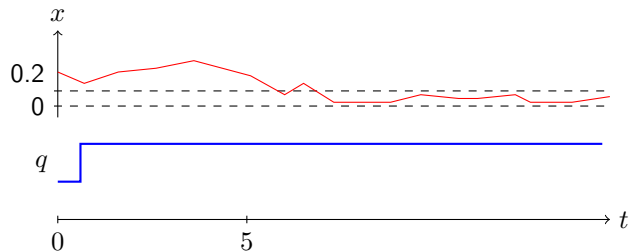
- ▶ Donzé, Ferrère, and Maler. Efficient robust monitoring for STL. In *Computer Aided Verification (CAV)*, 2013.

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# Motivation

- ▶ Find small segment of  $w$  sufficient to cause violation of  $\varphi$
- ▶ Example: violation of  $\square(\uparrow q \rightarrow \diamond_{[0,5]} \square_{[0,5]} x \leq 0.2)$

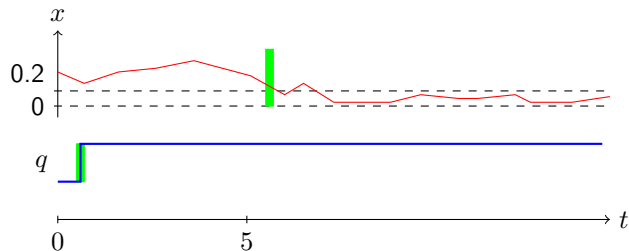


- ▶ Sub-traces = temporal implicants



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- ▶ Sub-traces = temporal **implicants**

# Propositional Implicants

- ▶ Implicant of  $\varphi \approx$  partial valuation whose extensions satisfy  $\varphi$

## Definition

Implicant of  $\varphi =$  term  $\gamma$  such that  $\gamma \Rightarrow \varphi$

Prime implicant of  $\varphi =$  implicant of  $\varphi$  maximal relative to  $\Rightarrow$

- ▶ For diagnostic: implicant compatible with observed values  $v$

## Problem (Diagnostic)

*For given  $\varphi$  and  $v$ , find  $\gamma \Rightarrow \neg\varphi$  such that  $v \models \gamma$*

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# Temporal Implicants

- ▶ Temporal implicant of  $\varphi \approx$  partial trace whose extensions satisfy  $\varphi$
- ▶ Syntactical considerations:
  - Terms with conjunctions  $\bigwedge_{t \in T} \theta(t)$  over intervals
  - Limit values handled by non-standard reals  $t^+$ ,  $t^-$
- ▶ Example:

$$\bigwedge_{t \in [0.5, 3.0]} \neg p(t) \quad \Rightarrow \quad \neg \diamond_{[1, 2]} p$$

## Theorem

*Every realtime property  $\varphi$  has a prime implicant*

Relies on boundedness of the time domain and non-standard extension

# Computation for Signal Temporal Logic

Diagnostic operators  $E, F$  such that:

- ▶ Explanation  $E(\varphi) \Rightarrow \varphi$
- ▶ Falsification  $F(\varphi) \Rightarrow \neg\varphi$

## Definition (Diagnostic Signal)

$$E(p) = p$$

$$E(\neg\varphi) = F(\varphi)$$

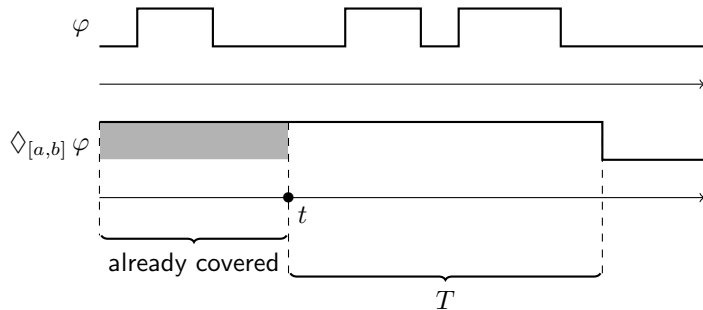
$$E(\diamond_{[a,b]} \varphi) = t \mapsto E(\varphi)(\xi(t)) \quad F(\diamond_{[a,b]} \varphi) = t \mapsto \bigwedge_{t' \in [t+a, t+b]} F(\varphi)(t')$$

with **selection function**  $\xi$  such that  $\xi(t) \in [t + a, t + b]$

## Selection Function

Compute  $\xi$  over some interval  $T$  where  $\diamond_{[a,b]} \varphi$  holds:

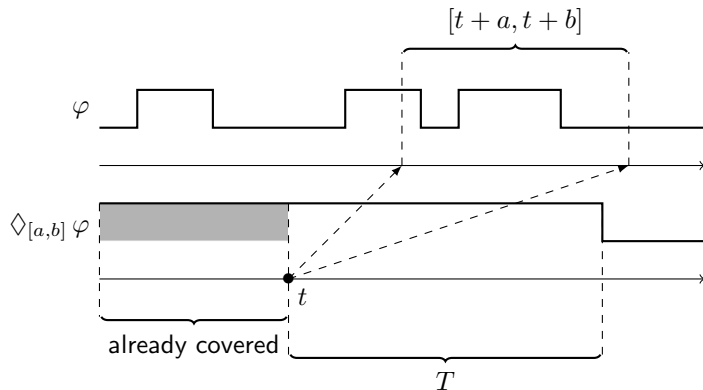
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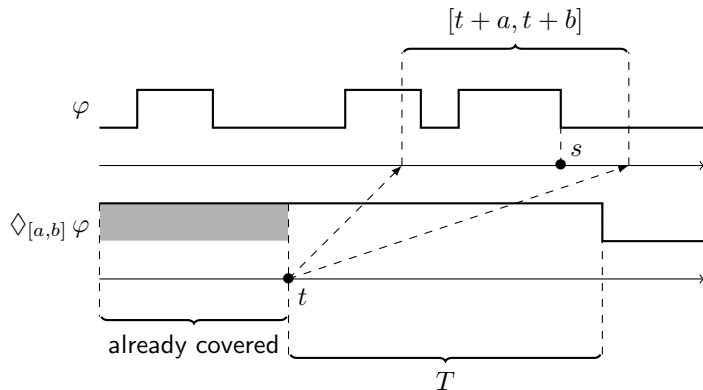
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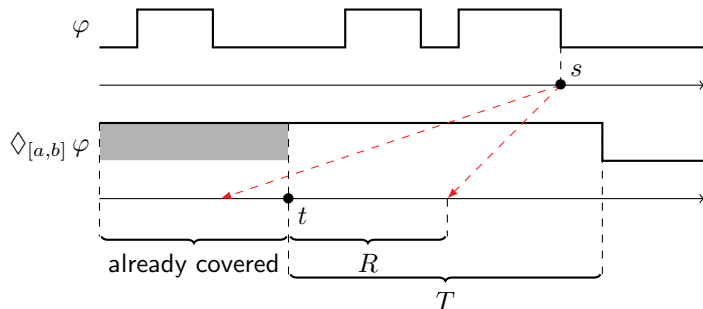




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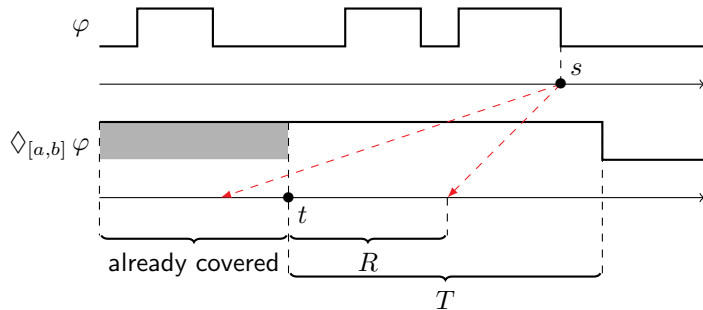
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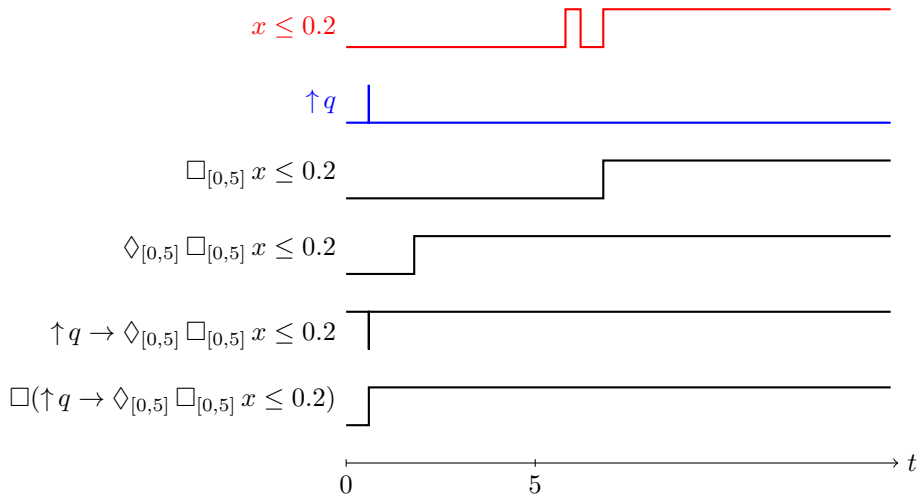
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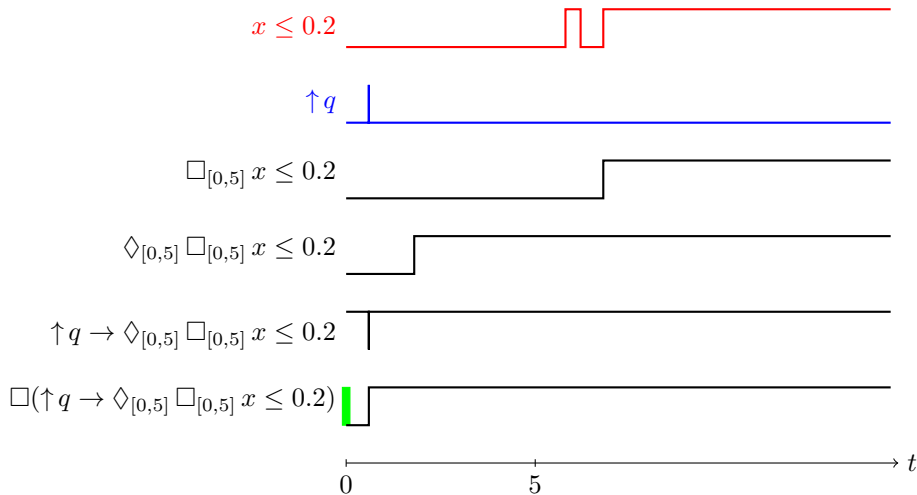
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- ▶ Worst-case complexity  $O(|\varphi|^2 \cdot |\mathbf{w}|)$

