The Lustre V6 Reference Manual

Erwan Jahier, Pascal Raymond, Nicolas Halbwachs

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How to read this manual

This reference manual is splitted in two parts. The first chapter presents and defines the Lustre basic concepts. This *Lustre Core* language corresponds more or less to the intersection of the various versions of the Lustre language (from V1 to V6). Advance features (structured types) that changed accross version versions are not presented here.

The second chapter deals with the V6 specific features. Arrays, that were introduced in V4, are processed quite differently, using iterators. But the main novelty resides in the introduction of a package mechanism. Readers already familiar with Lustre ougth to read directly this chapter.

Chapter 1

An Overview of the Lustre Language

1.1 Introduction

This manual presents the LUSTRE language, a synchronous language based on the dataflow model and designed for the description and verification of real-time systems. In this chapter, we present the general framework that forms the basis of the language: the synchronous model, the dataflow model, and the synchronous dataflow model. Then we introduce the main features of the language through some simple examples.

The end of the chapter gives some basic elements for reading the rest of the document: it makes precise the metalanguage used to describe the syntax throughout the document and describes the lexical rules of the language.

1.1.1 Synchronous Model

The synchronous model was introduced to provide abstract primitives assuming that a program reacts instantaneously to external events. Each output of the program is assigned a precise date in relation to the flow of input events.

A discrete time scale is introduced. The time granularity is considered to be adapted a priori to the time constraints imposed by the dynamics of the environment on which the system is to react. It is verified a posteriori. Each instant on the time scale corresponds to a computation cycle, i.e., in the case of LUSTRE, to the arrival of new inputs. The synchrony hypothesis presumes that the means of computation are powerful enough for the level of granularity to be respected. In other words, the time to compute outputs in function of their inputs is less than the level of granularity on the discrete time scale. Consequently, outputs are computed and inputs are taken into account "at the same time" (with respect to the discrete time scale).

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1.1.2 Dataflow Model

The dataflow model is based on a block diagram description. A block diagram can be described either graphically, or by a system of equations. A system is made up of a network of operators acting in parallel and in time with their input rate.

This model provides the following advantages:

- maximal use made of parallelism (the only constraints are dependencies between data),
- mathematical formalization (formal verification methods),
- program construction and modification,
- ability to describe a system graphically.

1.1.3 Synchronous Dataflow Model

The synchronous dataflow approach consists in adding a time dimension to the dataflow model. A natural way of doing this is to associate time with the rate of dataflow. The entities manipulated can naturally be interpreted as functions of time. A basic entity (or flow) is a couple made up of:

- a sequence of values of a given type,
- a clock representing a suite of graduations (on the discrete time scale).

A flow takes the t^{th} value in its sequence at the t^{th} instant of its clock. For instance, the description given by the previous diagram expresses the following relation:

```
for any instant t, s_t = 2 * (x_t + y_t)
```

The time dimension is therefore an underlying feature in any description of this type of model. LUSTRE is a synchronous language based on the dataflow model. The synchronous aspect introduces constraints on the type of input/output relations that can be expressed: the output of a program at a given instant cannot depend on future inputs (causality) and can depend on only a bounded number of inputs (each cycle can memorize the value of the previous input).

1.1.4 Building a Description

A LUSTRE program describes the relations between the outputs and inputs of a system. These relations are expressed using operators, auxiliary variables, and constants. The operators can be:

- basic operators,
- more complex, user-defined, operators, called nodes.

Each description written in LUSTRE is built up of a network of nodes. A node describes the relation between its input and output parameters using a system of equations. Nodes correspond to the functions of the system and allow complex networks to be built simply by passing parameters.

The synchrony hypothesis presumes that each operator in the network responds to its inputs instantaneously.

A LUSTRE description is a list of type, constant and node declarations. The declarations can occur in any order.

The *functional behavior* of an application described in LUSTRE does not depend on the clock cycle. It is therefore possible to perform a functional validation of the application (ignoring the time validation) by testing it on a machine different from the target machine (on the development machine in particular).

Time validation is performed on the target machine. If the computation time is less than the time interval between two instants on the discrete time scale, it can be considered to be zero, and the synchrony hypothesis is satisfied. The interval between two instants on the scale is imposed by the requirements report. Computation time depends on software and hardware performance. LUSTRE is a language describing systems with a deterministic behavior from both a functional and a time point of view.

1.2 Basic Features

In this section, we present informally the main basic features of the language, through several simple examples.

A LUSTRE program or subprogram is called a *node*. LUSTRE is a functional language operating on *flows*. For the moment, let us consider that a flow is a finite or infinite sequence of values. All the values of a flow are of the same type, which is called the

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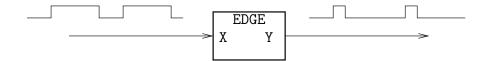


Figure 1.1: A Node

type of the flow. A program has a cyclic behavior. At the *n*th execution cycle of the program, all the involved flows take their *n*th value. A node defines one or several output parameters as functions of one or several input parameters. All these parameters are flows.

1.2.1 Simple control devices

As a very first example, let us consider a Boolean flow $X = (x_1, x_2, ..., x_n, ...)$. We want to define another Boolean flow $Y = (y_1, y_2, ..., y_n, ...)$ corresponding to the rising edge of X, i.e., such that y_{n+1} is true if and only if x_n is false and x_{n+1} is true (X raised from false to true at cycle n + 1). The corresponding node (let us call it EDGE) will take X as an input parameter and return Y as an output parameter (see Fig. 1.1). The *interface* of the node is the following:

```
node EDGE (X: bool) returns (Y: bool);
```

The definition of the output Y is given by a single *equation*:

```
Y = X and not pre(X);
```

This equation defines "Y" (its left-hand side) to be *always equal* to the right-hand side *expression* "X **and not pre**(X)". This expression involves the input parameter X and three *operators*:

- "and" and "not" are usual Boolean operators, extended to operate pointwise on flows: if $A = (a_1, a_2, \dots, a_n, \dots)$ and $B = (b_1, b_2, \dots, b_n, \dots)$ are two Boolean flows, then "A and B" is the Boolean flow $(a_1 \wedge b_1, a_2 \wedge b_2, \dots, a_n \wedge b_n, \dots)$. Most usual operators are available in that way, and are called "data-operators".
- The "**pre**" (for "*previous*") operator allows one to refer at cycle n to the value of a flow at cycle n-1: if $A=(a_1,a_2,\ldots,a_n,\ldots)$ is a flow, **pre**(A) is the flow ($nil,a_1,a_2,\ldots,a_{n-1},\ldots$). Its first value is the undefined value nil, and for any n>1, its nth value is the (n-1)th value of A

As a consequence, if $X = (x_1, x_2, ..., x_n, ...)$, the expression "X **and not pre**(X)" represents the flow $(nil, x_2 \land \neg x_1, ..., x_n \land \neg x_{n-1}, ...)$. Now, since its value at the first cycle is nil the program would be rejected by the compiler: it indicates that the output lacks an initialization. A correct equation could be:

¹Or, at least, a warning would be returned.

```
Y = false -> X and not pre(X);
```

Here, "**false**" denotes the *constant* flow, always equal to false. We have used the second specific LUSTRE operator, "->" (read "followed by") which defines initial values. If $A = (a_1, a_2, \ldots, a_n, \ldots)$ and $B = (b_1, b_2, \ldots, b_n, \ldots)$ are two flows of the same type, then "A -> B" is the flow $(a_1, b_2, \ldots, b_n, \ldots)$, equal to A at the first instant, and then forever equal to B.

So, the complete definition of the node EDGE is the following:

Example 2 The **EDGE** node

```
node EDGE (X: bool) returns (Y: bool);
let
  Y = false -> X and not pre(X);
tel
```

Once a node has been defined, it can be called from another node, using it as a new operator. For instance, let us write another node, computing the falling edge of its input parameter:

Example 3 The FALLING_EDGE node

```
node FALLING_EDGE (X: bool) returns (Y: bool);
let
  Y = EDGE(not X);
tel
```

The EDGE node is of very common usage for "deriving" a Boolean flow, i.e., transforming a "level" into a "signal". The converse operation is also very useful, it will be our second example: We want to implement a "switch", taking as input two signals "set" and "reset" and an initial value "initial", and returning a Boolean "level". Any occurrence of "set" rises the "level" to true, any occurrence of "reset" resets it to false. When neither "set" nor "reset" occurs, the "level" does not change. "initial" defines the initial value of "level". In LUSTRE, a signal is usually represented by a Boolean flow, whose value is true whenever the signal occurs. Below is a first version of the program:

Example 4 The SWITCH1 node

```
node SWITCH1 (set, reset, initial: bool) returns (level: bool);
let
  level = initial ->
    if set then true
    else if reset then false
    else pre(level);
tel
```

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which specifies that the "level" is initially equal to "initial", and then forever,

- if "set" occurs, then it becomes true
- if "set" does not occur but "reset" does, then "level" becomes false
- if neither "set" nor "reset" occur, "level" keeps its previous value (notice that "level" is *recursively defined*: its current value is defined by means of its previous value).

