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How to read this manual

This reference manual is split into two parts. The first chapter presents and defines the Lustre basic concepts. This *Lustre Core* language corresponds more or less to the intersection of the various versions of the Lustre language (from V1 to V6). Advanced features (structured types) that changed across version versions are not presented here.

The second chapter deals with the V6 specific features. Arrays, that were introduced in V4, are processed quite differently, using iterators. But the main novelty resides in the introduction of a package mechanism. Readers already familiar with Lustre ought to read directly this chapter.
Chapter 1

An Overview of the Lustre Language

1.1 Introduction

This manual presents the Lustre language, a synchronous language based on the dataflow model and designed for the description and verification of real-time systems. In this chapter, we present the general framework that forms the basis of the language: the synchronous model, the dataflow model, and the synchronous dataflow model. Then we introduce the main features of the language through some simple examples.

The end of the chapter gives some basic elements for reading the rest of the document: it makes precise the metalanguage used to describe the syntax throughout the document and describes the lexical rules of the language.

1.1.1 Synchronous Model

The synchronous model was introduced to provide abstract primitives assuming that a program reacts instantaneously to external events. Each output of the program is assigned a precise date in relation to the flow of input events.

A discrete time scale is introduced. The time granularity is considered to be adapted a priori to the time constraints imposed by the dynamics of the environment on which the system is to react. It is verified a posteriori. Each instant on the time scale corresponds to a computation cycle, i.e., in the case of Lustre, to the arrival of new inputs. The synchrony hypothesis presumes that the means of computation are powerful enough for the level of granularity to be respected. In other words, the time to compute outputs in function of their inputs is less than the level of granularity on the discrete time scale. Consequently, outputs are computed and inputs are taken into account “at the same time” (with respect to the discrete time scale).
1.1.2 Dataflow Model

The dataflow model is based on a block diagram description. A block diagram can be described either graphically, or by a system of equations. A system is made up of a network of operators acting in parallel and in time with their input rate.

Example 1 A Textual and a graphical view of the same network

```
node count (x,y: int) returns (s: int);
let
  s = 2*(x+y);
tel
```

This model provides the following advantages:

- maximal use made of parallelism (the only constraints are dependencies between data),
- mathematical formalization (formal verification methods),
- program construction and modification,
- ability to describe a system graphically.

1.1.3 Synchronous Dataflow Model

The synchronous dataflow approach consists in adding a time dimension to the dataflow model. A natural way of doing this is to associate time with the rate of dataflow. The entities manipulated can naturally be interpreted as functions of time. A basic entity (or flow) is a couple made up of:

- a sequence of values of a given type,
- a clock representing a suite of graduations (on the discrete time scale).

A flow takes the $t^{th}$ value in its sequence at the $t^{th}$ instant of its clock. For instance, the description given by the previous diagram expresses the following relation:

for any instant $t$, $s_t = 2*(x_t + y_t)$. 

A Graphic view of a network is shown.
The time dimension is therefore an underlying feature in any description of this type of model. LUSTRE is a synchronous language based on the dataflow model. The synchronous aspect introduces constraints on the type of input/output relations that can be expressed: the output of a program at a given instant cannot depend on future inputs (causality) and can depend on only a bounded number of inputs (each cycle can memorize the value of the previous input).

1.1.4 Building a Description

A LUSTRE program describes the relations between the outputs and inputs of a system. These relations are expressed using operators, auxiliary variables, and constants. The operators can be:

- basic operators,
- more complex, user-defined, operators, called nodes.

Each description written in LUSTRE is built up of a network of nodes. A node describes the relation between its input and output parameters using a system of equations. Nodes correspond to the functions of the system and allow complex networks to be built simply by passing parameters.

The synchrony hypothesis presumes that each operator in the network responds to its inputs instantaneously.

A LUSTRE description is a list of type, constant and node declarations. The declarations can occur in any order.

The functional behavior of an application described in LUSTRE does not depend on the clock cycle. It is therefore possible to perform a functional validation of the application (ignoring the time validation) by testing it on a machine different from the target machine (on the development machine in particular).

Time validation is performed on the target machine. If the computation time is less than the time interval between two instants on the discrete time scale, it can be considered to be zero, and the synchrony hypothesis is satisfied. The interval between two instants on the scale is imposed by the requirements report. Computation time depends on software and hardware performance. LUSTRE is a language describing systems with a deterministic behavior from both a functional and a time point of view.

1.2 Basic Features

In this section, we present informally the main basic features of the language, through several simple examples.

A LUSTRE program or subprogram is called a node. LUSTRE is a functional language operating on flows. For the moment, let us consider that a flow is a finite or infinite sequence of values. All the values of a flow are of the same type, which is called the
A program has a cyclic behavior. At the \( n \)th execution cycle of the program, all the involved flows take their \( n \)th value. A node defines one or several output parameters as functions of one or several input parameters. All these parameters are flows.

### 1.2.1 Simple control devices

As a very first example, let us consider a Boolean flow \( X = (x_1, x_2, \ldots, x_n, \ldots) \). We want to define another Boolean flow \( Y = (y_1, y_2, \ldots, y_n, \ldots) \) corresponding to the rising edge of \( X \), i.e., such that \( y_{n+1} \) is true if and only if \( x_n \) is false and \( x_{n+1} \) is true (\( X \) raised from false to true at cycle \( n + 1 \)). The corresponding node (let us call it \( \text{EDGE} \)) will take \( X \) as an input parameter and return \( Y \) as an output parameter (see Fig. 1.1). The interface of the node is the following:

```plaintext
node EDGE (X: bool) returns (Y: bool);
```

The definition of the output \( Y \) is given by a single equation:

\[
Y = X \text{ and not } \text{pre}(X);
\]

This equation defines \( Y \) (its left-hand side) to be always equal to the right-hand side expression \( X \text{ and not } \text{pre}(X) \). This expression involves the input parameter \( X \) and three operators:

- \( \text{and} \)" and \( \text{not} \) are usual Boolean operators, extended to operate pointwise on flows: if \( A = (a_1, a_2, \ldots, a_n, \ldots) \) and \( B = (b_1, b_2, \ldots, b_n, \ldots) \) are two Boolean flows, then \( A \text{ and } B \) is the Boolean flow \( (a_1 \land b_1, a_2 \land b_2, \ldots, a_n \land b_n, \ldots) \). Most usual operators are available in that way, and are called \"data-operators\".

- The \( \text{pre} \) (for \"previous\") operator allows one to refer at cycle \( n \) to the value of a flow at cycle \( n - 1 \): if \( A = (a_1, a_2, \ldots, a_n, \ldots) \) is a flow, \( \text{pre}(A) \) is the flow \((\text{nil}, a_1, a_2, \ldots, a_{n-1}, \ldots)\). Its first value is the undefined value \( \text{nil} \), and for any \( n > 1 \), its \( n \)th value is the \((n - 1)\)th value of \( A \).

As a consequence, if \( X = (x_1, x_2, \ldots, x_n, \ldots) \), the expression \( X \text{ and not } \text{pre}(X) \) represents the flow \((\text{nil}, x_2 \land \neg x_1, \ldots, x_n \land \neg x_{n-1}, \ldots)\). Now, since its value at the first cycle is \( \text{nil} \) the program would be rejected\(^1\) by the compiler: it indicates that the output lacks an initialization. A correct equation could be:

\(^1\)Or, at least, a warning would be returned.
Here, “false” denotes the constant flow, always equal to false. We have used the second specific LUSTRE operator, “->” (read “followed by”) which defines initial values. If A = (a₁, a₂, ..., aₙ, ...) and B = (b₁, b₂, ..., bₙ, ...) are two flows of the same type, then “A -> B” is the flow (a₁, b₂, ..., bₙ, ...), equal to A at the first instant, and then forever equal to B.

So, the complete definition of the node EDGE is the following:

```plaintext
Example 2 The EDGE node

node EDGE (X: bool) returns (Y: bool);
let
    Y = false -> X and not pre(X);
tel
```

Once a node has been defined, it can be called from another node, using it as a new operator. For instance, let us write another node, computing the falling edge of its input parameter:

```plaintext
Example 3 The FALLING_EDGE node

node FALLING_EDGE (X: bool) returns (Y: bool);
let
    Y = EDGE(not X);
tel
```

The EDGE node is of very common usage for “deriving” a Boolean flow, i.e., transforming a “level” into a “signal”. The converse operation is also very useful, it will be our second example: We want to implement a “switch”, taking as input two signals “set” and “reset” and an initial value “initial”, and returning a Boolean “level”. Any occurrence of “set” rises the “level” to true, any occurrence of “reset” resets it to false. When neither “set” nor “reset” occurs, the “level” does not change. “initial” defines the initial value of “level”. In LUSTRE, a signal is usually represented by a Boolean flow, whose value is true whenever the signal occurs. Below is a first version of the program:

```plaintext
Example 4 The SWITCH1 node

node SWITCH1 (set, reset, initial: bool) returns (level: bool);
let
    level = initial ->
        if set then true
        else if reset then false
        else pre(level);
tel
```
which specifies that the “level” is initially equal to “initial”, and then forever,

- if “set” occurs, then it becomes true
- if “set” does not occur but “reset” does, then “level” becomes false
- if neither “set” nor “reset” occur, “level” keeps its previous value (notice that “level” is recursively defined: its current value is defined by means of its previous value).