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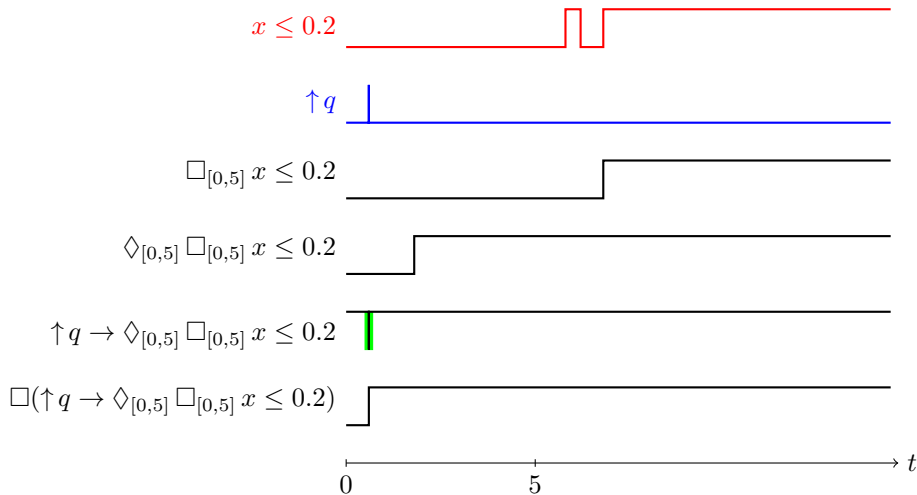
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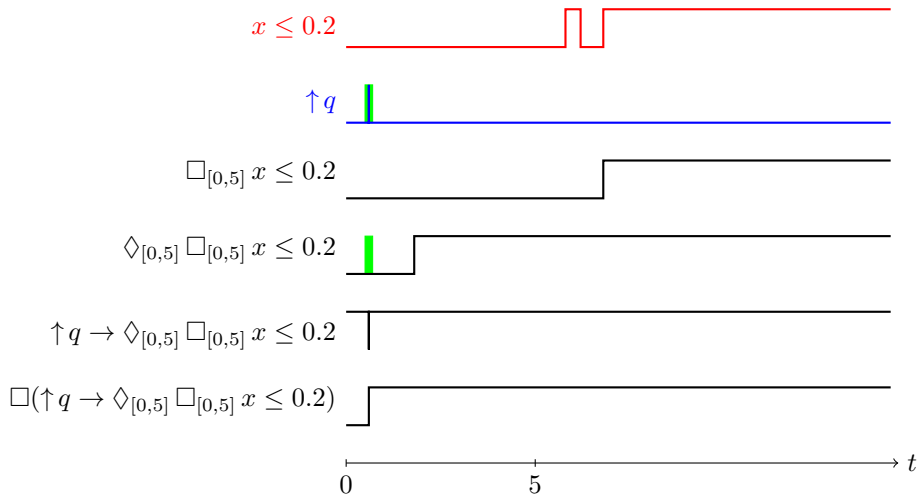
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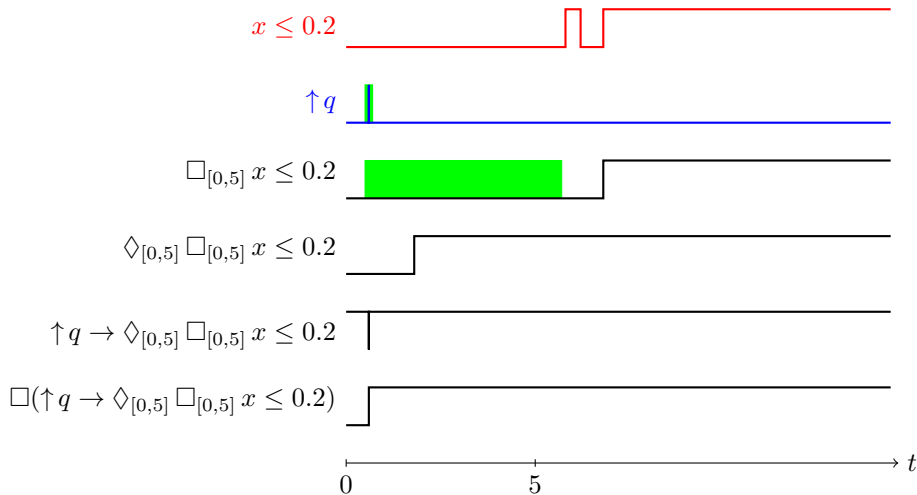
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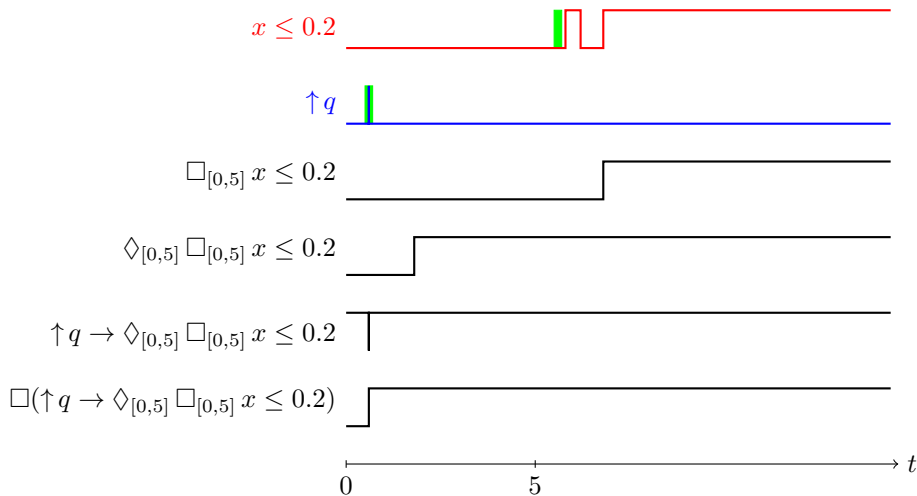
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- ▶ Ferrère, Maler, and Nickovic. Trace diagnostics using temporal implicants. In *Automated Technology for Verification and Analysis (ATVA)*, 2015.