Moreover, if this node is intended to be used only in contexts where inputs set and reset are never true together, such an *assertion* can be specified:

```
assert(not (set and reset));
```

Otherwise, this program has a flaw: It cannot be used as a "one-button" switch, whose level changes whenever its unique button is pushed. Let "change" be a Boolean flow representing a signal, then the call

```
state = SWITCH1(change,change,true);
```

will compute the always true flow: "state" is initialized to true, and never changes because the "set" formal parameter has been given priority. To get a node that can be used both as a "two-buttons" and a "one-button" switch, we have to make the program a bit more complex: the "set" signal must be considered only when the switch is turned off. We get the following program:

Example 5 The SWITCH node

```
node SWITCH (set, reset, initial: bool) returns (level: bool);
let
   level = initial ->
      if set and not pre(level) then true
   else if reset then false
   else pre(level);
tel
```

1.2.2 Numerical examples

Recursive sequences are very easy to define in LUSTRE. For instance, the equation " $N = 0 \rightarrow pre N + 1$;" defines the sequence of natural numbers. Let us complexify this definition to build an integer sequence, whose value is, at each instant, the number of occurrences of the "true" value of a Boolean flow X:

```
N = 0 \rightarrow if X then pre N + 1 else pre N;
```

This definition does not exactly meet the specification, since it ignores the initial value of X. A well-initialized counter could be:

```
PN = 0 -> pre N;
N = if X then PN + 1 else PN;

or, simply
N = if X then (0 -> pre N) + 1 else (0 -> pre N);

or even
N = (0 -> pre N) + if X then 0 else 1;
```

Let us write a more general operator, with additional inputs:

- an integer init, which is the initial value of the counter;
- an integer incr, which must be added to the counter when X is true;
- a Boolean reset, which reset the counter to the value init, whatever be the value of X.

The complete definition of this operator is the following:

node COUNTER (init, incr: int; X, reset: bool) returns (N: int); var PN: int; let PN = init -> pre N; N = if reset then init else if X then PN + incr else PN; tel

This node can be used to define, e.g., the sequence of odd integers:

```
odds = COUNTER (0,2,true,false);
or the sequence of integers modulo 10:

mod10 = COUNTER (0,1,true,reset);
reset = true -> pre(mod10)=9;
```

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Our next example involves real values. Let f be a real function of time, that we want to integrate using the trapezoid method. The program receives two real-valued flows F and STEP, such that

$$F_n = f(x_n)$$
 and $x_{n+1} = x_n + STEP_{n+1}$

It computes a real-valued flow Y, such that

$$Y_{n+1} = Y_n + (F_n + F_{n+1}) * STEP_{n+1}/2$$

The initial value of Y is also an input parameter:

Example 7 The integrator node

```
node integrator(F,STEP,init: real) returns (Y: real);
let
Y = init -> pre(Y) + ((F + pre(F))*STEP)/2.0;
tel
```

One can try to connect two such integrators in loop to compute the functions $\sin(\omega t)$ and $\cos(\omega t)$ in a simple-minded way:

Example 8 The buggy sincos node

```
-- there is a loop !
node sincos(omega:real) returns (sin, cos: real);
let
    sin = omega * integrator(cos,0.1,0.0);
    cos = omega * integrator(-sin,0.1,1.0);
tel
node integrator(F,STEP,init: real) returns (Y: real);
let
    Y = init -> pre(Y) + ((F + pre(F))*STEP)/2.0;
```

Called on this program, the compiler would complain that there is a *deadlock*. As a matter of fact, the variables \sin and \cos instantaneously depend on each other, i.e., the computation of the nth value of \sin needs the nth value of \cos , and conversely. We have to cut the dependence loop, introducing a "pre" operator:

Example 9 The sincos node

```
node sincos(omega : real) returns (sin, cos: real);
var pcos,psin: real;
let
  pcos = 1.0 fby(cos);
  psin = 0.0 fby sin;
  sin = omega * integrator(pcos,0.1,0.0);
  cos = omega * integrator(-psin,0.1,1.0);
tel
  node integrator(F,STEP,init: real) returns (Y: real);
let
  Y = init -> pre(Y) + ((F + pre(F))*STEP)/2.0;
```

1.2.3 Multiple Equation

The node sincos above does not work very well, but it is interesting since it returns more than one output. To call such a node, LUSTRE allows *multiple definitions* to be written. Let s, c, omega be three real variables, then

```
(s, c) = sincos(omega);
```

is a correct LUSTRE equation, defining s and c to be, respectively, the first and the second result of the call.

So, the left-hand side of an equation can be a list of variables. The right hand side of such a multiple definition must denote a corresponding list of expressions, of suitable types. It can be

- a call to a node returning several outputs
- an explicit list
- the application of a *polymorphic* operator to a list

For instance, the equation

```
(\min, \max) = \text{if a < b then (a,b) else (b,a)};
```

directly defines min and max to be, respectively, the least and greatest value of a and b.

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1.2.4 Clocks

count =

tel

else 0;

Let us consider the following control device: it receives a signal "set", and returns a Boolean "level" that must be true during "delay" cycles after each reception of "set". The program is quite simple:

node STABLE (set: bool; delay: int) returns (level: bool); var count: int; let level = (count > 0);

else if false -> pre(level) then pre(count)-1

Now, suppose we want the "level" to be high during "delay" seconds, instead of "delay" cycles. The "second" will be provided as a Boolean input "second", true whenever a second elapses. Of course, we can write a new program which freezes the counter whenever the "second" is not there:

Example 11 The TIME_STABLE1 node

if set then delay

```
node TIME_STABLE1(set,second:bool; delay:int) returns (level:bool);
var count: int;
let
  level = (count > 0);
  count =
    if set then delay
    else if second then
        if false -> pre(level) then pre(count)-1
        else 0
        else (0 -> pre(count));
tel
```

We can also reuse our node "STABLE", calling it at a suitable *clock*, by *filtering* its input parameters. It consists of changing the execution cycle of the node, activating it only at some cycles of the calling program. For the delay to be counted in seconds, the node "STABLE" must be activated only when either a "set" signal or a "second" signal occurs. Moreover, it must be activated at the initial instant, for initialization purposes. So the activation clock is

```
ck = true -> set or second;
```

Now a call "STABLE((set,delay) when ck)" will feed an instance of "STABLE" with rarefied inputs, as shown by the following table:

(set,delay)	(s_1, d_1)	(s_2, d_2)	(s_3,d_3)	(s_4, d_4)	(s_5,d_5)	(s_6, d_6)	(s_7, d_7)	
ck	true	false	false	true	true	false	true	
(set,delay) when ck	(s_1, d_1)			(s_4, d_4)	(s_5, d_5)		(s_7, d_7)	

According to the data-flow philosophy of the language, this instance of "STABLE" will have a cycle only when getting input values, i.e., when ck is true. As a consequence, the inside counter will have the desired behavior, but the output will also be delivered at this rarefied rate. In order to use the result, we have first to *project* it onto the clock of the calling program. The resulting node is

Example 12 The TIME_STABLE node

```
node TIME_STABLE(set, second: bool; delay: int) returns (level: bool);
var ck: bool;
let
   level = current(STABLE((set,delay) when ck));
   ck = true -> set or second;
tel
node STABLE (set: bool; delay: int) returns (level: bool);
var count: int;
let
   level = (count > 0);
   count = if set then delay else if false -> pre(level) then pre(count)-1 else 0;
tel
```

Here is a simulation of this node:

(set,delay)	(tt,2)	(ff,2)	(ff,2)	(ff,2)	(ff,2)	(ff,2)	(ff,2)	(tt,2)	(ff,2)
(second)	ff	ff	tt	ff	tt	ff	ff	ff	tt
ck	tt	ff	tt	ff	tt	ff	ff	tt	tt
(set,delay) when ck	(tt,2)		(ff,2)		(ff,2)			(tt,2)	(ff,2)
STABLE((set,delay when ck)	tt		tt		ff			tt	tt
current(STABLE (set,delay) when ck))	tt	tt	tt	tt	ff	ff	ff	tt	tt

Chapter 2

Lustre Core

2.1 Notations

In the remaining of the document, we use the following notations: The wave arrow \rightsquigarrow means that expression evaluates into. Grammar rule are given using an extended BNF notation, where non-terminals are written $\langle like_this \rangle$ and terminals "like that".