Moreover, if this node is intended to be used only in contexts where inputs set and reset are never true together, such an assertion can be specified:

```
assert not (set and reset);
```

Otherwise, this program has a flaw: It cannot be used as a “one-button” switch, whose level changes whenever its unique button is pushed. Let “change” be a Boolean flow representing a signal, then the call

```
state = SWITCH1(change,change,true);
```

will compute the always true flow: “state” is initialized to true, and never changes because the “set” formal parameter has been given priority. To get a node that can be used both as a “two-buttons” and a “one-button” switch, we have to make the program a bit more complex: the “set” signal must be considered only when the switch is turned off. We get the following program:

```
Example 5 The SWITCH node

node SWITCH (set, reset, initial: bool) returns (level: bool);
let
  level = initial ->
  if set and not pre(level) then true
  else if reset then false
  else pre(level);
  tel
```

1.2.2 Numerical examples

Recursive sequences are very easy to define in LUSTRE. For instance, the equation “\(N = 0 \rightarrow \text{pre } N + 1\);” defines the sequence of natural numbers. Let us complexify this definition to build an integer sequence, whose value is, at each instant, the number of occurrences of the “true” value of a Boolean flow \(X\):

```
N = 0 -> if X then pre N + 1 else pre N;
```
This definition does not exactly meet the specification, since it ignores the initial value of \( X \). A well-initialized counter could be:

\[
\begin{align*}
    PN &= 0 \rightarrow \text{pre } N; \\
    N &= \text{if } X \text{ then } PN + 1 \text{ else } PN;
\end{align*}
\]

or, simply

\[
    N = \text{if } X \text{ then } (0 \rightarrow \text{pre } N) + 1 \text{ else } (0 \rightarrow \text{pre } N);
\]

or even

\[
    N = (0 \rightarrow \text{pre } N) + \text{if } X \text{ then } 0 \text{ else } 1;
\]

Let us write a more general operator, with additional inputs:

- an integer \( \text{init} \), which is the initial value of the counter;
- an integer \( \text{incr} \), which must be added to the counter when \( X \) is true;
- a Boolean \( \text{reset} \), which reset the counter to the value \( \text{init} \), whatever be the value of \( X \).

The complete definition of this operator is the following:

**Example 6** The COUNTER node

```plaintext
node COUNTER (init, incr: int; X, reset: bool) returns (N: int);
var PN: int;
let
    PN = init \rightarrow \text{pre } N;
    N =
        if reset then init \\
        else if X then PN + incr \\
        else PN;
```

This node can be used to define, e.g., the sequence of odd integers:

```
    odds = COUNTER (0,2,true,false);
```

or the sequence of integers modulo 10:

```
    mod10 = COUNTER (0,1,true,reset); \\
    reset = true \rightarrow \text{pre}(mod10)=9;
```
Our next example involves real values. Let \( f \) be a real function of time, that we want to integrate using the trapezoid method. The program receives two real-valued flows \( F \) and \( \text{STEP} \), such that

\[
F_n = f(x_n) \quad \text{and} \quad x_{n+1} = x_n + \text{STEP}_{n+1}
\]

It computes a real-valued flow \( Y \), such that

\[
Y_{n+1} = Y_n + (F_n + F_{n+1}) \times \text{STEP}_{n+1}/2
\]

The initial value of \( Y \) is also an input parameter:

```
Example 7 The integrator node

node integrator(F,STEP,init: real) returns (Y: real);
let
  Y = init -> pre(Y) + ((F + pre(F))*STEP)/2.0;
tel
```

One can try to connect two such integrators in loop to compute the functions \( \sin(\omega t) \) and \( \cos(\omega t) \) in a simple-minded way:

```
Example 8 The buggy sincos node

-- there is a loop!
node sincos(omega:real) returns (sin, cos: real);
let
  sin = omega * integrator(cos,0.1,0.0);
  cos = omega * integrator(-sin,0.1,1.0);
tel
node integrator(F,STEP,init: real) returns (Y: real);
let
  Y = init -> pre(Y) + ((F + pre(F))*STEP)/2.0;
```

Called on this program, the compiler would complain that there is a **deadlock**. As a matter of fact, the variables \( \sin \) and \( \cos \) instantaneously depend on each other, i.e., the computation of the \( n \)th value of \( \sin \) needs the \( n \)th value of \( \cos \), and conversely. We have to cut the dependence loop, introducing a “\( \text{pre} \)” operator:
Example 9 The sincos node

```plaintext
--
node sincos(omega : real) returns (sin, cos : real);
var pcos, psin: real;
let
  pcos = 1.0 fby cos;
  psin = 0.0 fby sin;
  sin = omega * integrator(pcos,0.1,0.0);
  cos = omega * integrator(-psin,0.1,1.0);
let
node integrator(F,STEP,init: real) returns (Y: real);
let
  Y = init -> pre(Y) + ((F + pre(F))*STEP)/2.0;
```

1.2.3 Multiple Equation

The node sincos above does not work very well, but it is interesting since it returns more than one output. To call such a node, LUSTRE allows multiple definitions to be written. Let s, c, omega be three real variables, then

\[(s, c) = \text{sincos}(\omega)\]

is a correct LUSTRE equation, defining \(s\) and \(c\) to be, respectively, the first and the second result of the call.

So, the left-hand side of an equation can be a list of variables. The right hand side of such a multiple definition must denote a corresponding list of expressions, of suitable types. It can be

- a call to a node returning several outputs
- an explicit list
- the application of a polymorphic operator to a list

For instance, the equation

\[(\text{min}, \text{max}) = \text{if } a < b \text{ then } (a, b) \text{ else } (b, a)\]

directly defines \(\text{min}\) and \(\text{max}\) to be, respectively, the least and greatest value of \(a\) and \(b\).
1.2.4 Clocks

Let us consider the following control device: it receives a signal “set”, and returns a Boolean “level” that must be true during “delay” cycles after each reception of “set”. The program is quite simple:

Example 10 The STABLE node

```plaintext
node STABLE (set: bool; delay: int) returns (level: bool);
var count: int;
let
  level = (count > 0);
  count =
    if set then delay
    else if false -> pre(level) then pre(count)-1
    else 0;
tel
```

Now, suppose we want the “level” to be high during “delay” seconds, instead of “delay” cycles. The “second” will be provided as a Boolean input “second”, true whenever a second elapses. Of course, we can write a new program which freezes the counter whenever the “second” is not there:

Example 11 The TIME_STABLE1 node

```plaintext
node TIME_STABLE1(set, second: bool; delay:int) returns (level:bool);
var count: int;
let
  level = (count > 0);
  count =
    if set then delay
    else if second then
      if false -> pre(level) then pre(count)-1
      else 0
    else (0 -> pre(count));
tel
```

We can also reuse our node “STABLE”, calling it at a suitable clock, by filtering its input parameters. It consists of changing the execution cycle of the node, activating it only at some cycles of the calling program. For the delay to be counted in seconds, the node “STABLE” must be activated only when either a “set” signal or a “second” signal occurs.
Moreover, it must be activated at the initial instant, for initialization purposes. So the activation clock is

\[ \text{ck} = \text{true} \rightarrow \text{set or second}; \]

Now a call “STABLE((set,delay) when ck)” will feed an instance of “STABLE” with rarefied inputs, as shown by the following table:

<table>
<thead>
<tr>
<th>(set,delay) when ck</th>
<th>(s1,d1)</th>
<th>(s2,d2)</th>
<th>(s3,d3)</th>
<th>(s4,d4)</th>
<th>(s5,d5)</th>
<th>(s6,d6)</th>
<th>(s7,d7)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ck = true</td>
<td>true</td>
<td>false</td>
<td>false</td>
<td>true</td>
<td>true</td>
<td>false</td>
<td>true</td>
</tr>
</tbody>
</table>

According to the data-flow philosophy of the language, this instance of “STABLE” will have a cycle only when getting input values, i.e., when ck is true. As a consequence, the inside counter will have the desired behavior, but the output will also be delivered at this rarefied rate. In order to use the result, we have first to project it onto the clock of the calling program. The resulting node is

Example 12 The TIMESTABLE node

```plaintext
node TIME_STABLE(set, second: bool; delay: int) returns (level: bool);
var ck: bool;
let
    level = current(STABLE((set,delay) when ck));
    ck = true -> set or second;
tel

node STABLE (set: bool; delay: int) returns (level: bool);
var count: int;
let
    level = (count > 0);
    count = if set then delay else if false -> pre(level) then pre(count)-1 else 0;
tel
```

Here is a simulation of this node:

<table>
<thead>
<tr>
<th>(set,delay) (second) when ck</th>
<th>(tt,2)</th>
<th>(ff,2)</th>
<th>(ff,2)</th>
<th>(ff,2)</th>
<th>(ff,2)</th>
<th>(ff,2)</th>
<th>(tt,2)</th>
<th>(ff,2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(tt,2)</td>
<td>tt</td>
<td>ff</td>
<td>ff</td>
<td>ft</td>
<td>ft</td>
<td>ft</td>
<td>tt</td>
<td>tt</td>
</tr>
<tr>
<td>(ff,2)</td>
<td>(ff,2)</td>
<td>(ff,2)</td>
<td>(ff,2)</td>
<td>(tt,2)</td>
<td>(ff,2)</td>
<td>(ff,2)</td>
<td>(ff,2)</td>
<td>(ff,2)</td>
</tr>
<tr>
<td>STABLE((set,delay) when ck)</td>
<td>tt</td>
<td>tt</td>
<td>ff</td>
<td>tt</td>
<td>tt</td>
<td>tt</td>
<td>tt</td>
<td>tt</td>
</tr>
<tr>
<td>current(STABLE (set,delay) (set,delay) when ck))</td>
<td>tt</td>
<td>tt</td>
<td>tt</td>
<td>tt</td>
<td>ff</td>
<td>ff</td>
<td>ff</td>
<td>tt</td>
</tr>
</tbody>
</table>

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Chapter 2

Lustre Core

2.1 Notations

In the remaining of the document, we use the following notations: The wave arrow \( \rightarrow \) means that expression evaluates into. Grammar rule are given using an extended BNF notation, where non-terminals are written \langle like this \rangle and terminals “like that”.

2.2 Lexical aspects

- One-line comments start with -- and stop at the the end of the line.
- Multi-line comments start with (* and end at the next following *). Multi-line comments cannot be nested.
- Ident stands for identifier, following the C standard ([_a-zA-Z][_a-zA-Z0-9]*),
- Floating and Integer stands for decimal floating point and integer notations, following C standard,
\( \langle \text{Ident} \rangle \langle \text{string} \rangle \langle \text{Value} \rangle \langle \text{comment} \rangle \)

2.3 Pragmas

A pragma is either empty, or an arbitrary string between “%” (no “%” inside the string, or some escape to be defined), or a list of such things:

\( \langle P \rangle ::= \langle \% \rangle \langle \text{string} \rangle \langle \% \rangle ^ * \)
2.4 Identifiers

Entities are generally referred to through identifiers, but they can also depend on a package instance (like in BIN8: :binary). So we distinguish between \(\text{Ident}\), and \(\text{Identifier}\):

\[
\text{Identifier} ::= \text{Ident} | \text{Ident} :: \text{Ident}
\]

2.5 Types

\[
\begin{align*}
\text{Type} & ::= \text{type} \quad \text{Ident} + \langle P \rangle ; \\
\text{Record_Type} & ::= \text{struct} \quad \{ \langle Field \rangle \} \\
\text{Field} & ::= \text{Ident} \quad \langle Type \rangle \\
\text{Array_Type} & ::= \langle Type \rangle ^ \langle Expression \rangle \\
\text{Enum_Type} & ::= \text{enum} \quad \{ \langle Ident \rangle \}
\end{align*}
\]

Example 14 Type Declarations

```plaintext
type alias = int;
type pair = struct { a:int; b:int };
type color = enum { blue, white, black };

node type_decl(i1, i2: int) returns (x: pair);
let
  x = pair {a=i1; b=i2};
tel
```

2.6 Constants and Variables

\[
\begin{align*}
\text{Const_Decl} & ::= \text{const} \langle One_Const_Decl \rangle^+ \\
\text{One_Const_Decl} & ::= \text{Ident} \quad ; \quad \text{Type} \quad \langle P \rangle ; \\
\text{Ident_List} & ::= \text{Ident} \quad , \quad \text{Ident} \quad ;
\end{align*}
\]

Example 15 Constant Declarations

```plaintext
type alias = int;
type pair = struct { a:int; b:int };
type color = enum { blue, white, black };

node type_decl(i1, i2: int) returns (x: pair);
let
  x = pair {a=i1; b=i2};
tel
```
2.7 Functions and Nodes

The main way of structuring Lustre equations is via nodes. A memoryless node can be declared a function. A Lustre node is made of an interface (input/output declarations) and a set of equations defining the outputs.

\[
\langle \text{Node Decl} \rangle ::= \langle \text{Node Header} \rangle \ [ \langle \text{FN Body} \rangle ]
\]

\[
\langle \text{Node Header} \rangle ::= \ [ \text{"unsafe"} ] \ [ \text{"extern"} ] \ (\text{"node"} \ | \ \text{"function"}) \ (\text{"returns"}) \ (\text{"\langle FN Params \rangle \"returns\" \text{\langle P \rangle \";\"}})
\]

\[
\langle \text{FN Params} \rangle ::= \langle \text{Var Decl List} \rangle
\]

\[
\langle \text{Var Decl List} \rangle ::= \langle \text{Var Decl} \rangle \ | \ \langle \text{Var Decl} \rangle \ ; \ \langle \text{Var Decl List} \rangle
\]

\[
\langle \text{Var Decl} \rangle ::= \langle \text{Ident List} \rangle : \langle \text{Type} \rangle \ [ \langle \text{Declared Clock} \rangle \ ] \langle \text{P} \rangle
\]

\[
\langle \text{Declared Clock} \rangle ::= \text{"when"} \ (\text{Clock})
\]

\[
\langle \text{Clock} \rangle ::= \langle \text{Identifier} \rangle
\]

\[
\langle \text{FN Body} \rangle ::= (\langle \text{Local Decl} \rangle)* \ "let" \ (\text{Equation List}) "tel" [ "\;" ]
\]

\[
\langle \text{Local Decl} \rangle ::= \langle \text{Local Var Decl} \rangle \ | \ \langle \text{Local Const Decl} \rangle
\]

\[
\langle \text{Local Var Decl} \rangle ::= \text{"var"} \ (\text{Var Decl List}) ";" \ +
\]

\[
\langle \text{Local Const Decl} \rangle ::= \text{"const"} \ (\langle \text{Ident} \rangle [ "\:" \ (\text{Type}) \ "=" \ (\text{Expression}) \ ";" \ ] \ +
\]

Example 16 Node

\text{node \ sum(A:int) \ returns \ (S:int)}
\text{let}
\text{ \ \ S=A+(0->pre(S));}
\text{tel}
\text{function \ plus(A,B:int) \ returns \ (X:int)}
\text{let}
\text{ \ \ X=A+B;}
\text{tel}

Functions and nodes can be extern, in which case they should be preceeded by the \text{extern} keyword, and have an empty body. Of course if an extern entity is declared as a function while it has memory, the behavior of the whole program is unpredictable.

Example 17 Extern Nodes

\text{extern \ node \ foo \ with \ mem(A:int, B:bool, C: real) \ returns \ (X:int, Y: real);}
\text{extern \ function \ sin(A:real) \ returns \ (sinx: real);}

Extern nodes that performs side-effects should be declared as unsafe. A node that uses unsafe node is unsafe (a warning is emitted if a node is unsafe while it is not declared as such).
Example 18 Unsafe Nodes

```plaintext
unsafe extern node rand() returns (R: real);
unsafe node randr(r:real) returns (R: int);
let
  R = r*rand();
tel
```

2.8 Equations

```plaintext
⟨Equation_List⟩ ::= ⟨Eq_or_Ast⟩ | ⟨Eq_or_Ast⟩ ⟨Equation_List⟩
⟨Eq_or_Ast⟩ ::= ⟨Equation⟩ | ⟨Assertion⟩
⟨Equation⟩ ::= ⟨Left_Part⟩ “=” ⟨Right_Part⟩ ⟨P⟩ “;”
⟨Left_Part⟩ ::= “(” ⟨Left_List⟩ “)” | ⟨Left_List⟩
⟨Left_List⟩ ::= ⟨Left⟩ (“,” ⟨Left⟩)*
⟨Left⟩ ::= ⟨Identifier⟩ | ⟨Left⟩ ⟨Selector⟩
⟨Selector⟩ ::= “.” ⟨Ident⟩ | “[” ⟨Expression⟩ [ ⟨SelTrancheEnd] ] “]”
⟨SelTrancheEnd⟩ ::= “..” ⟨Expression⟩
⟨Assertion⟩ ::= “assert” ⟨Expression⟩ ⟨P⟩ “;”
```

Example 19 Equations

```plaintext
... x = a[2]; -- accessing an array slice = a[2..5] -- get an array slice (i.e., a sub array) ...
```

2.9 Assertions

2.10 Expressions

Lustre is a data-flow language: each variable or expression denotes a infinite sequence of values, i.e., a stream. All values in a stream are of the same data type, which is simply called the type of the stream. A variable $X$ of type $\tau$ represents a sequence of values $X_i \in \tau$ with $i \in \mathbb{N}$.

For instance, the predefined constant $true$ denotes the infinite sequence of Boolean values $(true, true, \cdots)$, and the integer constant 42 denotes the infinite sequence $(42, 42, \cdots)$.