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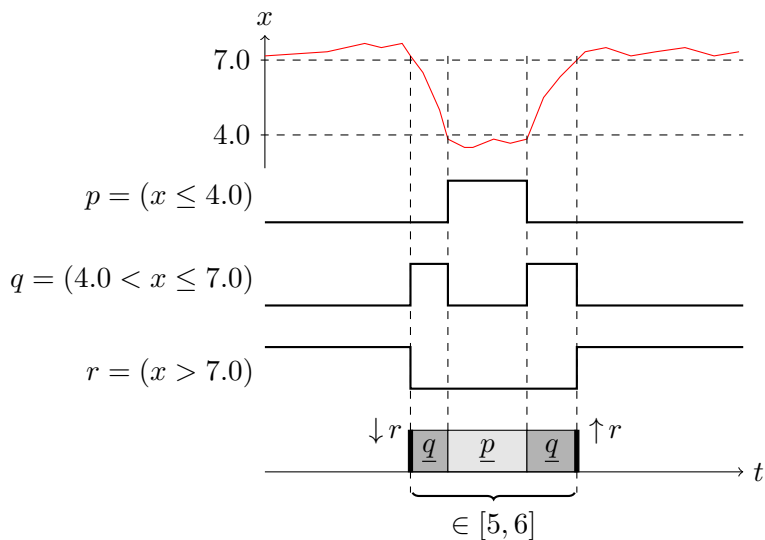
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# Signal Regular Expressions

- ▶ Propositions  $p$ : Boolean variables  $q$ , threshold conditions  $x \leq c$
- ▶ Atomic expressions: holding  $\underline{p}$ , events  $\uparrow p$
- ▶ Concatenation:  $\varphi \cdot \psi$
- ▶ Kleene star:  $\varphi^*$
- ▶ Duration restriction:  $\langle \varphi \rangle_I$

## Example

Pulse pattern:  $\psi = \downarrow r \cdot \langle \underline{q} \cdot \underline{p} \cdot \underline{q} \rangle_{[5,6]} \cdot \uparrow r$