2.2 Lexical aspects

- One-line comments start with -- and stop at the the end of the line.
- Multi-line comments start with (* and end at the next following *). Multi-line comments cannot be nested.
- *Ident* stands for identifier, following the C standard ([_a-zA-Z] [_a-zA-Z0-9]*),
- Floating and Integer stands for decimal floating point and integer notations, following C standard,

```
(Ident) (string) (Value) (comment)
```

2.3 Pragmas

A pragma is either empty, or an arbitrary string between "%" (no "%" inside the string, or some escape to be defined), or a list of such things:

```
\langle \mathcal{P} \rangle ::= (""," \langle string \rangle "",")^*
```

Example 13 Pragmas

% foo.lus:42:1%

2.4 Identifiers

Entities are generally referred to through identifiers, but they can also depend on a package instance (like in BIN8::binary). So we distinguish between $\langle Ident \rangle$, and $\langle Identifier \rangle$:

```
\langle Identifier \rangle ::= \langle Ident \rangle \mid \langle Ident \rangle "::"\langle Ident \rangle
```

2.5 Types

```
 \langle \textit{Type\_Decl} \rangle \quad ::= \quad \text{"type"} \, \langle \textit{Ident} \rangle^+ \, \langle \mathcal{P} \rangle \, \text{";"} \\ \quad | \quad \text{"type"} \, \langle \textit{Ident} \rangle \, \text{"=" } \, \langle \textit{Type} \rangle \, \langle \mathcal{P} \rangle \, \text{";"} \\ \langle \textit{Type} \rangle \quad ::= \quad \langle \textit{Ident} \rangle \, | \, \langle \textit{Record\_Type} \rangle \, | \, \langle \textit{Enum\_Type} \rangle \\ \langle \textit{Record\_Type} \rangle \quad ::= \quad \text{"struct"} \, \text{"} \, \langle \text{Field\_List} \rangle \, \text{"} \, \rangle \\ \langle \textit{Field\_List} \rangle \quad ::= \quad \langle \textit{Field} \rangle \, | \, \langle \textit{Field} \rangle \, \text{","} \, \langle \textit{Field\_List} \rangle \\ \langle \textit{Field} \rangle \quad ::= \quad \langle \textit{Ident} \rangle \, \text{":"} \, \langle \textit{Type} \rangle \\ \langle \textit{Array\_Type} \rangle \quad ::= \quad \langle \textit{Type} \rangle \, \text{"?"} \, \langle \textit{Expression} \rangle \\ \langle \textit{Enum\_Type} \rangle \quad ::= \quad \text{"enum"} \, \text{"} \, \{ \text{"} \, \langle \textit{Ident\_List} \rangle \, \text{"} \} \, \text{"}
```

Example 14 Type Declarations

```
type alias = int;
type pair = struct { a:int; b:int };
type color = enum { blue, white, black };

node type_decl(i1, i2: int) returns (x: pair);
let
    x= pair {a=i1; b=i2};
tel
```

2.6 Constants and Variables

```
Example 15 Constant Declarations
```

```
const x,y,z : int; verbose = true; pi:real = 3.14159265359;
```

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2.7 Functions and Nodes

The main way of structuring Lustre equations is via *nodes*. A memoryless node can be declared a *function*. A Lustre node is made of an interface (input/output declarations) and a set of equations defining the outputs.

```
(Node_Decl)
                            ::= \langle Node\_Header \rangle [\langle FN\_Body \rangle]
                                  ["unsafe"]["extern"]("node" | "function")"(" (FN_Params)")"
(Node_Header)
                            ::=
                                         "returns" "("\langle FN\_Params \rangle")" \langle \mathcal{P} \rangle ";"
〈FN_Params〉
                                 (Var_Decl_List)
                            ::=
                                   ⟨Var_Decl⟩ | ⟨Var_Decl⟩ ";" ⟨Var_Decl_List⟩
⟨Var_Decl_List⟩
                            ::=
                                 \langle Ident\_List \rangle ":" \langle Type \rangle [ \langle Declared\_Clock \rangle ] \langle P \rangle
〈Var_Decl〉
                           ::=
                                 "when" \langle Clock \rangle
(Declared_Clock)
\langle Clock \rangle
                                 (Identifier)
                            ::=
\langle FN\_Body \rangle
                                 ( \langle Local_Decl \rangle )* "let" \langle Equation_List \rangle "tel" [ ";" ]
                            ::=
                                 \langle Local_Var_Decl \rangle \langle Local_Const_Decl \rangle
〈Local_Decl〉
                           ::=
                                 "var" (Var_Decl_List) ";"
\Local_Var_Decl\
                            ::=
                                  "const" ( \( \lant \) [ ":" \( \text{Type} \) ] "=" \( \text{Expression} \) ";" \( \)^+
\langle Local\_Const\_Decl \rangle ::=
```

Example 16 Node

```
node sum(A:int) returns (S:int)
let
    S=A+(0->pre(S));
tel
function plus(A,B:int) returns (X:int)
let
    X=A+B;
tel
```

Functions and nodes can be extern, in which case they should be preceded by the extern keyword, and have an empty body. Of course if an extern entity is declared as a function while it has memory, the behavior of the whole program is unpredictable.

```
extern node foo_with_mem(A:int, B:bool, C: real) returns (X:int, Y: real);
extern function sin(A:real) returns (sinx: real);
```

Extern nodes that performs side-effects should be declared as unsafe. A node that uses unsafe node is unsafe (a warning is emitted if a node is unsafe while it is not declared as such).

unsafe extern node rand() returns (R: real); unsafe node randr(r:real) returns (R: int); let R = r*rand(); tel

2.8 Equations

```
 \langle Equation\_List \rangle \quad ::= \quad \langle Eq\_or\_Ast \rangle \mid \langle Eq\_or\_Ast \rangle \langle Equation\_List \rangle 
 \langle Eq\_or\_Ast \rangle \quad ::= \quad \langle Equation \rangle \mid \langle Assertion \rangle 
 \langle Equation \rangle \quad ::= \quad \langle Left\_Part \rangle \quad "=" \langle Right\_Part \rangle \langle \mathcal{P} \rangle \quad ";" 
 \langle Left\_Part \rangle \quad ::= \quad "(" \langle Left\_List \rangle ")" \mid \langle Left\_List \rangle 
 \langle Left\_List \rangle \quad ::= \quad \langle Left \rangle \quad ("," \langle Left \rangle)^* 
 \langle Left \rangle \quad ::= \quad \langle Left \rangle \quad ("," \langle Left \rangle)^* 
 \langle Left \rangle \quad ::= \quad \langle Identifier \rangle \mid \langle Left \rangle \langle Selector \rangle 
 \langle Selector \rangle \quad ::= \quad "." \langle Ident \rangle \mid "[" \langle Expression \rangle [ \langle SelTrancheEnd \rangle ] \quad "]" 
 \langle SelTrancheEnd \rangle \quad ::= \quad "." \langle Expression \rangle 
 \langle Assertion \rangle \quad ::= \quad "assert" \langle Expression \rangle \langle \mathcal{P} \rangle \quad ";"
```

```
Example 19 Equations
...
x = a[2]; -- accessing an array
slice = a[2..5] -- get an array slice (i.e., a sub array)
...
```

2.9 Assertions

```
node divide(i1,i2:int) returns (res:int);
let
   assert(i2<>0);
   o = i1/i2;
tel
```

Assertions takes boolean expressions. Tools that parse lustre program can use it (or ignore it). For instance, the Lesar model-checker uses them to cut some some paths in the state graph. Lustre interpreters generate a warning when an assertion is violated.

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2.10 Expressions

Lustre is a data-flow language: each variable or expression denotes a infinite sequence of values, i.e., a *stream*. All values in a stream are of the same data type, which is simply called the type of the stream. A variable X of type τ represents a sequence of values $X_i \in \tau$ with $i \in \mathbb{N}$.

For instance, the predefined constant true denotes the infinite sequence of Boolean values ($true, true, \cdots$), and the integer constant 42 denotes the infinite sequence (42, 42, \cdots).

Three predefined types are provided: Boolean, integer and real. All the classical arithmetic and logic operators over those types are also predefined. We say that hey are *combinationnal* in the sense that they are operating pointwise on streams.