Three predefined types are provided: Boolean, integer and real. All the classical arithmetic and logic operators over those types are also predefined. We say that hey are combinationnal in the sense that they are operating pointwise on streams.
Example 20 Expressions

X + Y denotes the stream \((X_i + Y_i)_i\) with \(i \in \mathbb{N}\).

Z = X + Y defines the stream Z from the streams X and Y.

\[
\langle Expression \rangle ::= \langle Identifier \rangle
\]

\[
\langle Unary \rangle ::= \sim \mid \neg
\]

\[
\langle Binary \rangle ::= + \mid \sim \mid \ast \mid / \mid \text{div} \mid \text{mod} \mid > \mid < \mid \geq \mid \leq \mid <> \mid =\mid \text{or} \mid \text{and} \mid \text{xor} \mid >=
\]

\[
\langle Nary \rangle ::= \# \mid \text{nor}
\]

2.11 Combinational operators

An operator is a predefined Lustre node.
2.12 Temporal operators

In addition to the combinationnal operators, Lustre provides a delay (\texttt{pre}) and an initialization operator (\texttt{->}).

\textbf{Example 22 Temporal operators}

The equation
\[
X = 0 \rightarrow \texttt{pre} \ X + 1;
\]
defines \(X\) as the stream \((0,1,2,3,...)\)

\[
\begin{align*}
\langle \text{Unary} \rangle & ::= \texttt{"pre"} | \texttt{"current"} \\
\langle \text{Binary} \rangle & ::= \\
& | \texttt{"->"} | \texttt{"when"} | \texttt{"fby"}
\end{align*}
\]

\textbf{Example 23 Operators}

2.13 Operators Priority

The list below shows the relative precedences and associativity of operators. The constructions with lower precedence come first.

- \texttt{"else"}
- \texttt{"->"}
- \texttt{"=>"} (right associative)
- \texttt{"or"} \texttt{"xor"}
- \texttt{"and"}
- \texttt{"<"} \texttt{"<="} \texttt{"="} \texttt{">"} \texttt{">="} \texttt{"<>"}
- \texttt{"not"}
- \texttt{"+"} \texttt{"-"} (left associative)
- \texttt{"*"} \texttt{"/"} \texttt{"%"} \texttt{"mod"} \texttt{"div"} (left associative)
- \texttt{"when"}
- \texttt{"-"} (unary minus) \texttt{"pre"} \texttt{"current"}
2.14 Clocks

It also provides a notion of clock, with a sampling operator \texttt{when} and a dual projection operator \texttt{current}.

\begin{example}
node \texttt{TIME\_STABLE(set, second: bool; delay: int)} \texttt{returns (level: bool)};
\begin{verbatim}
var ck: bool;
let
  level = current(\texttt{STABLE((set,delay)} \texttt{when} ck));
  ck = true \texttt{-> set or second};
\end{verbatim}
\end{example}

\begin{example}
node \texttt{STABLE (set: bool; delay: int)} \texttt{returns (level: bool)};
\begin{verbatim}
var count: int;
let
  level = (count > 0);
  count = if set then delay else if false \texttt{-> pre(level)} then \texttt{pre(count)-1} else 0;
\end{verbatim}
\end{example}

2.15 Abstract types

At last, complex data types and functions are handled via a mechanism of \textit{abstract types} (also called \textit{imported types}). An imported type is defined as a simple name. Abstract constants and function manipulating such types can be declared. The way those external items are effectively launched from a Lustre program depends on the back-ends of the compiler.

\begin{example}
package \texttt{complex}
\begin{verbatim}
provides
  type \texttt{t}; -- Encapsulation
  const \texttt{i:t};
  node \texttt{re(c: t)} \texttt{returns (r:real)};
body
  type \texttt{t = struct} \{ \texttt{re : real ; im : real} \};
  const \texttt{i:t} = \{ \texttt{re = 0. ; im = 1.} \};
  node \texttt{re(c: t)} \texttt{returns (re:real)};
  let \texttt{re = c.re}; \texttt{tel};
  \texttt{node complex = re};
end
\end{verbatim}
\end{example}
2.16 Programs

A Lustre-core program is a set of constant, types, function and node Declarations.
Chapter 3

Lustre V6

In this chapter, we present the Lustre V6 specific features, that are not part of the basic Lustre. In Section 3.1 we introduce the Lustre V6 Structured data types (records, enumerations, arrays). In Section 3.2 we introduce array iterators. In Section 3.4 we introduce The Lustre V6 package system which aims at introduced a new level of structuration and modularity as well as namespace facilities. In Section 3.5 we provide the predefined entities (constant, type, operator and package) of Lustre V6. In Section A.1 we provide the Lustre V6 syntax rules. In Section 3.7 we provide a complete and commented program example.

3.1 User-defined data types

Structured data type are introduced in Lustre V6. We give an informal description of them in this Section. The syntax for their declaration and used is provided in Section A.1.

Enumerations. Enumerations are similar to enumerations in other languages.

```
Example 26 Enumerations

type color1 = enum { blue, white, black };
type color2 = enum { green, orange, yellow };

node enum0(x: color1) returns (y: color2);
let
  y = if x = blue then green else if x = white then orange else yellow;
tel
```
Records. The declaration of a structured type is (semantically) equivalent to the declaration of an abstract type, a collection of field-access functions, and a constructor function.

Example 27 Records

```plaintext
type complex = { re : real ; im : real };
const j = { re = -sqrt(3)/2; im = sqrt(3)/2 }; -- a complex constant
node get_im(c:complex) returns (x:real);
let
  x = c.im;
end
```

Arrays. Here are a few examples of array declarations and definitions.

Example 28 Arrays

```plaintext
type matrix_3_3 = int ^ 3 ^ 3 ; -- to define a type matrix of integers
const m1 = 0 ^ 3 ^ 3;               -- a constant of type matrix_3_3
const m2 = [1,2,3] ^ 3;           -- another constant
const sm1 = m2[2]                 -- a constant of type int^3 (~ [1,2,3])
```

3.2 Array iterators

One the main novelty of Lustre-V6 is to provide a (restricted) notion of higher-order programming by defining array iterators to operate over arrays. Iterators replace the use of Lustre V4 homomorphic extension [1].
Using node expressions. In Lustre V6, a node denotation is not necessarily a simple identifier, since a node can be “built” by instantiating an iterator with static arguments. A node expression is then defined by:

\[
\begin{align*}
\text{node-exp} &::= \text{ident} \\
&| \quad \text{meta-op} \ll \text{static-arg} \{ ; \text{static-arg} \}^+ \gg \\
\text{static-arg} &::= \text{meta-op} \\
\text{meta-op} &::= \text{map} | \text{fill} | \text{red} | \text{fillred} | \text{boolred} \\
&| \quad \text{val-exp} | \text{node-exp} | \text{usual-op}
\end{align*}
\]

A static argument may be a statically evaluable expression (with the restriction that it can be statically evaluated), or a node expression as defined below. With some restrictions, it is also possible to use the “usual denotation” of the predefined operators (like +, >= etc). See ?? for a complete discussion on the use of predefined operators.

The semantics of iterators are presented in the sequel.

Using node expressions. The rules presented here complete the basic ones (chapter ??).

Node expressions can be used as static parameters (see above), in value expressions:

\[
\begin{align*}
\text{val-exp} &::= \text{node-exp}( \text{val-exp}\{,\text{val-exp}\}^+ )
\end{align*}
\]

Node expressions can also be used to define a node:

\[
\langle \text{node-def} \rangle ::= \langle \text{node} \rangle \langle \text{id} \rangle = \langle \text{node-exp} \rangle ;
\]

3.2.1 From scalars to arrays: fill

The fill iterator transforms a scalar-to-scalar node into a scalar-to-array node. The node argument must have a single input (input accumulator), a first output of the same type (output accumulator), and at least one another output.

The figure 3.1 shows the data-flow scheme of the fill iterator.
Definition 1: fill

For any integer constant \( n \) and any node \( \mathbb{N} \) of type:
\[
\tau \rightarrow \tau \times \theta_1 \times \ldots \times \theta_\ell,
\]

\( \text{fill}<<\mathbb{N}; n>> \) denotes a node of type:
\[
\tau \rightarrow \tau \times \theta_1 \cap n \times \ldots \times \theta_\ell \cap n
\]
such that
\[
(a_{out}, Y_1, \ldots, Y_\ell) = \text{fill}<<\mathbb{N}; n>>(a_{in})
\]
if and only if, \( \exists a_0, \ldots, a_n \) such that \( a_0 = a_{in}, a_n = a_{out} \) and
\[
\forall i = 0 \ldots n - 1, (a_{i+1}[i], Y_1[i], \ldots, Y_\ell[i]) = N(a_i)
\]

Example 29 fill

\[
\text{fill}<<\text{incr}; 4>>(0) \leadsto (4, [0,1,2,3])
\]

with:

\[
\begin{align*}
\text{node incr}(\text{ain} : \text{int}) & \text{ returns } (\text{aout}, z : \text{int}); \\
\text{let} & \\
& \quad z = \text{ain}; \text{aout} = \text{ain} + 1; \\
\text{tel}
\end{align*}
\]

3.2.2 From arrays to scalars: red

The red iterator transforms a scalar-to-scalar node into an array-to-scalar node. The node argument must have a single output, a first input of the same type, and at least another input.