# Monitoring

- ▶ For any  $w$  expression  $\varphi$  defines a set of segments  $(t, t')$  such that  $w[t, t']$  matches  $\varphi$
- ▶ Offline approach: for all subexpressions  $\varphi$  compute the complete set of matches  $[\varphi]_w$  of  $\varphi$  relative to  $w$

## Definition (Match Set)

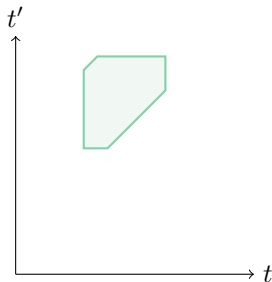
$$[p]_w = \{(t, t') : t < t'' < t' \rightarrow p_w(t'') = 1\} \quad [\varphi \vee \psi]_w = [\varphi]_w \cup [\psi]_w$$

$$[\langle \varphi \rangle_I]_w = \{(t, t') : t' - t \in I\} \cap [\varphi]_w \quad [\varphi \wedge \psi]_w = [\varphi]_w \cap [\psi]_w$$

$$[\varphi \cdot \psi]_w = [\varphi]_w \circ [\psi]_w \quad [\varphi^*]_w = \bigcup_{i \geq 0} [\varphi^i]_w$$

# Match Set Representation

- ▶ A zone = convex set with horizontal, vertical and diagonal boundaries
- ▶ Represents a set of signal segments

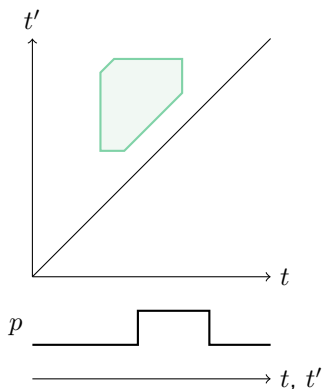


## Theorem

*For any  $\varphi$  and  $w$  with finite variability,  $[\varphi]_w$  is a finite union of zones*

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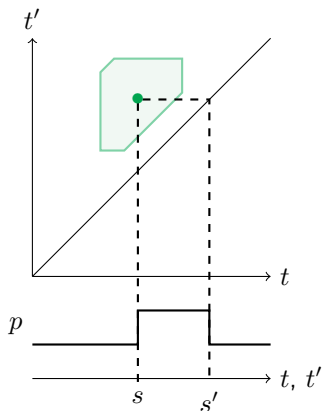


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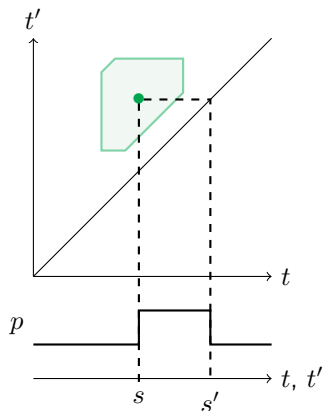
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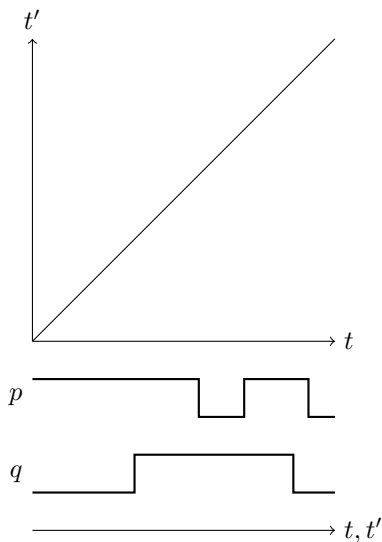
### Theorem

For any  $\varphi$  and  $w$  with finite variability,  $[\varphi]_w$  is a finite union of **zones**

## Example

$$\langle \underline{p} \rangle_{[2,4]} \cdot \langle \underline{q} \rangle_{[1,2]}$$