Example 21 Expressions

```
X + Y denotes the stream (X_i + Y_i)_i with i \in \mathbb{N}.
```

Z = X + Y defines the stream Z from the streams X and Y

```
\langle Expression \rangle
                              (Identifier)
                        ::=
                               (Value)
                              "(" (Expression_List) ")"
                               \langle Record\_Exp \rangle
                               \langle Array\_Exp \rangle
                               (Unary) (Expression)
                               ⟨Expression⟩ ⟨Binary⟩ ⟨Expression⟩
                               ⟨Nary⟩ ⟨Expression⟩
                               "if" (Expression) "then" (Expression) "else" (Expression)
                               \langle Call \rangle
                               ⟨Expression⟩ ⟨Selector⟩
                              ⟨Expression⟩ | ⟨Expression⟩ "," ⟨Expression_List⟩
(Expression_List)
                        ::=
                              ⟨Ident⟩ "{" ⟨Field_Exp_List⟩ "}"
\langle Record\_Exp \rangle
                        ::=
                             ⟨Field_Exp⟩ | ⟨Field_Exp⟩ ";" ⟨Field_Exp_List⟩
\Field_Exp_List\
                        ::=
\langle Field\_Exp \rangle
                              ⟨Ident⟩ "=" ⟨Expression⟩
                        ::=
                              "[" \( Expression List \) "]" \( \lambda Expression \rangle "\cdot" \) "\( Expression \rangle \)
\langle Array_Exp \rangle
                        ::=
                              \langle User\_Op \rangle \langle P \rangle "(" \langle Expression\_List \rangle")"
\langle Call \rangle
                        ::=
〈User_Op〉
                             (Identifier)
                        ::=
                               ⟨Iterator⟩ << ⟨User_Op⟩ "," ⟨Expression⟩ >>
                              "map" | "red" | "fill" | "fillred" | "boolred"
\langle Iterator \rangle
```

Example 22 Array Expressions

```
array2 = [1,2];
array10 = 42^10;
array12 = array2 | array10; -- concat
slice = array12[1..10]; -- slice
array_sum = map<<+, 10>>(array10,slice);
max_elt = red<<max, 10>>(array_sum)
```

Example 23 Struct Expressions

```
type Toto = struct
x : int = 1;
y : int = 2;
[...]
s = Toto x = 12; y = 13;
ns = Toto s with x = 42;
x = s.x + ns.y;
```

2.11 Combinational operators

An operator is a predefined Lustre node.

```
\langle Unary \rangle ::= "-" | "not" \\ \langle Binary \rangle ::= "+" | "-" | "*" | "\div" | "mod" \\ | ">" | "\<" | "\<=" | "\<=" | "\<>" | "=" \\ | "or" | "and" | "xor" | "=>" \\ \langle Nary \rangle ::= "\pm" | "nor"
```

2.12 Temporal operators

In addition to the combinationnal operators, Lustre provides a delay (pre) and an initialization operator (->).

```
\langle Unary \rangle ::= "pre" | "current" \langle Binary \rangle ::= | "->" | "when" | "fby"
```

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Example 24 Temporal operators

```
The equation

pX = 0 -> pre(X) + 1; -- or pre X + 1

pY = 0 fby Y + 1; -- or 0 fby(y)+1

defines X and Y as the stream (0,1,2,3, ...)
```

Example 25 Operators

```
X_on_c = X when C;
curr_X_on_base = current(X_on_C);
```

2.13 Operators Priority

The list below shows the relative precedences and associativity of operators. The constructions with lower precedence come first.

- "else"
- "->"
- "=>" (right associative)
- "or" "xor"
- "and"
- "<" "<=" ">=" ">" ">" "<>"
- "not"
- "+" "-" (left associative)
- "*" "/" "%" "mod" "div" (left associative)
- "when"
- "-" (unary minus) "pre" "current"

2.14 Clocks

It also provides a notion of clock, with a sampling operator (when) and a dual projection operator current.

node TIME_STABLE(set, second: bool; delay: int) returns (level: bool); var ck: bool; let level = current(STABLE((set,delay) when ck)); ck = true -> set or second; tel node STABLE (set: bool; delay: int) returns (level: bool); var count: int; let level = (count > 0); count = if set then delay else if false -> pre(level) then pre(count)-1 else 0; tel

2.15 Abstract types

At last, complex data types and functions are handled via a mechanism of *abstract types* (also called *imported types*). An imported type is defined as a simple name. Abstract constants and function manipulating such types can be declared. The way those external items are effectively launched from a Lustre program depends on the back-ends of the compiler.

2.16 Programs

A Lustre-core program is a set of constant, types, function and node Declarations.

Chapter 3

Lustre V6

In this chapter, we present the Lustre V6 specific features, that are not part of the basic Lustre. In Section 3.1 we introduce the Lustre V6 Structured data types (records, enumerations, arrays). In Section 3.2 we introduce array iterators. In Section 3.4 we introduce The Lustre V6 package system which aims at introduced a new level of structuration and modularity as well as namespace facilities. In Section 3.5 we provide the predefined entities (constant, type, operator and package) of Lustre V6. In Section A.1 we provide the Lustre V6 syntax rules. In Section 3.7 we provide a complete and commented program example.

3.1 User-defined data types

Structured data type are introduced in Lustre V6. We give an informal description of them in this Section. The syntax for their declaration and used is provided in Section A.1.

Enumerations. Enumerations are similar to enumerations in other languages.

```
type color1 = enum { blue, white, black };
type color2 = enum { green, orange, yellow };

node enum0(x: color1) returns (y: color2);
let
    y = if x = blue then green else if x = white then orange else yellow;
tel
```

Records. The declaration of a structured type is (semantically) equivalent to the declaration of an abstract type, a collection of field-access functions, and a constructor function.

type complex = { re : real ; im : real }; const j = { re = -sqrt(3)/2; im = sqrt(3)/2 }; -- a complex constant node get_im(c:complex) returns (x:real) ; let x = c.im; tel

Arrays. Here are a few examples of array declarations and definitions.

```
type matrix_3_3 = int ^ 3 ^ 3 ; -- to define a type matrix of integers

const m1 = 0 ^ 3 ^ 3; -- a constant of type matrix_3_3

const m2 = [1,2,3] ^ 3; -- another constant

const sm1 = m2[2] -- a constant of type int^3 (\sim [1,2,3])
```

```
 \langle Type\_Decl \rangle \qquad ::= \ \text{"type"} \ \langle Ident \rangle^+ \ \langle P \rangle \text{";"} \\ | \ \text{"type"} \ \langle Ident \rangle \text{"=" } \ \langle Type \rangle \ \langle P \rangle \text{";"} \\ | \ \langle Type \rangle \qquad ::= \ \langle Ident \rangle \ | \ \langle Record\_Type \rangle \ | \ \langle Lnum\_Type \rangle \\ | \ \langle Record\_Type \rangle \qquad ::= \ \text{"} \ \langle Field\_List \rangle \text{"} \ \rangle \\ | \ \langle Field\_List \rangle \qquad ::= \ \langle Field \rangle \ | \ \langle Field \rangle \text{";"} \ \langle Field\_List \rangle \\ | \ \langle Field \rangle \qquad ::= \ \langle Ident \rangle \text{":"} \ \langle Type \rangle \\ | \ \langle Array\_Type \rangle \qquad ::= \ \langle Type \rangle \text{"``"} \ \langle Expression \rangle \\ | \ \langle Enum\_Type \rangle \qquad ::= \ \text{"enum"} \ " \ \langle Ident\_List \rangle \text{"} \ \rangle
```

TO DO !!!slices

3.2 Array iterators

One the main novelty of Lustre-V6 is to provide a (restricted) notion of higher-order programming by defining *array iterators* to operate over arrays. Iterators replace the use of Lustre V4 homomorphic extension [?].

Using node expressions. In Lustre V6, a node denotation is not necessarily a simple identifier, since a node can be "built" by instantiating an iterator with static arguments. A node expression is then defined by:

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A static argument may be a statically evaluable expression (with the restriction that it can be statically evaluated), or a node expression as defined below. With some restrictions, it is also possible to use the "usual denotation" of the predefined operators (like +, >= etc). See ?? for a complete discussion on the use of predefined operators.

The semantics of iterators are presented in the sequel.

Using node expressions. The rules presented here complete the basic ones (chapter ??).

Node expressions can be used as static parameters (see above), in value expressions:

```
val-exp ::= node-exp(val-exp{ , val-exp} }^+)
```

Node expressions can also be used to define a node:

```
\langle node\text{-}def \rangle ::= \langle node \rangle \langle ident \rangle = \langle node\text{-}exp \rangle;
```

3.2.1 From scalars to arrays: fill

The fill iterator transforms a scalar-to-scalar node into a scalar-to-array node. The node argument must have a single input (input accumulator), a first output of the same type (output accumulator), and at least one another output.

The figure 3.1 shows the data-flow scheme of the fill iterator.

```
Definition 1: fill
```

```
For any integer constant n and any node N of type: \tau \to \tau \times \theta_1 \times \ldots \times \theta_\ell, fill<<N; n>> denotes a node of type: \tau \to \tau \times \theta_1 \hat{\ } n \times \ldots \times \theta_\ell \hat{\ } n such that (a_{out}, Y_1, \cdots, Y_\ell) = \text{fill} <<\text{N}; n>> (a_{in}) if and only if, \exists a_0, \cdots a_n such that a_0 = a_{in}, a_n = a_{out} and \forall i = 0 \cdots n-1, (a_{i+1}, Y_1[i], \cdots, Y_\ell[i]) = \text{N}(a_i)
```

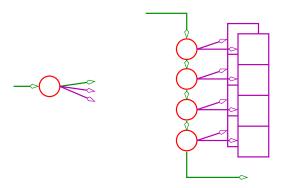


Figure 3.1: A node N (1 input, 1+2 outputs), and the node fill<<N; 4>>

```
fill<<incr; 4>>(0) \( \times \) (4, [0,1,2,3])

with:

node incr(ain : int) returns (aout, z : int);
let
    z = ain; aout = ain + 1;
tel
```

3.2.2 From arrays to scalars: red

The red iteretor transforms a scalar-to-scalar node into an array-to-scalar node. The node argument must have a single output, a first input of the same type, and at least another input.