The figure 3.2 shows the data-flow scheme of the reduce iterator.
For any integer constant $n$ and any node $N$ of type:
$$\tau \times \tau_1 \times \ldots \times \tau_k \rightarrow \tau,$$
\red{}\ denotes a node of type:
$$\tau \times \tau_1^n \times \ldots \times \tau_k^n \rightarrow \tau$$
such that
$$a_{out} = \red{}(a_{in}, X_1, \ldots, X_k)$$
if and only if, $\exists a_0, \ldots, a_n$ such that $a_0 = a_{in}$, $a_n = a_{out}$ and
$$\forall i = 0 \ldots n - 1, a_{i+1} = N(a_i, X_1 [i], \ldots, X_k [i])$$

**Example 30** \red{}
\red{}$(0, [1,2,3]) \mapsto 6$

### 3.2.3 From arrays to arrays: \fillred{}

The \fillred{} iterator generalizes the \fill{} and the \red{} ones. It maps a scalar-to-scalar node into a “scalar and array”-to-“scalar and array” node. The node argument must have a (first) input and a (first) output of the same type, and at least one more input and one more output. The degenerated case with no other input (resp. output) corresponds to the \fill{} (resp. \red{}) iterators.

The Figure 3.3 shows the data-flow scheme of the \fillred{} iterator.
Definition 3: fillred

For any integer constant \(n\) and any node \(N\) of type:
\[
\tau \times \tau_1 \times \ldots \times \tau_k \rightarrow \tau \times \theta_1 \times \ldots \times \theta_\ell,
\]
where \(k\) and \(\ell \geq 0\); \(\text{fillred}<N; n>\) denotes a node of type:
\[
\tau \times \tau_1^\hat{n} \times \ldots \times \tau_k^\hat{n} \rightarrow \tau \times \theta_1^\hat{n} \times \ldots \times \theta_\ell^\hat{n}
\]
such that
\[
(a_{\text{out}}, Y_1, \ldots, Y_\ell) = \text{fillred}\langle N; n\rangle(a_{\text{in}}, X_1, \ldots, X_k)
\]
if and only if, \(\exists a_0, \ldots, a_n\) such that \(a_0 = a_{\text{in}}, a_n = a_{\text{out}},\) and
\[
\forall i = 0 \ldots n - 1, (a_{i+1}, Y_1[i], \ldots, Y_\ell[i]) = N(a_i, X_1[i], \ldots, X_k[i])
\]

Example 31 fillred

A classical example is the binary adder, obtained by mapping the “full-adder”. The unsigned sum \(Z\) of two bytes \(X\) and \(Y\), and the corresponding overflow flag can be obtained by:

\[
(\text{over}, Z) = \text{fillred}\langle \text{fulladd}, 8\rangle(\text{false}, X, Y)
\]

where:

node fulladd(cin, x, y : bool) returns (cout, z : bool);
let
\[
z = \text{cin xor } x \text{ xor } y;
\]
\[
cout = \text{if } \text{cin then } x \text{ or } y \text{ else } x \text{ and } y;
\]

tel

3.2.4 From arrays to arrays, without an accumulator: map

The map iterator transforms a scalar-to-scalar node into an array-to-array node. The figure 3.4 shows the data-flow scheme of the map iterator.
Figure 3.4: A node \( N \) (3 inputs, 2 outputs), and the node map<<N; 4>>

**Definition 4: map**

For any integer constant \( n \) and any node \( N \) of type:
\[
\tau_1 \times \ldots \times \tau_k \rightarrow \theta_1 \times \ldots \times \theta_\ell,
\]
map<<N; n>> denotes a node of type:
\[
\tau_1 \hat{n} \times \ldots \times \tau_k \hat{n} \rightarrow \theta_1 \hat{n} \times \ldots \times \theta_\ell \hat{n}
\]
such that
\[
(Y_1, \ldots, Y_\ell) = \text{map<<N; n>>}(X_1, \ldots, X_k)
\]
if and only if
\[
\forall i = 0 \cdots n - 1, (Y_1[i], \ldots, Y_\ell[i]) = N(X_1[i], \ldots, X_k[i])
\]

**Example 32 map**

\[
\text{map} \ <<+; 3>> ([1,0,2],[3,6,-1]) \leadsto [4,6,1]
\]

### 3.2.5 From Boolean arrays to Boolean scalar: boolred

**Definition 5: boolred**

This iterator has 3 integer static input arguments:
\[
\text{boolred}<<i; j; k>>
\]
such that \( 0 \leq i \leq j \leq k \) and \( k > 0 \).
It denotes a combinational node whose profile is \( \text{bool}^k \rightarrow \text{bool} \), and whose semantics is given by: the output is true if and only if at least \( i \) and at most \( j \) elements are true in the input array.

Note that this iterator can be used to implement efficiently the diese and the nor operators:

**Example 33 boolred**

\[
\#(a_1, \ldots, a_n) \leadsto \text{boolred}(0,1,n)[a_1, \ldots, a_n]
\]
\[
\text{nor}(a_1, \ldots, a_n) \leadsto \text{boolred}(0,0,n)[a_1, \ldots, a_n]
\]
3.2.6 Lustre iterators versus usual functional languages ones.

Note that those iterators are more general than the ones usually provided in functional language libraries. Indeed, the arity of the node is not fixed. For example, in a usual functional language, you would have \texttt{map} and \texttt{map2} with the following profile:

\begin{align*}
\texttt{map} : \quad \left( 'a \to 'b \right) \to (a' \text{ array}) &\to (b' \text{ array}) \\
\texttt{map2} : \quad \left( 'a \to 'b \to 'c \right) \to (a' \text{ array}) &\to (b' \text{ array}) \to (c' \text{ array})
\end{align*}

whereas the \texttt{map} iterator we define here would have the following profile in the functional programming world:

\begin{align*}
\texttt{mapn} : \quad \left( 'a_1 \to 'a_2 \to \ldots \to 'a_n \right) \to (a_1' \text{ array}) &\to (a_2' \text{ array}) \to \ldots \\
&\to (a_{n-1}' \text{ array}) \to (a_n' \text{ array})
\end{align*}

Note that it even note possible to give a milner-style type to describe this iterator. Indeed, the type of the node depends on the size of the array; it would therefore require a dependant-type system.
3.3 Parametric nodes

A node can be parametrised by constants, types, and nodes.

**Example 34 Parametric Node**

```plaintext
node mk_tab<<type t; const init: t; const size: int>>
 (a:t) returns (res: t^size);
let
 res = init ^ size;
tel
node tab_int3 = mk_tab<<int, 0, 3>>;
node param_node2 = mk_tab<<bool, true, 4>>;
```

**Example 35 Parametric Node**

```plaintext
node toto_n<<
 node f(a, b: int) returns (x: int);
 const n : int
>>(a: int) returns (x: int^n);
var v : int;
let
 v = f(a, 1);
x = v ^ n;
tel
node param_node = toto_n<<Lustre::iplus, 3>>;
```

Nodes can even be defined recursively using the “with” construct.

**Example 36 Recursive Node**

```plaintext
node consensus<<const n : int>>(T: bool^n) returns (a: bool);
let
 a = with (n = 1) then T[0]
   else T[0] and consensus << n-1 >> (T[1 .. n-1]);
tel

node consensus2 = consensus<<8>>;
```
3.4 Packages and models

A lustre V6 program is a list of packages, models (generic packages), and model instances.

Basic lustre programs are still accepted by the lustre V6 compiler, which consider implicitly that a program without package annotations:

- uses no other package
- provides all the package parameters it defines
- is part of a package that is made of the file name

\[
\langle \text{Program} \rangle ::= (\langle \text{Package} \rangle \mid \langle \text{Model} \rangle \mid \langle \text{Model\_Instance} \rangle)^* 
\]

A package is made of:

- a header, which gives the name of the package, the entities exported by the package, and the packages and models used by the package;
- and an optional body which consists of the declarations of the entities defined by the package. When the body is not given, the package is external.

\[
\langle \text{Package} \rangle ::= \langle \text{Package\_Header} \rangle \ [ \langle \text{Package\_Body} \rangle ] \ "\text{end}" 
\]

\[
\langle \text{Package\_Header} \rangle ::= \ "\text{package}" \ \langle \text{Ident} \rangle \ \langle P \rangle \ [ \ "\text{uses}" \ \langle \text{Ident\_List} \rangle ] 
\]

\[
"\text{provides}" \ \langle \text{Package\_Params} \rangle 
\]

\[
\langle \text{Package\_Params} \rangle ::= (\langle \text{Package\_Param} \rangle)^+ 
\]

\[
\langle \text{Package\_Param} \rangle ::= \ "\text{const}" \ \langle \text{Ident} \rangle \ "\" \ \langle \text{Type\_Identifier} \rangle \ \langle P \rangle \ "\;" 
\]

\[
| \ "\text{type}" \ \langle \text{Type\_Ident\_List} \rangle \ \langle P \rangle \ "\;" 
\]

\[
| \ \langle \text{Function\_Header} \rangle 
\]

\[
| \ \langle \text{Node\_header} \rangle 
\]

\[
\langle \text{Type\_Identifier} \rangle ::= \ \langle \text{Identifier} \rangle 
\]

\[
\langle \text{Type\_Ident\_List} \rangle ::= \ \langle \text{Ident} \rangle \ "\;" | \ \langle \text{Ident} \rangle \ "\"," \ \langle \text{Type\_Ident\_List} \rangle 
\]

The output parameters of packages can be constants, types, nodes, or functions.
Example 37 Package

```plaintext
package pack
   uses pack1, pack2;
   provides
      const pi,e:real;
      type t1,t2;
      function cos(x:real) returns (y:real);
      node rising_edge(x:bool) returns (re:bool);
body
   ...
end
```

A model has an additional section (needs ...) in its header which declares the formal parameters of the model. A model is somehow a parametric package.