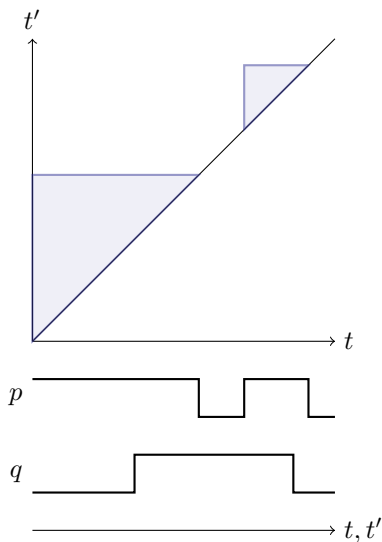
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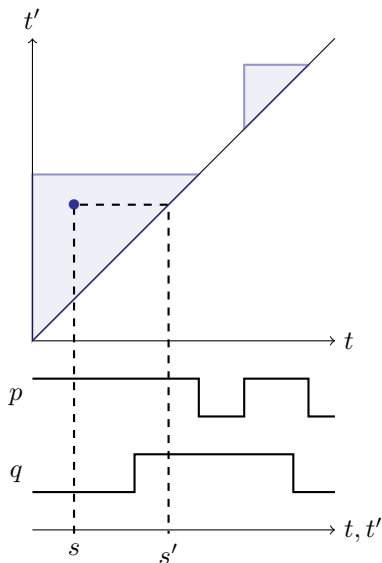
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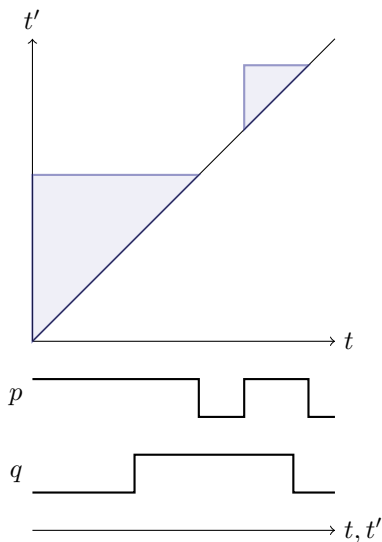
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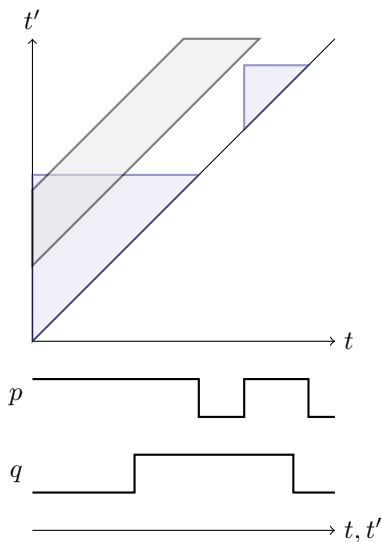
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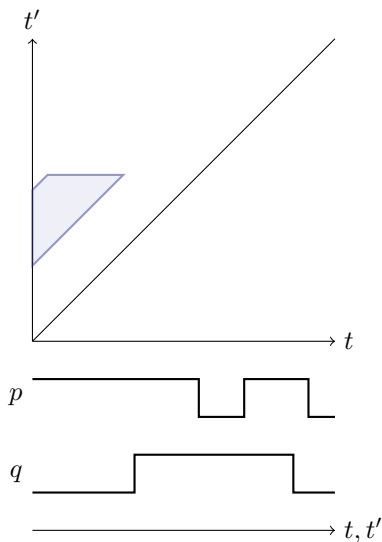
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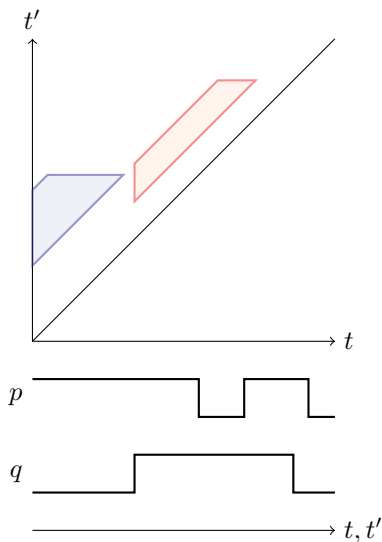
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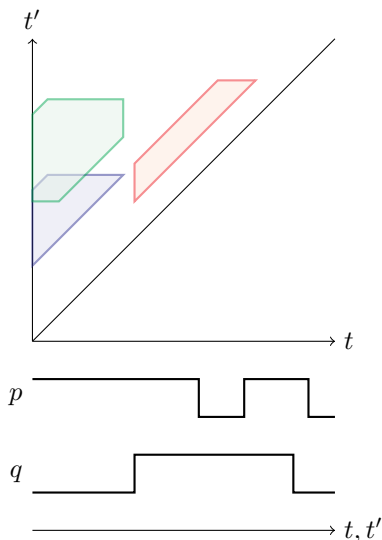




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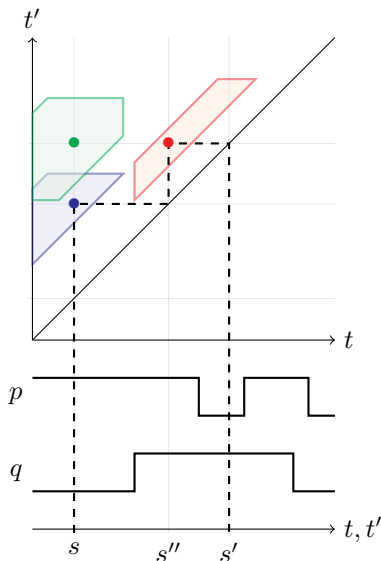
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# Kleene Star