The figure 3.2 shows the data-flow scheme of the reduce iterator.

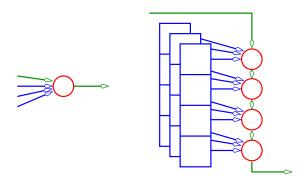


Figure 3.2: A node N (1+3 inputs, 1 output), and the node red<<N; 4>>

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Definition 2: red

For any integer constant n and any node N of type:

$$\tau \times \tau_1 \times \ldots \times \tau_k \to \tau$$
,

red<<N; n>> denotes a node of type:

$$\tau \times \tau_1 \hat{n} \times \ldots \times \tau_k \hat{n} \to \tau$$

such that

$$\mathbf{a}_{out} = \text{red} << \mathbb{N}; \quad \mathbf{n}>> (\mathbf{a}_{in}, \mathbf{X}_1, \cdots, \mathbf{X}_k)$$

if and only if, $\exists a_0, \dots a_n$ such that $a_0 = a_{in}$, $a_n = a_{out}$ and

$$\forall i = 0 \cdots n-1, a_{i+1} = \mathbb{N}(a_i, X_1[i], \cdots, X_k[i])$$

Example 31 red

```
red<<+; 3>>(0, [1,2,3]) \leftrightarrow 6
```

3.2.3 From arrays to arrays: fillred

The fillred iterator generalizes the fill and the red ones. It maps a scalar-to-scalar node into a "scalar and array"-to-"scalar and array" node. The node argument must have a (first) input and a (first) output of the same type, and at least one more input and one more output. The degenerated case with no other input (resp. output) corresponds to the fill (resp. red) iterators.

The Figure 3.3 shows the data-flow scheme of the fillred iterator.

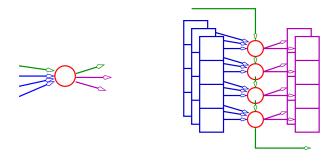


Figure 3.3: A node N (1+3 inputs, 1+2 outputs), and the node +fillred<<N; 4>>

Definition 3: fillred

For any integer constant n and any node N of type:

$$\tau \times \tau_1 \times \ldots \times \tau_k \to \tau \times \theta_1 \times \ldots \times \theta_\ell$$

where k and $\ell \ge 0$; fillred<<N; n>> denotes a node of type:

$$\tau \times \tau_1 \hat{n} \times \ldots \times \tau_k \hat{n} \rightarrow \tau \times \theta_1 \hat{n} \times \ldots \times \theta_\ell \hat{n}$$

such that

$$(a_{out}, Y_1, \dots, Y_\ell) = fillred << N; n>> (a_{in}, X_1, \dots, X_k)$$

if and only if, $\exists a_0, \dots, a_n$ such that $a_0 = a_{in}$, $a_n = a_{out}$, and

$$\forall i = 0 \cdots n - 1, (a_{i+1}, Y_1[i], \cdots, Y_{\ell}[i]) = N(a_i, X_1[i], \cdots, X_k[i])$$

Example 32 fillred

A classical exemple is the binary adder, obtained by mapping the "full-adder". The unsigned sum Z of two bytes X and Y, and the corresponding overflow flag can be obtained by:

```
(over, Z) = fillred<<fulladd, 8>>(false, X, Y)
where:

node fulladd(cin, x, y : bool) returns (cout, z : bool);
let
    z = cin xor x xor y;
    cout = if cin then x or y else x and y;
tel
```

3.2.4 From arrays to arrays, without an accumulator: map

The map iterator transforms a scalar-to-scalar node into an array-to-array node. The figure 3.4 shows the data-flow scheme of the map iterator.

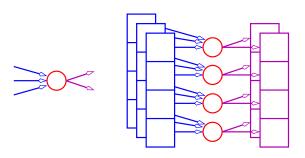


Figure 3.4: A node N (3 inputs, 2 outputs), and the node map<<N; 4>>

Definition 4: map

```
For any integer constant n and any node N of type: \tau_1 \times \ldots \times \tau_k \to \theta_1 \times \ldots \times \theta_\ell, map<<N; n>> denotes a node of type: \tau_1 \hat{\ } n \times \ldots \times \tau_k \hat{\ } n \to \theta_1 \hat{\ } n \times \ldots \times \theta_\ell \hat{\ } n such that (Y_1, \cdots, Y_\ell) = \max < N; \ n>> (X_1, \cdots, X_k) if and only if \forall i = 0 \cdots n-1, \ (Y_1[i], \cdots, Y_\ell[i]) = \mathbb{N}(X_1[i], \cdots, X_k[i])
```

Example 33 map

```
map <<+; 3>>([1,0,2],[3,6,-1]) <math>\leftrightarrow [4,6,1]
```

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3.2.5 From Boolean arrays to Boolean scalar: boolred

Definition 5: boolred

This iterator has 3 integer static input arguments:

```
boolred<<i; j; k>>
```

such that $0 \le i \le j \le k$ and k > 0.

It denotes a combinational node whose profile is bool^k \rightarrow bool, and whose semantics is given by: the output is true if and only if at least i and at most j elements are true in the input array.

Note that this iterator can be used to implement efficiently the diese and the nor operators:

Example 34 boolred

```
#(a1, ..., an) \rightsquigarrow boolred<<0,1,n>>(a1, ..., an) nor(a1, ..., an) \rightsquigarrow boolred<<0,0,n>>(a1, ..., an)
```

3.2.6 Lustre iterators versus usual functional languages ones.

Note that those iterators are more general than the ones usually provided in functional language librairies. Indeed, the arity of the node is not fixed. For example, in a usual functional language, you would have map and map2 with the following profile:

```
map : ('a -> 'b) -> (a' array) -> (b' array)
map2 : ('a -> 'b -> 'c) -> (a' array) -> (b' array) -> (c' array)
```

whereas the map iterator we define here would have the following profile in the functional programming world:

```
mapn : ('a<sub>1</sub> -> 'a<sub>2</sub> -> ... -> 'a<sub>n</sub>) -> (a<sub>1</sub>' array) -> (a<sub>2</sub>' array) -> ... -> (a<sub>n-1</sub>' array) -> (a<sub>n</sub>' array)
```

Note that it even note possible to give a milner-style type to describe this iterator. Indeed, the type of the node depends on the size of the array; it would therefore require a dependant-type system.

3.3 Parametric nodes

node can be parametrised by constants, types, and nodes.

Example 35 Parametric Node

Example 36 Parametric Node

```
node toto_n<<
    node f(a, b: int) returns (x: int);
    const n : int
    >>(a: int) returns (x: int^n);
var v : int;
let
    v = f(a, 1);
    x = v^n;
tel
node param_node = toto_n<<Lustre::iplus, 3>>;
```

nodes can even be defined recursively using the "with" construct

Example 37 Recursive Node

```
node consensus<<const n : int>>(T: bool^n)
returns (a: bool);
let
   a = with (n = 1) then T[0]
      else T[0] and consensus << n-1 >> (T[1 .. n-1]);
tel
node consensus2 = consensus<<8>>;
```

3.4 Packages and models

A lustre V6 program is a list of packages, models (generic packages), and model instances.

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Basic lustre programs are still accepted by the lustre V6 compiler, which consider implicitely that a program without package annotations:

- uses no other package
- provides all the package parameters it defines
- is part of a package that is made of the file name

```
\langle Program \rangle ::= (\langle Package \rangle \mid \langle Model \rangle \mid \langle Model Instance \rangle)^*
```

A package is made of:

- a header, which gives the name of the package, the entities exported by the package, and the packages and models used by the package;
- and an optional body which consists of the declarations of the entities defined by the package. When the body is not given, the package is external.

```
⟨Package_Header⟩ [ ⟨Package_Body⟩ ] "end"
(Package)
(Package_Header)
                            ::= "package" \langle Ident \rangle \langle \mathcal{P} \rangle
                                          [ "uses" \langle Ident \perp List \rangle ]
                                          "provides" (Package Params)
                            ::= (\langle Package\_Param \rangle)^+
(Package_Params)
                            ::= "const" \langle Ident \rangle ":" \langle Type\_Identifier \rangle \langle P \rangle ";"
(Package_Param)
                                   "type" \langle Tupe\_Ident\_List \rangle \langle P \rangle ";"
                                   (Function_Header)
                                    (Node_header)
(Type_Identifier)
                            ::= \langle Identifier \rangle
                            ::= \(\lambda Ident\rangle ";" \rangle \( Ident\rangle "," \rangle Type Ident List\rangle \)
(Type_Ident_List)
```