Example 38 Model

```plaintext
model model_example
   needs
      type t;
      const pi;
   provides
      node n(init, in : t ) returns (res : t);
body
      node n(init, in: t) returns (res: t);
      let
         res = init -> pre in;
      tel
end
```

A model instance defines a package as an instance of a model by providing input parameters. It declares the list of packages it uses. It provides all objects exported by the model and its effective parameters.
The user decide which node is the main one at compile time, following the Lustre V4 tradition. For example the node bar of package p in file foo.lus will be used as main node if the following command is launched: lv6 foo.lus -main p::bar.

Example 39 Model instance

Here is how to obtain packages by instanciating the model given in Example 38:

```
package model_instance_example_bool is model_example(t=bool,pi=3.14);
package model_instance_example_int is model_example(t=int,pi=3.14);
```

In this way, model_instance_example_bool is a package that provides the node:

```
n(init, in : bool) returns (res : bool)
```

3.4.1 Package body

```
(package_body) ::= ["body"] (entity_decl)*
(entity_decl) ::= (const_decl)
| (type_decl)
| (model_instance)
| (function_decl)
| (node_decl)
```
3.5 Predefined entities

a package is a set of definitions of entities: types, constants and operators (nodes or functions).

a model can have as parameters a type, a constant, or a node.
### 3.6 The Merge operator

**Example 41 The Merge operator**

```plaintext
type piece = enum { Pile, Face, Tranche }

node test_merge(clk: piece
    i1 : int
    i2 : int
    i3 : int)
returns (y: int);
let
    y = test_merge_clk(clk, i1 when Pile(clk), i2 when Face(clk), i3 when Tranche(clk))

tel

node test_merge_clk(clk: piece
    i1 : int when Pile(clk)
    i2 : int when Face(clk)
    i3 : int when Tranche(clk))
returns (y: int);
let
    y = merge clk
        ( Pile  -> (0->i1))
        ( Face  -> i2)
        ( Tranche -> i3);

tel

node merge_bool_alt(clk : bool
    i1 : int when clk
    i2 : int when not clk)
returns (y: int);
let
    y = merge clk (true -> i1) (false-> i2);

tel

node merge_bool_ter(clk : bool
    i1 : int when clk
    i2 : int when not clk)
returns (y: int);
let
    y = merge clk (false-> i2) (true -> i1);

tel
```

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<table>
<thead>
<tr>
<th>clk</th>
<th>Pile</th>
<th>Pile</th>
<th>Face</th>
<th>Tranche</th>
<th>Pile</th>
<th>Face</th>
</tr>
</thead>
<tbody>
<tr>
<td>i1</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>i2</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>i3</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>y</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>3</td>
<td>2</td>
</tr>
</tbody>
</table>
3.7 A complete example (finish me)

Example 42 Detecting the stability of a flow

```plaintext
const cycle_time = 1.0;
const epsilon = 0.0001;

node vrai_depuis_n_secondes(n: real; signal: bool) returns (res: bool)
var
tempo : real;
let
tempo = n -> if not signal then n else max(0.0, pre tempo - cycle_time);
res = (tempo = 0.0);
tel

node vrai_depuis_n_secondes_bis(n, t : real; signal: bool) returns (res: bool)
var
tempo : real;
pt : real; -- un registre pour memoriser l'horodate de l'instant precedent
let
pt = 0.0 -> pre t;
tempo = n -> if not signal then n else max(0.0, pre tempo - (t-pt));
res = (tempo = 0.0);
tel

-- assign the jth element of an array to a value
type update_acc = {
  i: int;
  j: int;
  v: real
};

function update_cell_do(const d: int>>(acc: update_acc; cell: real)
returns (nacc: update_acc; ncell: real);
let
ncell = if acc.i = acc.j then acc.v else cell;
nacc = update_acc { i = acc.i+1; j = acc.j ; v = acc.v }; -- arg...
tel

function assign(const d: int>>(v: real; jv: int; t: real^d) returns (nt: real^d)
var
dummy: update_acc;
let
dummy, nt=fillred(update_cell_do<<d>>( update_acc { i = 0 ; j = jv ; v = v }),
tel

-- Compute the average of the elements of an array
function average<const d : int>>(t: real^d) returns (res: real)
```

Appendix A

Appendix

A.1 The syntax rules summary

\[ \langle P \rangle ::= \langle \text{"%" string \text{"%"} \rangle }^* \]

\[ \langle \text{Identifier} \rangle ::= \langle \text{Ident} \rangle | \langle \text{Ident} \rangle"::" \langle \text{Ident} \rangle \]

\[ \langle \text{Type Decl} \rangle ::= \langle \text{"type"} \langle \text{Ident} \rangle{+} \langle P \rangle \";" \]
\[ \quad | \langle \text{"type"} \langle \text{Ident} \rangle=" \langle \text{Type} \rangle \langle P \rangle \";" \]
\[ \langle \text{Type} \rangle ::= \langle \text{Ident} \rangle | \langle \text{Record Type} \rangle | \langle \text{Array Type} \rangle | \langle \text{Enum Type} \rangle \]
\[ \langle \text{Record Type} \rangle ::= \langle \text{"struct" \{"} \langle \text{Field List} \rangle \"\} \rangle \]
\[ \langle \text{Field List} \rangle ::= \langle \text{Field} \rangle | \langle \text{Field} \";" \langle \text{Field List} \rangle \]
\[ \langle \text{Field} \rangle ::= \langle \text{Ident} \rangle:" \langle \text{Type} \rangle \]
\[ \langle \text{Array Type} \rangle ::= \langle \text{Type} \"^" \langle \text{Expression} \langle P \rangle \rangle \]
\[ \langle \text{Enum Type} \rangle ::= \langle \text{"enum" \{"} \langle \text{Ident List} \rangle \"\} \rangle \]