On bounded traces  $\mathbf{w}$  the sequence  $\bigvee_{i=0}^n \varphi^i$  converges to a fix-point in finitely many steps

- ▶ Assume  $\mathbf{w}$  can be split in  $m$  constant segments  $\mathbf{v}$  of length less than 1
- ▶ Over each segment either  $[\varphi]_{\mathbf{v}} = [\top]_{\mathbf{v}}$  or  $[\varphi]_{\mathbf{v}} = [\perp]_{\mathbf{v}}$

## Lemma

$[\varphi^n]_{\mathbf{w}} \subseteq [\varphi^{n-1}]_{\mathbf{w}}$  for any  $n > 2m + 1$

Compute  $\bigvee_{i=0}^n \varphi^i$  by squaring:  $\epsilon, \varphi, \varphi^2, \varphi^4, \dots, \varphi^{2^k}$  up to  $k > \log(2m + 1)$

# Evaluation

- ▶ Worst-case complexity:  $|\mathbf{w}|^{O(|\varphi|)}$  without star
- ▶ Implementation using DBM for efficient zones computation
- ▶ Benchmarked for

$$\varphi = \langle (\langle \underline{p} \cdot \neg \underline{p} \rangle_{[0,10]})^* \wedge (\langle \underline{q} \cdot \neg \underline{q} \rangle_{[0,10]})^* \rangle_{[80,\infty]}$$

with randomized traces:

$ \mathbf{w} $	$ \llbracket \varphi \rrbracket_{\mathbf{w}} $	time
3654	0	0.27
6715	10	1.35
13306	23	2.73
26652	47	5.83

- ▶ Observed performance linear in  $|\mathbf{w}|$

## Publications

- ▶ Ulus, Ferrère, Asarin, and Maler. Timed pattern matching. In *Formal Modeling and Analysis of Timed Systems (FORMATS)*, 2014.
- ▶ Ulus, Ferrère, Asarin, and Maler. Online timed pattern matching using derivatives In *Tools and Algorithms for the Construction and Analysis of Systems (TACAS)*, 2016.

# Outline

1. Preliminaries
2. Robustness Computation
3. Diagnostics
4. Regular Expressions Monitoring
- 5. Pattern-Based Measurements**
6. Analog Measures in Digital Environment
7. Conclusion

# Measurement Language

- ▶ Motivation: automate the extraction of mixed-signal measures
- ▶ Signal Regular Expressions control when the measure takes place
- ▶ Measure: aggregating operator duration, min, max, and average
- ▶ Example:

$$\text{average}(\uparrow(x > 1.0) \cdot (x > 1.0) \cdot \downarrow(x > 1.0))$$

measures average value of  $x$  on high portions

# Conditionals and Events

Construct expressions delimited by events

- ▶ **conditional operators:**
  - $?\varphi$  begins a match of  $\varphi$
  - $!\varphi$  ends a match of  $\varphi$
- ▶ **event-bounded** expressions  $\psi$ :
  - event  $\uparrow p, \downarrow p$
  - conditional event  $\psi?, \psi!$
  - sequence  $\psi \cdot \varphi \cdot \psi$

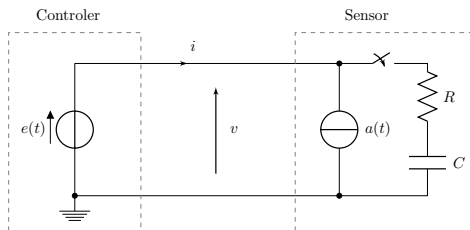
## Theorem

*For any  $w$  and  $\psi$  event-bounded,  $[\varphi]_\psi$  is finite*

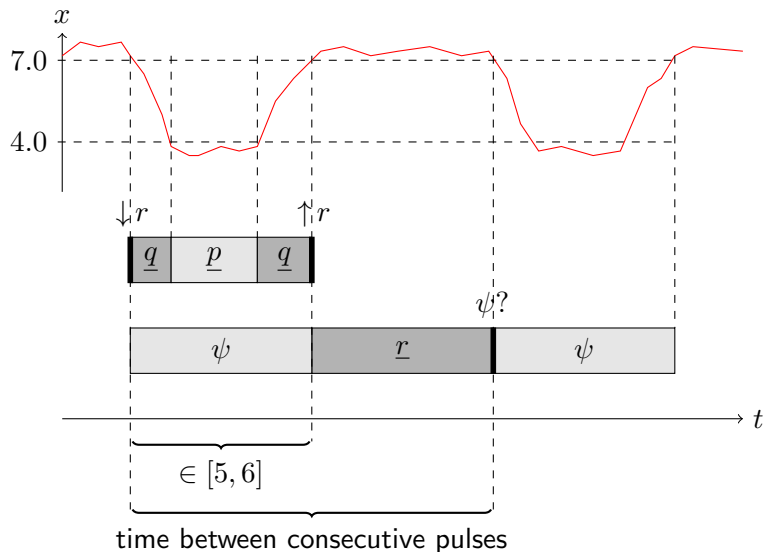


# Case Study: Distributed System Interface

- ▶ DSI3 is a protocol for electronics in automotive industry
- ▶ Based on pulse communication
- ▶ Requirements about magnitude of signals and timing of events
- ▶ Implementation: behavioral model