The output parameters of packages can be constants, types, nodes, or functions.

```
package pack
  uses pack1, pack2;
  provides
    const pi,e:real;
    type t1,t2;
    function cos(x:real) returns (y:real);
    node rising_edge(x:bool) returns (re:bool);
body
    ...
end
```

package complex provides type t; -- Encapsulation const i:t; node re(c: t) returns (r:real); body type t = struct { re : real ; im : real }; const i:t = t { re = 0. ; im = 1. }; node re(c: t) returns (re:real);

let re = c.re; tel;
node complex = re;

A *model* has an additional section (needs ...) in its header which declares the formal parameters of the model. A model is somehow a parametric package.

```
 \langle Model \rangle \qquad ::= \langle Model Header \rangle \left[ \langle Body \rangle \right] \text{``end''} \\ \langle Model Header \rangle \qquad ::= \text{``model''} \langle Ident \rangle \langle \mathcal{P} \rangle \\ \qquad \qquad \left[ \text{``uses''} \langle Ident List \rangle \right] \\ \qquad \text{``needs''} \langle Package Params \rangle \\ \qquad \text{``provides''} \langle Package Params \rangle
```

```
model model_example
needs
    type t;
    const pi;
provides
    node n(init, in : t) returns (res : t);
    body
        node n(init, in: t) returns (res: t);
    let
        res = init -> pre in;
    tel
    end
```

A *model instance* defines a package as an instance of a model by providing input parameters. It declares the list of packages it uses. It provides all objects exported by the model and its effective parameters.

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```
\langle Model\_Instance \rangle \quad ::= \text{``package''} \langle Ident \rangle \\ \quad [\text{``uses''} \langle Ident\_List \rangle \text{]} \\ \quad \text{``is''} \langle Ident \rangle \text{``(''} \langle Model\_Actual\_List \rangle \text{'`)''} \langle \mathcal{P} \rangle \text{``;''} \\ \langle Model\_Actual\_List \rangle \quad ::= \langle Model\_Actual \rangle \text{ | } \langle Model\_Actual \rangle \text{``,''} \langle Model\_Actual\_List \rangle \\ \langle Model\_Actual \rangle \quad ::= \langle Identifier \rangle \langle \mathcal{P} \rangle \text{ | } \langle Expression \rangle \langle \mathcal{P} \rangle
```

The user decide which node is the main one at compile time, following the Lustre V4 tradition. For example the node bar of package p in file foo.lus will be used as main node if the following command is launched: lv6 foo.lus -main p::bar.

Example 41 Model instance

```
Here is how to obtain packages by instanciating the model given in Example 40:

package model_instance_examble_bool is model_example(t=bool,pi=3.14);

package model_instance_examble_int is model_example(t=int,pi=3.14);

In this way, model_instance_examble_bool is a package that provides the node:

n(init, in : bool) returns (res : bool)
```

3.4.1 Package body

```
 \begin{array}{lll} \langle \textit{Package\_Body} \rangle & ::= & [~~\textbf{body}"~] \, \langle \textit{Entity\_Decl} \rangle^+ \\ \langle \textit{Entity\_Decl} \rangle & ::= & \langle \textit{Const\_Decl} \rangle \\ & | & \langle \textit{Type\_Decl} \rangle \\ & | & \langle \textit{Model\_Instance} \rangle \\ & | & \langle \textit{Function\_Decl} \rangle \\ & | & \langle \textit{Node\_Decl} \rangle \end{array}
```

Example 42 Package body

3.5 Predefined entities

a package is a set of definitions of entities: types, constants and operators (nodes or functions).

a model can have as parameters a type, a constant, or a node.

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3.6 The Merge operator

Example 43 The Merge operator

```
type piece = enum { Pile, Face, Tranche };
node test_merge(clk: piece; i1, i2, i3 : int)
returns (y: int);
let
 y = test_merge_clk(clk, i1 when Pile(clk),
                          i2 when Face(clk),
                          i3 when Tranche(clk));
node test_merge_clk(clk: piece;
   i1 : int when Pile(clk) ;
   i2 : int when Face(clk);
   i3 : int when Tranche(clk))
returns (y: int);
let
    y = merge clk
        ( Pile -> (0->i1))
        ( Face -> i2)
        ( Tranche -> i3);
node merge_bool_alt(clk : bool ;
                    i1 : int when clk;
                    i2 : int when not clk)
returns (y: int);
let
    y = merge clk (true -> i1) (false-> i2);
node merge_bool_ter(clk : bool ;
                   i1 : int when clk;
                    i2 : int when not clk)
returns (y: int);
    y = merge clk (false-> i2) (true -> i1);
tel
```

clk	Pile	Pile	Face	Tranche	Pile	Face
i1	1	2			3	
i2			1			2
i3				1		
y	1	2	1	1	3	2

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3.7 A complete example

Example 44 Detecting the stability of a flow

```
-- Time-stamp: <modified the 18/12/2017 (at 15:20) by Erwan Jahier>
-- Computes the speed (of some vehicle with wheels) out of 2 sampled inputs:
-- + Rot, true iff the wheel has performed a complete rotation
-- + Tic, true iff some external clock has emitted a signal indicating that
          some constant amount of time elapsed (e.g., 100 ms)
-- This example was inspired from a real program in a train regulating system
const period = 0.1; -- in seconds
const wheel_girth = 1.4; -- in meter
const size = 20; -- size of the sliding window used to compute the speed
node compute_speed(Rot, Tic: bool) returns (Speed:real);
var d,t,dx,tx:real;
  dx = if Rot then wheel_girth else 0.0;
  tx = if Tic then period else 0.0;
  d = sum << size, 0.0 >> (dx);
  t = sum<<size,period>>(tx);
  -- the speed is actually the average speed during the last "size*period" seconds
  Speed = (d/t);
  -- nb : yes there can be some division by zero! For instance if the vehicle
  -- overtakes the speed of size*wheel_girth/period
  -- (i.e., with size=20, period=0.1, wheel_girth=1.4, if the speed is > 1008km/h)
  -- This means that for high-speed vehicle, one needs to increase "size".
-- The idea is to call the node that do the computation only when needed, i.e.,
-- when Tic or Rot is true.
node speed(Rot, Tic: bool) returns (Speed:real);
var
  TicOrRot : bool;
  NewSpeed : real when TicOrRot;
let
  TicOrRot = Tic or Rot;
  NewSpeed = compute_speed(Rot when TicOrRot, Tic when TicOrRot);
  Speed = current(NewSpeed);
-- computes the sum of the last d values taken by s
node sum<<const d: int; const init:real>>(s: real) returns (res:real);
  a,pre_a: real^d; -- circular array
  i: int;
let
  i = 0 \text{ fby } i + 1;
 pre_a = (init^d) fby a;
 a = assign << d>>(s, i mod d, pre_a); 40
 res =red<<+; d>>(0.0, a);
  - assign the jth element of an array to a value. v.(j) <- i
type update_acc = { i: int; j: int; v: real };
function update_cell_do<<const d: int>>(acc: update_acc; cell: real)
returns (nacc: update_acc; ncell: real);
```

Appendix A

Appendix

A.1 The syntax rules summary

```
\langle \mathcal{P} \rangle ::= ("%" \langle string \rangle "%")^*
```

```
\langle Identifier \rangle ::= \langle Ident \rangle \mid \langle Ident \rangle "::" \langle Ident \rangle
```

```
 \langle Type\_Decl \rangle \qquad ::= \text{"type"} \langle Ident \rangle^+ \langle \mathcal{P} \rangle \text{";"} \\ | \text{"type"} \langle Ident \rangle \text{"=" } \langle Type \rangle \langle \mathcal{P} \rangle \text{";"} \\ | \langle Type \rangle \qquad ::= \langle Ident \rangle \mid \langle Record\_Type \rangle \mid \langle Array\_Type \rangle \mid \langle Enum\_Type \rangle \\ | \langle Record\_Type \rangle \qquad ::= \text{"struct" } \text{"} \text{" } \langle Field\_List \rangle \text{"} \text{"} \\ | \langle Field\_List \rangle \qquad ::= \langle Field \rangle \mid \langle Field \rangle \text{"," } \langle Field\_List \rangle \\ | \langle Field \rangle \qquad ::= \langle Ident \rangle \text{":" } \langle Type \rangle \\ | \langle Array\_Type \rangle \qquad ::= \langle Type \rangle \text{"^ "} \langle Expression \rangle \\ | \langle Enum\_Type \rangle \qquad ::= \text{"enum" } \text{"} \text{"} \langle Ident\_List \rangle \text{"} \} \text{"}
```

```
 \begin{array}{lll} \langle Const\_Decl \rangle & ::= & \text{``const''} \left( \langle One\_Const\_Decl \rangle \right)^{+} \\ \langle One\_Const\_Decl \rangle & ::= & \langle Ident\_List \rangle \text{'`:''} \langle Type \rangle \langle \mathcal{P} \rangle \text{'`;''} \\ & & & | & \langle Ident \rangle \text{''=''} \langle Expression \rangle \langle \mathcal{P} \rangle \text{'`;''} \\ & & & | & \langle Ident \rangle \text{'':''} \langle Type \rangle \text{''=''} \langle Expression \rangle \langle \mathcal{P} \rangle \text{'';''} \\ & & & | & \langle Ident\_List \rangle & ::= & \langle Ident \rangle & | & \langle Ident\_List \rangle \\ \end{array}
```