\[ \langle \text{Const Decl} \rangle ::= \langle \text{"const" \{\langle \text{One Const Decl} \rangle} \rangle^+ \]
\[ \langle \text{One Const Decl} \rangle ::= \langle \text{Ident List} \rangle:" \langle \text{Type} \rangle \langle P \rangle \";" \]
\[ \quad | \langle \text{Ident} \rangle=" \langle \text{Expression} \rangle \langle P \rangle \";" \]
\[ \quad | \langle \text{Ident} \rangle:" \langle \text{Type} \rangle=" \langle \text{Expression} \rangle \langle P \rangle \";" \]
\[ \langle \text{Ident List} \rangle ::= \langle \text{Ident} \rangle | \langle \text{Ident} \rangle:" \langle \text{Ident List} \rangle \]
\begin{itemize}
\item \textbf{(Node Decl)} ::= \textbf{(Node Header)} [ \textbf{(FN Body)} ]
\item \textbf{(Node Header)} ::= \texttt{[ "unsafe"] [ "extern"] ("node" | "function") "(" (\textbf{FN Params}) ") returns" "(" (\textbf{FN Params}) ") \}) ";
\item \textbf{(FN Params)} ::= \textbf{(Var Decl List)}
\item \textbf{(Var Decl List)} ::= \textbf{(Var Decl)} | \textbf{(Var Decl)} ; \textbf{(Var Decl List)}
\item \textbf{(Var Decl)} ::= \textbf{\{Ident List\}} "\:" \textbf{(Type)} [ \textbf{(Declared Clock)} ] \textbf{(P)}
\item \textbf{(Declared Clock)} ::= \texttt{"when" (\textbf{Clock})}
\item \textbf{(Clock)} ::= \textbf{(Identifier)}
\item \textbf{(FN Body)} ::= ( \textbf{(Local Decl)} )* \texttt{"let" (Equation List) "tel" [ ";" ]}
\item \textbf{(Local Decl)} ::= \textbf{(Local Var Decl)} | \textbf{(Local Const Decl)}
\item \textbf{(Local Var Decl)} ::= \texttt{"var" (\textbf{Var Decl List}) ; ;}
\item \textbf{(Local Const Decl)} ::= \texttt{"const" (\textbf{Ident}) [ "\:" (\textbf{Type}) "=" \textbf{(Expression)} ; ;]}
\item \textbf{(Equation List)} ::= \textbf{(Eq or Ast)} | \textbf{(Eq or Ast)} \textbf{(Equation List)}
\item \textbf{(Eq or Ast)} ::= \textbf{(Equation)} | \textbf{(Assertion)}
\item \textbf{(Equation)} ::= \textbf{(Left Part)} "\=" \textbf{(Right Part)} \textbf{(P)} " ; ;
\item \textbf{(Left Part)} ::= \texttt{"(" (\textbf{Left List}) \")"} | \textbf{(Left List)}
\item \textbf{(Left List)} ::= \textbf{(Left)} ( " , " \textbf{(Left)} ) *
\item \textbf{(Left)} ::= \textbf{(Identifier)} | \textbf{(Left)} \textbf{(Selector)}
\item \textbf{(Selector)} ::= ( "." (\textbf{Ident}) | "[" \textbf{(Expression)} [ \textbf{(SelTrancheEnd)} ] "]")
\item \textbf{(SelTrancheEnd)} ::= ( ".." \textbf{(Expression)}
\item \textbf{(Assertion)} ::= \texttt{"assert" \textbf{(Expression)} \textbf{(P)} ; ;}
\end{itemize}
\[
\langle \text{Expression} \rangle \ ::= \langle \text{Identifier} \rangle \\
| \langle \text{Value} \rangle \\
| “(” \langle \text{Expression List} \rangle “)” \\
| \langle \text{Record Exp} \rangle \\
| \langle \text{Array Exp} \rangle \\
| \langle \text{Unary} \rangle \langle \text{Expression} \rangle \\
| \langle \text{Expression} \rangle \langle \text{Binary} \rangle \langle \text{Expression} \rangle \\
| \langle \text{Nary} \rangle \langle \text{Expression} \rangle \\
| “if” \langle \text{Expression} \rangle “then” \langle \text{Expression} \rangle “else” \langle \text{Expression} \rangle \\
| \langle \text{Call} \rangle \\
\]

\[
\langle \text{Expression List} \rangle \ ::= \langle \text{Expression} \rangle | \langle \text{Expression} \rangle “,” \langle \text{Expression List} \rangle \\
\]

\[
\langle \text{Record Exp} \rangle \ ::= \langle \text{Expression} \rangle “{” \langle \text{Field Exp List} \rangle “}” \\
\]

\[
\langle \text{Field Exp List} \rangle \ ::= \langle \text{Field Exp} \rangle | \langle \text{Field Exp} \rangle “;” \langle \text{Field Exp List} \rangle \\
\]

\[
\langle \text{Field Exp} \rangle \ ::= \langle \text{Ident} \rangle “=” \langle \text{Expression} \rangle \\
\]

\[
\langle \text{Array Exp} \rangle \ ::= “[” \langle \text{Expression List} \rangle “]” | \langle \text{Expression} \rangle “^” \langle \text{Expression} \rangle \\
\]

\[
\langle \text{Call} \rangle \ ::= \langle \text{User Op} \rangle \langle P \rangle “(” \langle \text{Expression List} \rangle “)” \\
\]

\[
\langle \text{User Op} \rangle \ ::= \langle \text{Identifier} \rangle \\
| \langle \text{Iterator} \rangle “<<” \langle \text{User Op} \rangle “;” \langle \text{Expression} \rangle “>>” \\
\]

\[
\langle \text{Iterator} \rangle \ ::= “map” | “red” | “fill” | “fillred” | “boolred” \\
\]

\[
\langle \text{Unary} \rangle \ ::= “-” | “not” \\
\]

\[
\langle \text{Binary} \rangle \ ::= “+” | “-” | “*” | “/” | “div” | “mod” \\
| “>” | “<” | “>=” | “<=” | “<>” | “=” \\
| “or” | “and” | “xor” | “=>” \\
\]

\[
\langle \text{Nary} \rangle \ ::= “♯” | “nor” \\
\]

\[
\langle \text{TypeDecl} \rangle \ ::= “type” \langle \text{Ident} \rangle “;” \\
| “type” \langle \text{Ident} \rangle “=” \langle \text{Type} \rangle “;” \\
\]

\[
\langle \text{Type} \rangle \ ::= \langle \text{Ident} \rangle | \langle \text{Record Type} \rangle | \langle \text{Array Type} \rangle | \langle \text{Enum Type} \rangle \\
\]

\[
\langle \text{Record Type} \rangle \ ::= “{” \langle \text{Field List} \rangle “}” \\
\]

\[
\langle \text{Field List} \rangle \ ::= \langle \text{Field} \rangle | \langle \text{Field} \rangle “;” \langle \text{Field List} \rangle \\
\]

\[
\langle \text{Field} \rangle \ ::= \langle \text{Ident} \rangle “:” \langle \text{Type} \rangle \\
\]

\[
\langle \text{Array Type} \rangle \ ::= \langle \text{Type} \rangle “^” \langle \text{Expression} \rangle \\
\]

\[
\langle \text{Enum Type} \rangle \ ::= “enum” “{” \langle \text{List} \rangle “}” \\
\]
| node-exp            ::=  ident  
|                     | meta-op << static-arg{ ; static-arg }+ >>  
| static-arg          ::=  meta-op ::= map | fill | red | fillred | boolred  
|                       | val-exp | node-exp | usual-op  

\[\langle\text{node-def}\rangle ::= \langle\text{node}\rangle\langle\text{ident}\rangle = \langle\text{node-exp}\rangle;\]

\[\langle\text{Program}\rangle ::= (\langle\text{Package}\rangle | \langle\text{Model}\rangle | \langle\text{Model\_Instance}\rangle)^*\]

\[\langle\text{Package}\rangle ::= \langle\text{Package\_Header}\rangle [ \langle\text{Package\_Body}\rangle ] "end"\]
\[\langle\text{Package\_Header}\rangle ::= "package" \langle\text{Ident}\rangle \langle\text{P}\rangle \]
\[\quad [ "uses" \langle\text{Ident\_List}\rangle ]\]
\[\quad "provides" \langle\text{Package\_Params}\rangle\]

\[\langle\text{Package\_Params}\rangle ::= (\langle\text{Package\_Param}\rangle)\]
\[\langle\text{Package\_Param}\rangle ::= "const" \langle\text{Ident}\rangle ":" \langle\text{Type\_Identifier}\rangle \langle\text{P}\rangle ";"\]
\[\quad | "type" \langle\text{Type\_Ident\_List}\rangle \langle\text{P}\rangle ";"\]
\[\quad | \langle\text{Function\_Header}\rangle\]
\[\quad | \langle\text{Node\_Header}\rangle\]

\[\langle\text{Type\_Identifier}\rangle ::= \langle\text{Ident}\rangle ";" | \langle\text{Ident}\rangle "," \langle\text{Type\_Ident\_List}\rangle\]

\[\langle\text{Model}\rangle ::= \langle\text{Model\_Header}\rangle [ \langle\text{Body}\rangle ] "end"\]
\[\langle\text{Model\_Header}\rangle ::= "model" \langle\text{Ident}\rangle \langle\text{P}\rangle\]
\[\quad [ "uses" \langle\text{Ident\_List}\rangle ]\]
\[\quad "needs" \langle\text{Package\_Params}\rangle\]
\[\quad "provides" \langle\text{Package\_Params}\rangle\]

\[\langle\text{Model\_Instance}\rangle ::= "package" \langle\text{Ident}\rangle\]
\[\quad [ "uses" \langle\text{Ident\_List}\rangle ]\]
\[\quad "is" \langle\text{Ident}\rangle "(" \langle\text{Model\_Actual\_List}\rangle ")" \langle\text{P}\rangle ";"\]

\[\langle\text{Model\_Actual\_List}\rangle ::= \langle\text{Model\_Actual}\rangle | \langle\text{Model\_Actual}\rangle "," \langle\text{Model\_Actual\_List}\rangle\]

\[\langle\text{Model\_Actual}\rangle ::= \langle\text{Ident}\rangle \langle\text{P}\rangle | \langle\text{Expression}\rangle \langle\text{P}\rangle\]

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A.2 The syntax rules (automatically generated)

Lexical rules:

- `Ident` is an identifier, following the C standard.
- `IdentRef` is either an identifier, or a long identifier, that is an two identifiers separated by a double colon (`Ident : Ident`).
- `IntConst` is an integer notation, following the C standard.
- `RealConst` is a floating-point notation, following the C standard.