# Timing Requirement



# Results

- ▶ Pulse description:

$$\psi = \downarrow r \cdot \langle \underline{q} \cdot \underline{p} \cdot \underline{q} \rangle_{[5,6]} \cdot \uparrow r$$

- ▶ Measure expression:

$$\varphi = \text{duration}(\psi \cdot \underline{r} \cdot \psi?)$$

- ▶ Computation time cost:

$ \mathbf{w} $	quantize	match	extract	total
$1 \cdot 10^6$	0.047	0.617	0.000	0.664
$5 \cdot 10^6$	0.197	0.612	0.000	0.809
$1 \cdot 10^7$	0.386	0.606	0.000	0.992
$2 \cdot 10^7$	0.759	0.609	0.000	1.368

# Publications

- ▶ Ferrère, Maler, Nickovic, and Ulus. Measuring with timed patterns. In *Computer Aided Verification (CAV)*, 2015.

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# Analog Measurements and Digital Testbench

- ▶ Simulator-implemented measures provide guarantees:
  - accuracy
  - reproducible
- ▶ Unfortunately only accessible in analog environment
- ▶ Digital testbench enables structured verification
  - assertion tracking
  - coverage indicators
  - ...
- ▶ Mixed-signal verification often done with user-defined monitors

# Measurement Tasks

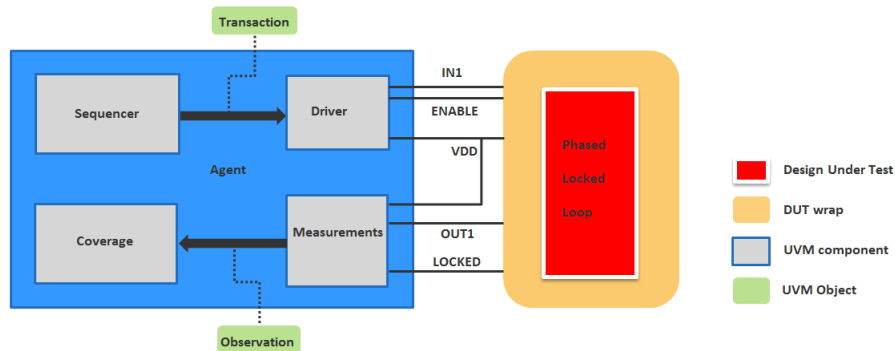
- ▶ We propose new measurements functions as **system tasks**

$$\text{task}_\mu(x, p, y, q, e, r)$$

- ▶ Input:  $(x, p)$ , output:  $(y, q)$
- ▶ Control: enable event  $e$  and reset event  $r$
- ▶ Accessed in a variety of context: module, class, etc.
- ▶ Prototype implementation using VPI with functions:  $\text{initialize}_\mu$ ,  $\text{update}_\mu$ ,  $\text{status}_\mu$ , and  $\text{evaluate}_\mu$

# Phase Locked Loop

- ▶ Digital testbench using the Universal Verification Methodology:



- ▶ Measure relative jitter online, locking time and enforce safe operating area of current through VDD
- ▶ Computation time  $< 1s$  for measurements,  $\approx 300s$  for simulation



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# Contributions

- ▶ Diagnostic procedure for realtime assertions
- ▶ Efficient algorithms for robustness computation
- ▶ Monitoring of regular expressions
- ▶ Pattern-based measurements
- ▶ Bring practice of analog and digital verification closer

## Publications

1. Donzé, Ferrère, and Maler. Efficient robust monitoring for STL. In *Computer Aided Verification (CAV)*, 2013.
2. Ulus, Ferrère, Asarin, and Maler. Timed pattern matching. In *Formal Modeling and Analysis of Timed Systems (FORMATS)*, 2014.
3. Ferrère, Maler, Nickovic, and Ulus. Measuring with timed patterns. In *Computer Aided Verification (CAV)*, 2015.
4. Ferrère, Maler, and Nickovic. Trace diagnostics using temporal implicants. In *Automated Technology for Verification and Analysis (ATVA)*, 2015.
5. Ulus, Ferrère, Asarin, and Maler. Online timed pattern matching using derivatives In *Tools and Algorithms for the Construction and Analysis of Systems (TACAS)*, 2016.

## Future Works

- ▶ Robustness of Signal Regular Expressions
- ▶ New monitoring algorithms for SRE
- ▶ Integrate SRE with STL
- ▶ Formal verification using regular expressions