```
⟨Node_Decl⟩
                               ⟨Node_Header⟩ [ ⟨FN_Body⟩ ]
                         ::=
                              ["unsafe"]["extern"]("node" | "function")"(" \langle FN_Params \rangle ")"
(Node_Header)
                         ::=
                                     "returns" "("(FN_Params)")" (P) ";"
                               ⟨Var_Decl_List⟩
〈FN_Params〉
                         ::=
                               (Var_Decl) | (Var_Decl) ";" (Var_Decl_List)
⟨Var_Decl_List⟩
                         ::=
                               ⟨Ident_List⟩ ":" ⟨Type⟩ [ ⟨Declared_Clock⟩ ] ⟨P⟩
⟨Var_Decl⟩
                         ::=
(Declared_Clock)
                              "when" \langle Clock \rangle
                         ::=
\langle Clock \rangle
                             (Identifier)
                         ::=
                         ::= (\langle Local_Decl\rangle )* "let" \langle Equation_List\rangle "tel" [ ";" ]
\langle FN\_Body \rangle
⟨Local_Decl⟩
                             \langle Local_Var_Decl\rangle \langle Local_Const_Decl\rangle
                         ::= "var" \(\forall Var_Decl_List\) ";"
\Local_Var_Decl\
\langle Local\_Const\_Decl \rangle ::= "const" ( \langle Ident \rangle [":" \langle Type \rangle ] "=" \langle Expression \rangle ";" )^+
```

```
\langle Eq\_or\_Ast \rangle \mid \langle Eq\_or\_Ast \rangle \langle Equation\_List \rangle
(Equation_List)
\langle Eq\_or\_Ast \rangle
                                        \langle Equation \rangle \mid \langle Assertion \rangle
                               ::=
                                        (Left_Part) "=" (Right_Part) (P) ";"
\langle Equation \rangle
                               ::=
                               ::= "(" \Left_List\) ")" | \Left_List\
(Left_Part)
                               ::= \langle Left \rangle ("," \langle Left \rangle)^*
⟨Left_List⟩
                               ::= \(\lambda \text{Identifier} \rangle \lambda \text{Left} \rangle \( \text{Selector} \rangle \)
\langle Left \rangle
                                       "." \(\text{Ident}\) | "[" \(\text{Expression}\) [ \(\text{SelTrancheEnd}\) ] "]"
\langle Selector \rangle
                               ::=
(SelTrancheEnd)
                               ::= ".." \langle Expression \rangle
                                        "assert" \langle Expression \rangle \langle P \rangle ";"
\langle Assertion \rangle
                               ::=
```

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```
\langle Expression \rangle
                           ::= \langle Identifier \rangle
                                   ⟨Value⟩
                                   "(" \(Expression_List\)")"
                                   \langle Record\_Exp \rangle
                                   \langle Array\_Exp \rangle
                                   ⟨Unary⟩ ⟨Expression⟩
                                   (Expression) (Binary) (Expression)
                                   ⟨Nary⟩ ⟨Expression⟩
                                   "if" (Expression) "then" (Expression) "else" (Expression)
                                   \langle Call \rangle
                                   (Expression) (Selector)
                           ::= \langle Expression \rangle \mid \langle Expression \rangle "," \langle Expression List \rangle
(Expression_List)
                           ::= \(\lambda Ident\rangle\) "\{" \(\rangle Field_Exp_List\rangle\)\"\}"
\langle Record\_Exp \rangle
                           ::= \langle Field_Exp \rangle \langle Field_Exp_List \rangle
〈Field_Exp_List〉
〈Field_Exp〉
                           ::= \langle Ident \rangle "=" \langle Expression \rangle
                           ::= "[" ⟨Expression_List⟩ "]" | ⟨Expression⟩ "^ " ⟨Expression⟩
\langle Array\_Exp \rangle
                           ::= \langle User\_Op \rangle \langle P \rangle "(" \langle Expression\_List \rangle")"
\langle Call \rangle
                           ::= \langle Identifier \rangle
⟨User_Op⟩
                                   \(\lambda \text{Iterator}\rangle << \lambda \text{User_Op}\rangle "," \lambda \text{Expression}\rangle >>
                                 "map" | "red" | "fill" | "fillred" | "boolred"
\langle Iterator \rangle
                           ::=
```

```
\langle Unary \rangle \text{ ::= "-" | "not"} 
\langle Binary \rangle \text{ ::= "+" | "-" | "*" | "/" | "div" | "mod" | "or" | "<=" | "<>" | "<=" | "<>" | "=" | "cr" | "=" | "cr" | "=>" | "\langle Nary \rangle \text{ ::= "$\psi'' | "nor"}
```

```
\langle Unary \rangle ::= "pre" | "current" \langle Binary \rangle ::= | "->" | "when" | "fby"
```

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```
\langle node-def \rangle ::= \langle node \rangle \langle ident \rangle = \langle node-exp \rangle;
```

```
\langle Program \rangle ::= (\langle Package \rangle \mid \langle Model \rangle \mid \langle Model Instance \rangle)^*
```

```
(Package)
                           ::=
                                 ⟨Package_Header⟩ [ ⟨Package_Body⟩ ] "end"
(Package_Header)
                                 "package" \langle Ident \rangle \langle \mathcal{P} \rangle
                          ::=
                                        ["uses" \langle Ident\_List \rangle]
                                        "provides" \langle Package Params\rangle
(Package_Params)
                           ::= (\langle Package\_Param \rangle)^+
                                 "const" (Ident) ":" (Type_Identifier) (P) ";"
(Package_Param)
                                 "type" \langle Type\_Ident\_List \rangle \langle P \rangle ";"
                                 (Function_Header)
                                 (Node_header)
(Type_Identifier)
                           ::= \langle Identifier \rangle
                          ::= \(\lambda Ident\rangle\ ";" \| \lambda Ident\rangle\ "," \lambda Type_Ident_List\rangle
(Type_Ident_List)
```

```
 \langle Model \rangle \qquad ::= \langle Model Header \rangle \left[ \langle Body \rangle \right] \text{``end''} 
 \langle Model Header \rangle \qquad ::= \text{``model''} \langle Ident \rangle \langle \mathcal{P} \rangle 
 \left[ \text{``uses''} \langle Ident List \rangle \right] 
 \text{``needs''} \langle Package Params \rangle 
 \text{``provides''} \langle Package Params \rangle
```

```
\langle Model\_Instance \rangle \quad ::= \quad \text{``package''} \langle Ident \rangle \\ \quad [\text{``uses''} \langle Ident\_List \rangle \text{]} \\ \quad \text{``is''} \langle Ident \rangle \text{``(''} \langle Model\_Actual\_List \rangle \text{'`)''} \langle \mathcal{P} \rangle \text{``;''} \\ \langle Model\_Actual\_List \rangle \quad ::= \quad \langle Model\_Actual \rangle \mid \langle Model\_Actual \rangle \text{``,''} \langle Model\_Actual\_List \rangle \\ \langle Model\_Actual \rangle \quad ::= \quad \langle Identifier \rangle \langle \mathcal{P} \rangle \mid \langle Expression \rangle \langle \mathcal{P} \rangle
```

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```
 \begin{array}{lll} \langle \textit{Package\_Body} \rangle & ::= & [~\textbf{``body''}~] \langle \textit{Entity\_Decl} \rangle^+ \\ \langle \textit{Entity\_Decl} \rangle & ::= & \langle \textit{Const\_Decl} \rangle \\ & & | & \langle \textit{Type\_Decl} \rangle \\ & & | & \langle \textit{Model\_Instance} \rangle \\ & & | & \langle \textit{Function\_Decl} \rangle \\ & & | & \langle \textit{Node\_Decl} \rangle \end{array}
```

A.2 The syntax rules (automatically generated)

Lexical rules:

- *Ident* is an identifier, following the C standard.
- *IdentRef* is either an identifier, or a long identifier, that is an two identifiers separated by a double colon (*Ident*::*Ident*).
- *IntConst* is a integer notation, following the C standard.
- *RealConst* is a floating-point notation, following the C standard.

```
{ Include } ( PackBody | PackList )
program
PackList
                            OnePack { OnePack }
OnePack
                            ModelDecl | PackDecl | PackEq
Include
                            include "<string>"
                       ::=
Provides
                            [provides Provide; { Provide; } ]
                            const Lv6Id : Type [ = Expression ]
Provide
                            unsafe node Lv6Id StaticParams Params returns
                            node Lv6Id StaticParams Params returns Params
                            unsafe function Lv6Id StaticParams Params returns
                            function Lv6Id StaticParams Params returns Params
                            type OneTypeDecl
ModelDecl
                            model Lv6Id Uses needs StaticParamList; Provides
                            body PackBody end
PackDecl
                            package Lv6Id Uses Provides body PackBody end
                            uses Lv6Id { , Lv6Id } ;
Uses
Eq_or_Is
                            =
                       ::=
                            is
PackEq
                            package Lv6Id Eq_or_Is Lv6Id ( ByNameStaticArgList )
PackBody
                            OneDecl { OneDecl }
```

```
OneDecl
                            ConstDecl | TypeDecl | ExtNodeDecl | NodeDecl
TypedLv6IdsList
                       ::=
                            TypedLv6Ids { ; TypedLv6Ids }
TypedLv6Ids
                       ::=
                            Lv6Id \{ , Lv6Id \} : Type
TypedValuedLv6Ids
                       ::=
                            TypedValuedLv6Id { ; TypedValuedLv6Id }
TypedValuedLv6Id
                       ::=
                            Lv6Id (: Type | , Lv6Id { , Lv6Id } : Type | : Type =
                            Expression)
Const Decl
                            const ConstDeclList
                       ::=
ConstDeclList
                            OneConstDecl; { OneConstDecl; }
OneConstDecl
                            Lv6Id (: Type | , Lv6Id { , Lv6Id } : Type | : Type =
                            Expression \mid = Expression
TypeDecl
                            type TypeDeclList
                       ::=
TypeDeclList
                       ::=
                            OneTypeDecl; { OneTypeDecl; }
OneTypeDecl
                       ::=
                            Lv6Id = ( Type | enum { Lv6Id { , Lv6Id } } | [ struct
                             [ { TypedValuedLv6Ids [ ; ] }
Type
                            (bool | int | real | Lv6IdRef ) { ^ Expression }
                       ::=
ExtNodeDecl
                            extern function unsafe extern function
                       ::=
                             extern node unsafe extern node Lv6Id Params
                            returns Params ;
NodeDecl
                            LocalNode
LocalNode
                            node Lv6Id StaticParams Params returns Params ;
                            LocalDecls Body ( . | [; ])
                            function Lv6Id StaticParams Params returns Params
                            [;] LocalDecls Body ( . | [;])
                            node Lv6Id StaticParams NodeProfileOpt = EffectiveNode
                             ;
                            function Lv6Id StaticParams NodeProfileOpt =
                            EffectiveNode ;
                            unsafe node Lv6Id StaticParams Params returns
                            Params [; ] LocalDecls Body (. | [; ])
                            unsafe function Lv6Id StaticParams Params returns
                            Params [; ] LocalDecls Body (. | [; ])
                            unsaf e node Lv6Id StaticParams NodeProfileOpt =
                            EffectiveNode [;]
                            unsafe function Lv6Id StaticParams NodeProfileOpt =
                            EffectiveNode [;]
NodeProfileOpt
                             [ Params returns Params ]
StaticParams
                            << StaticParamList >> ]
                       ::=
```

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```
StaticParamList
                             StaticParam { ; StaticParam }
StaticParam
                             type Lv6Id
                             const Lv6Id: Type
                             node Lv6Id Params returns Params
                             function Lv6Id Params returns Params
                             unsafe node Lv6Id Params returns Params
                             unsafe function Lv6Id Params returns Params
Params
                             ( [ VarDeclList [ ; ] ] )
                        ::=
LocalDecls
                             [LocalDeclList]
                        ::=
LocalDeclList
                             OneLocalDecl { OneLocalDecl }
OneLocalDecl
                             LocalVars
                             LocalConsts
LocalConsts
                             const ConstDeclList
                        ::=
LocalVars
                             var VarDeclList ;
                        ::=
VarDeclList
                             VarDecl { ; VarDecl }
VarDecl
                             TypedLv6Ids
                             TypedLv6Ids when ClockExpr
                             ( TypedLv6IdsList ) when ClockExpr
                             let [ EquationList ] tel
Body
                        ::=
EquationList
                        ::=
                             Equation { Equation }
Equation
                             (assert | Left = ) Expression;
                        ::=
Left
                             LeftItemList
                             ( LeftItemList )
LeftItemList
                        ::=
                             LeftItem { , LeftItem }
LeftItem
                             Lv6Id
                             FieldLeftItem
                             TableLeftItem
FieldLeftItem
                             LeftItem . Lv6Id
TableLeftItem
                             LeftItem [ ( Expression | Select ) ]
Expression
                             Constant
                             Lv6IdRef
                             not Expression
                             - Expression
                             pre Expression
```

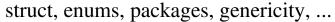
current Expression int Expression real Expression Expression when ClockExpr Expression **fby** Expression *Expression* -> *Expression* Expression and Expression Expression or Expression Expression **xor** Expression Expression => Expression *Expression* = *Expression* Expression <> Expression Expression < Expression *Expression* <= *Expression Expression* > *Expression Expression* >= *Expression* Expression div Expression Expression mod Expression Expression - Expression Expression + Expression Expression / Expression *Expression* * *Expression* if Expression then Expression else Expression with Expression then Expression else Expression **#** (ExpressionList) nor (ExpressionList) *CallByPosExpression* [ExpressionList] Expression * Expression Expression | Expression Expression [Expression]

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```
Expression [ Select ]
                             Expression . Lv6Id
                             CallByNameExpression
                             ( ExpressionList )
                             merge Lv6Id MergeCaseList
MergeCaseList
                             [ MergeCase ] { MergeCase }
                        ::=
MergeCase
                             [((Lv6IdRef | true | false) -> Expression)]
                        ::=
ClockExpr
                        ::=
                             Lv6IdRef (Lv6Id)
                             Lv6Id
                             not Lv6Id
                             not ( Lv6Id )
PredefOp
                             not | fby | pre | current | -> | and | or | xor | => | = |
                             <> | < | <= | > | >= | div | mod | - | + | / | * | if
CallByPosExpression
                             EffectiveNode (ExpressionList)
EffectiveNode
                             Lv6IdRef [ << StaticArgList >> ]
StaticArgList  
                             StaticArg { ( , | ; ) StaticArg }
StaticArg
                             type Type
                        ::=
                             const Expression
                             node EffectiveNode
                             function EffectiveNode
                             PredefOp
                             SimpleExp
                             SurelyType
                             SurelyNode
ByNameStaticArgList
                             ByNameStaticArg { (, |; ) ByNameStaticArg }
ByNameStaticArg
                        ::=
                             type Lv6Id = Type
                             const Lv6Id = Expression
                             node Lv6Id = EffectiveNode
                             function Lv6Id = EffectiveNode
                             Lv6Id = PredefOp
                             Lv6Id = SimpleExp
                             Lv6Id = SurelyType
                             Lv6Id = SurelyNode
```

```
SurelyNode
                            Lv6IdRef << StaticArgList >>
SurelyType
                            ( bool | int | real ) { ^ Expression }
                       ::=
SimpleExp
                            Constant
                            Lv6IdRef
                            SimpleTuple
                            not SimpleExp
                            - SimpleExp
                            SimpleExp and SimpleExp
                            SimpleExp or SimpleExp
                            SimpleExp xor SimpleExp
                            SimpleExp => SimpleExp
                            SimpleExp = SimpleExp
                            SimpleExp <> SimpleExp
                            SimpleExp < SimpleExp
                            SimpleExp <= SimpleExp
                            SimpleExp > SimpleExp
                            SimpleExp >= SimpleExp
                            SimpleExp div SimpleExp
                            SimpleExp mod SimpleExp
                            SimpleExp - SimpleExp
                            SimpleExp + SimpleExp
                            SimpleExp / SimpleExp
                            SimpleExp * SimpleExp
                            if SimpleExp then SimpleExp else SimpleExp
SimpleTuple
                            ( SimpleExpList )
                       ::=
SimpleExpList
                       ::=
                            SimpleExp { , SimpleExp }
                            [Lv6IdRef { [ Lv6IdRef with ] CallByNameParamList [
CallByNameExpression
                       ::=
                            ; ] ] } ]
CallByNameParamList
                       ::=
                            CallByNameParam { (; ), CallByNameParam }
CallByNameParam
                       ::=
                            Lv6Id = Expression
```

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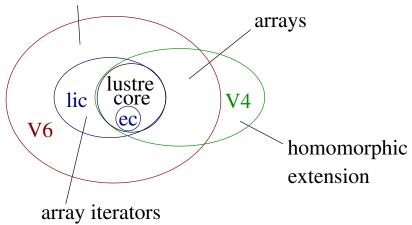


Figure A.1: Lustre potatoes

A.3 Lustre History

Lustre V1, v2, v3, ..., v6

A.4 Some Lustre V4 features not supported in Lustre V6

```
- recursive arrays slices : use iterators instead
[int, real] -> use structures instead
[int, int] -> use int^2 instead
```

Bibliography