\[
\text{program} ::= \{ \text{Include} \} (\text{PackBody} | \text{PackList})
\]
\[
\text{PackList} ::= \text{OnePack} \{ \text{OnePack} \}
\]
\[
\text{OnePack} ::= \text{ModelDecl} | \text{PackDecl} | \text{PackEq}
\]
\[
\text{Include} ::= \text{include} "<string>"
\]
\[
\text{Provides} ::= [\text{provides} \text{Provide} ; \{ \text{Provide} ; \}]
\]
\[
\text{Provide} ::= \text{const} \text{Lv6Id} : \text{Type} [ = \text{Expression} ]
\]
\[
\text{unsafe node} \text{Lv6Id StaticParams Params returns Params}
\]
\[
\text{node} \text{Lv6Id StaticParams Params returns Params}
\]
\[
\text{unsafe function} \text{Lv6Id StaticParams Params returns Params}
\]
\[
\text{function} \text{Lv6Id StaticParams Params returns Params}
\]
\[
\text{type} \text{OneTypeDecl}
\]
\[
\text{ModelDecl} ::= \text{model} \text{Lv6Id} \text{Uses needs StaticParamList ;} \text{Provides}
\]
\[
\text{PackDecl} ::= \text{package} \text{Lv6Id} \text{Uses Provides} \text{body PackBody} \text{end}
\]
\[
\text{Uses} ::= [\text{uses} \text{Lv6Id} \{ , \text{Lv6Id} \} ;]
\]
\[
\text{Eq_or_Is} ::= =
\]
\[
\text{PackEq} ::= \text{package} \text{Lv6Id Eq_or_Is Lv6Id (ByNameStaticArgList)}
\]
\[
\text{PackBody} ::= \text{OneDecl} \{ \text{OneDecl} \}
\]
OneDecl ::= ConstDecl | TypeDecl | ExtNodeDecl | NodeDecl
TypedLv6IdsList ::= TypedLv6Ids { ; TypedLv6Ids }
TypedLv6Ids ::= Lv6Id { , Lv6Id } : Type
TypedValuedLv6Ids ::= TypedValuedLv6Id { ; TypedValuedLv6Id }
TypedValuedLv6Id ::= Lv6Id ( : Type | , Lv6Id { , Lv6Id } : Type | : Type = Expression )
ConstDecl ::= const ConstDeclList
ConstDeclList ::= OneConstDecl ; { OneConstDecl ; }
OneConstDecl ::= Lv6Id ( : Type | , Lv6Id { , Lv6Id } : Type | : Type = Expression | = Expression )
TypeDecl ::= type TypeDeclList
TypeDeclList ::= OneTypeDecl ; { OneTypeDecl ; }
OneTypeDecl ::= Lv6Id [ ( Type | enum { Lv6Id { , Lv6Id } } | struct { TypedValuedLv6Ids [ ; ] } ) ]
Type ::= ( bool | int | real | Lv6IdRef ) { ~ Expression }
ExtNodeDecl ::= ( extern function | unsafe extern function | extern node | unsafe extern node ) Lv6Id Params returnsParams
               | returnsParams [ ; ]
NodeDecl ::= LocalNode
LocalNode ::= node Lv6Id StaticParams Params returns Params [ ; ]
            | function Lv6Id StaticParams Params returns Params [ ; ] LocalDecls Body ( . | [ ; ] )
            | node Lv6Id StaticParams NodeProfileOpt = EffectiveNode [ ; ]
            | function Lv6Id StaticParams NodeProfileOpt = EffectiveNode [ ; ]
            | unsafe node Lv6Id StaticParams Params returns Params [ ; ] LocalDecls Body ( . | [ ; ] )
            | unsafe function Lv6Id StaticParams Params returns Params [ ; ] LocalDecls Body ( . | [ ; ] )
            | unsafe node Lv6Id StaticParams NodeProfileOpt = EffectiveNode [ ; ]
            | unsafe function Lv6Id StaticParams NodeProfileOpt = EffectiveNode [ ; ]
NodeProfileOpt ::= [ Params returnsParams ]
StaticParams ::= [ << StaticParamList >> ]
StaticParamList ::= \[ \text{StaticParam \{ ; StaticParam \}} \]

StaticParam ::= type Lv6Id
| const Lv6Id : Type
| node Lv6Id Params returns Params
| function Lv6Id Params returns Params
| unsafe node Lv6Id Params returns Params
| unsafe function Lv6Id Params returns Params

Params ::= ( [ VarDeclList ; ] )

LocalDecls ::= [ LocalDeclList ]

LocalDeclList ::= OneLocalDecl \{ OneLocalDecl \}

OneLocalDecl ::= LocalVars
| LocalConsts

LocalConsts ::= const ConstDeclList

LocalVars ::= var VarDeclList

VarDeclList ::= VarDecl \{ ; VarDecl \}

VarDecl ::= TypedLv6Ids
| TypedLv6Ids when ClockExpr
| ( TypedLv6IdsList ) when ClockExpr

Body ::= let [ EquationList ] tel

EquationList ::= Equation \{ Equation \}

Equation ::= ( assert \{ Left = \} Expression ;

Left ::= LeftItemList
| ( LeftItemList )

LeftItemList ::= LeftItem \{ , LeftItem \}

LeftItem ::= Lv6Id
| FieldLeftItem
| TableLeftItem

FieldLeftItem ::= LeftItem . Lv6Id

TableLeftItem ::= LeftItem [ ( Expression | Select ) ]

Expression ::= Constant
| Lv6IdRef
| not Expression
| \- Expression
| \text{pre} Expression
current Expression
int Expression
real Expression

Expression when ClockExpr
Expression fby Expression
Expression -> Expression
Expression and Expression
Expression or Expression
Expression xor Expression
Expression => Expression
Expression = Expression
Expression <> Expression
Expression < Expression
Expression <= Expression
Expression > Expression
Expression >= Expression
Expression div Expression
Expression mod Expression
Expression - Expression
Expression * Expression
Expression / Expression

Expression * Expression
if Expression then Expression else Expression
with Expression then Expression else Expression
# ( ExpressionList )
nor ( ExpressionList )

CallByPosExpression
[ ExpressionList ]

Expression ~ Expression
Expression | Expression
Expression [ Expression ]
Expression [ Select ]
Expression . Lv6Id

CallByNameExpression
( ExpressionList )
merge Lv6Id MergeCaseList

MergeCaseList ::= [ MergeCase ] { MergeCase }
MergeCase ::= [ ( Lv6IdRef | true | false ) -> Expression ]

ClockExpr ::= Lv6IdRef ( Lv6Id )
Lv6Id
not Lv6Id
not ( Lv6Id )

PredefOp ::= not | fby | pre | current | -> | and | or | xor | => | = |
| <> | < | <= | > | >= | div | mod | - | + | / | * | if

CallByPosExpression ::= EffectiveNode ( ExpressionList )
EffectiveNode ::= Lv6IdRef [ << StaticArgList >> ]
StaticArgList ::= StaticArg { ( , | ; ) StaticArg }
StaticArg ::= type Type
const Expression
node EffectiveNode
function EffectiveNode
PredefOp
SimpleExp
SurelyType
SurelyNode

ByNameStaticArgList ::= ByNameStaticArg { ( , | ; ) ByNameStaticArg }
ByNameStaticArg ::= type Lv6Id = Type
const Lv6Id = Expression
node Lv6Id = EffectiveNode
function Lv6Id = EffectiveNode
Lv6Id = PredefOp
Lv6Id = SimpleExp
Lv6Id = SurelyType
Lv6Id = SurelyNode
SurelyNode ::= Lv6IdRef << StaticArgList >>
SurelyType ::= ( bool | int | real ) { ~ Expression }
SimpleExp ::= Constant
              | Lv6IdRef
              | SimpleTuple
              | not SimpleExp
              | - SimpleExp
              | SimpleExp and SimpleExp
              | SimpleExp or SimpleExp
              | SimpleExp xor SimpleExp
              | SimpleExp => SimpleExp
              | SimpleExp = SimpleExp
              | SimpleExp <> SimpleExp
              | SimpleExp < SimpleExp
              | SimpleExp <= SimpleExp
              | SimpleExp > SimpleExp
              | SimpleExp >= SimpleExp
              | SimpleExp div SimpleExp
              | SimpleExp mod SimpleExp
              | SimpleExp - SimpleExp
              | SimpleExp + SimpleExp
              | SimpleExp / SimpleExp
              | SimpleExp * SimpleExp
              | if SimpleExp then SimpleExp else SimpleExp
SimpleTuple ::= [ SimpleExpList ]
SimpleExpList ::= SimpleExp { , SimpleExp }
CallByNameExpression ::= [ Lv6IdRef { [ [ Lv6IdRef with ] CallByNameParamList [ ; ] ] } ]
CallByNameParamList ::= CallByNameParam { ( ; | , ) CallByNameParam }
CallByNameParam ::= Lv6Id = Expression
Figure A.1: Lustre potatoes

ExpressionList ::= Expression { , Expression }
Constant ::= true | false | IntConst | RealConst
Select ::= Expression .. Expression
Step ::= [step Expression]
Pragma ::= { % TK_IDENT : TK_IDENT % }

A.3 Lustre History

Lustre V1, v2, v3, ..., v6

A.4 Some Lustre V4 features not supported in Lustre V6

- recursive arrays slices: use iterators instead
  [int, real] -> use structures instead

  [int, int] -> use int^2 instead
Bibliography